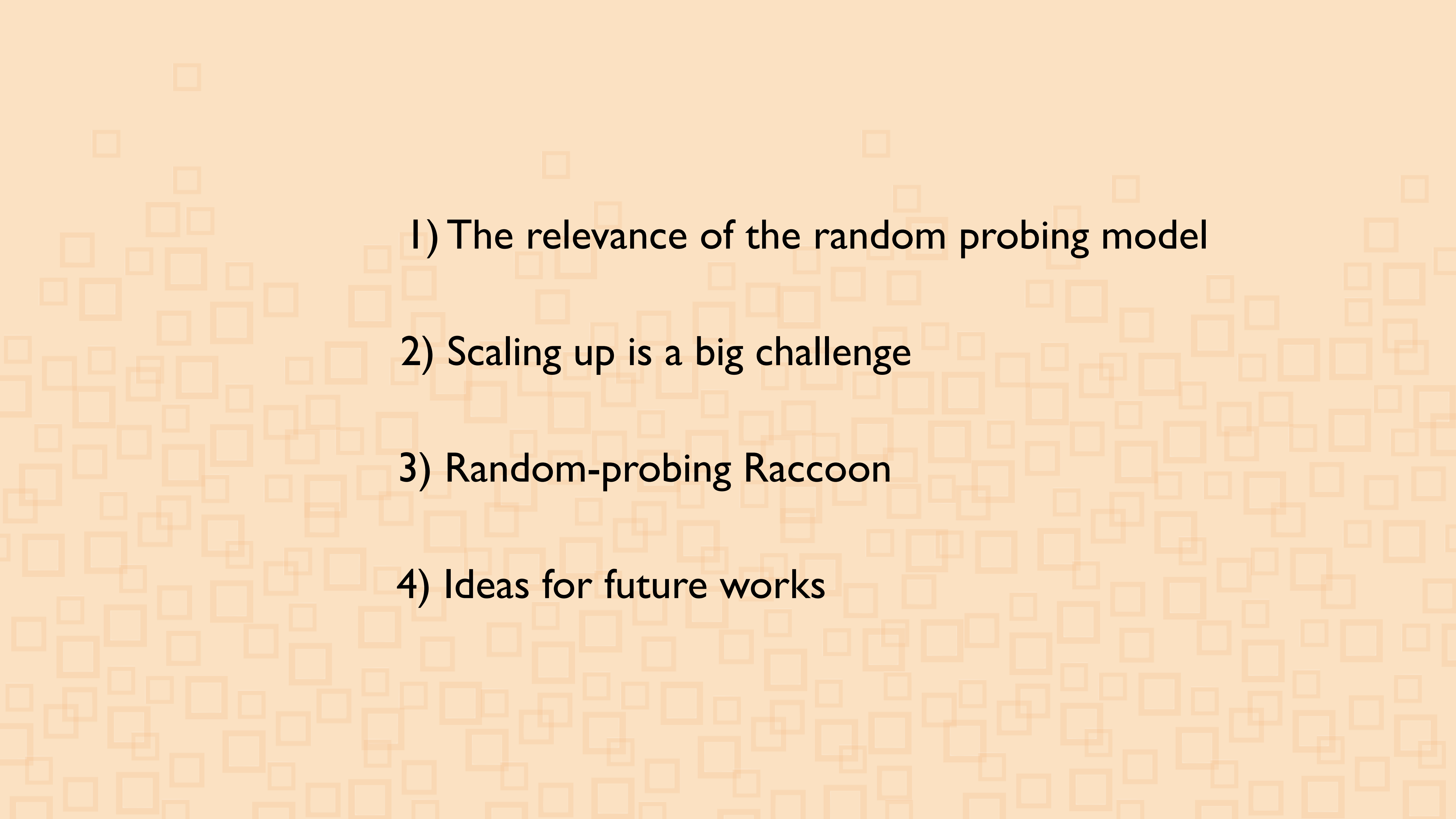


# The relevance and challenges of random probing security for post-quantum algorithms

## Application to Raccoon Signature Scheme

Mélissa Rossi

WRACH, Roscoff, 23/04/2025

- 
- 1) The relevance of the random probing model
  - 2) Scaling up is a big challenge
  - 3) Random-probing Raccoon
  - 4) Ideas for future works

1) The relevance of the random probing model

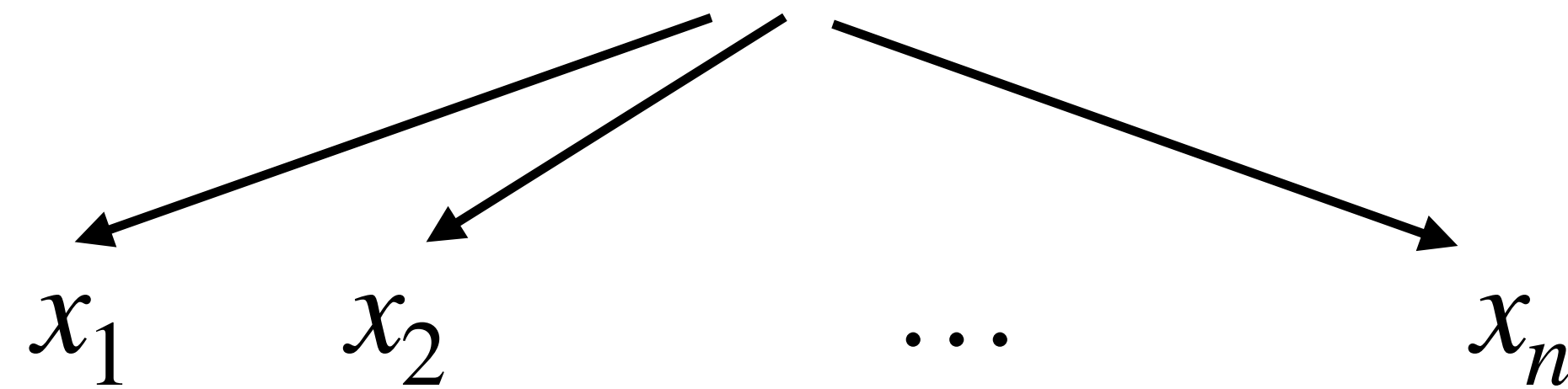
2) Scaling up is a big challenge

3) Random-probing Raccoon

4) Ideas for future works

# Masking

Sensitive variable  $x$



Each strict subset of  $(x_i)_{1 \leq i \leq n}$  is independent from  $x$

$$x_1, x_2, \dots, x_{n-1} \leftarrow \$$$

$$x_n \leftarrow x - (x_1 + x_2 + \dots + x_{n-1})$$

# Masking in Practice

## ■ Masking linear operations

$$z \leftarrow x \oplus y$$

$$x = x_0 \oplus x_1 \oplus \dots \oplus x_{n-1}$$

$$y = y_0 \oplus y_1 \oplus \dots \oplus y_{n-1}$$

$$\mathbf{z} = (x_0 \oplus y_0, x_1 \oplus y_1, \dots, x_{n-1} \oplus y_{n-1})$$

## ■ Masking non linear operations

- Cannot be done share by share
- Example of multiplication for  $n = 2$

$$x = x_0 \oplus x_1$$

$$y = y_0 \oplus y_1$$

$$z \leftarrow x_0y_0 \oplus x_0y_1 \oplus x_1y_0 \oplus x_1y_1$$

$$z_0 \leftarrow x_0y_0 \oplus x_0y_1$$

$$z_1 \leftarrow x_1y_1 \oplus x_1y_0$$

# From a gadget to a circuit

 $x_1$  $x_2$  $k_1$  $k_2$ 

## A Multiplication gadget

$$z_1 + z_2 = (x_1 + x_2) \cdot (k_1 + k_2)$$

$$r \leftarrow \$$$

$$z_1 \leftarrow x_1 k_1 + r$$

$$r' \leftarrow x_1 k_2 - r$$

$$r'' \leftarrow r' + x_2 k_1$$

$$z_2 \leftarrow r'' + x_2 k_2$$

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 $x_1$  $x_2$  $k_1$  $k_2$  $r$ 

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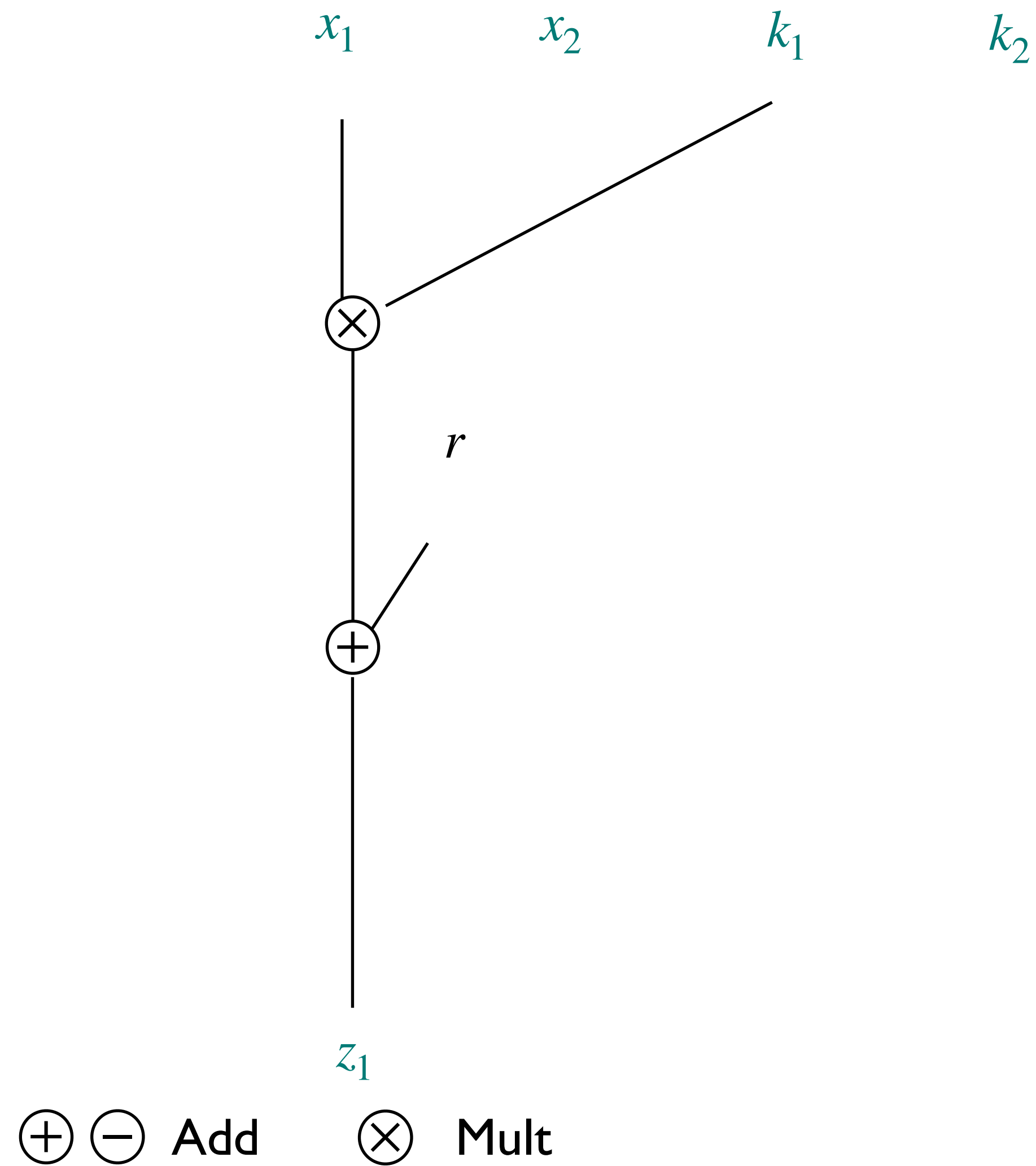
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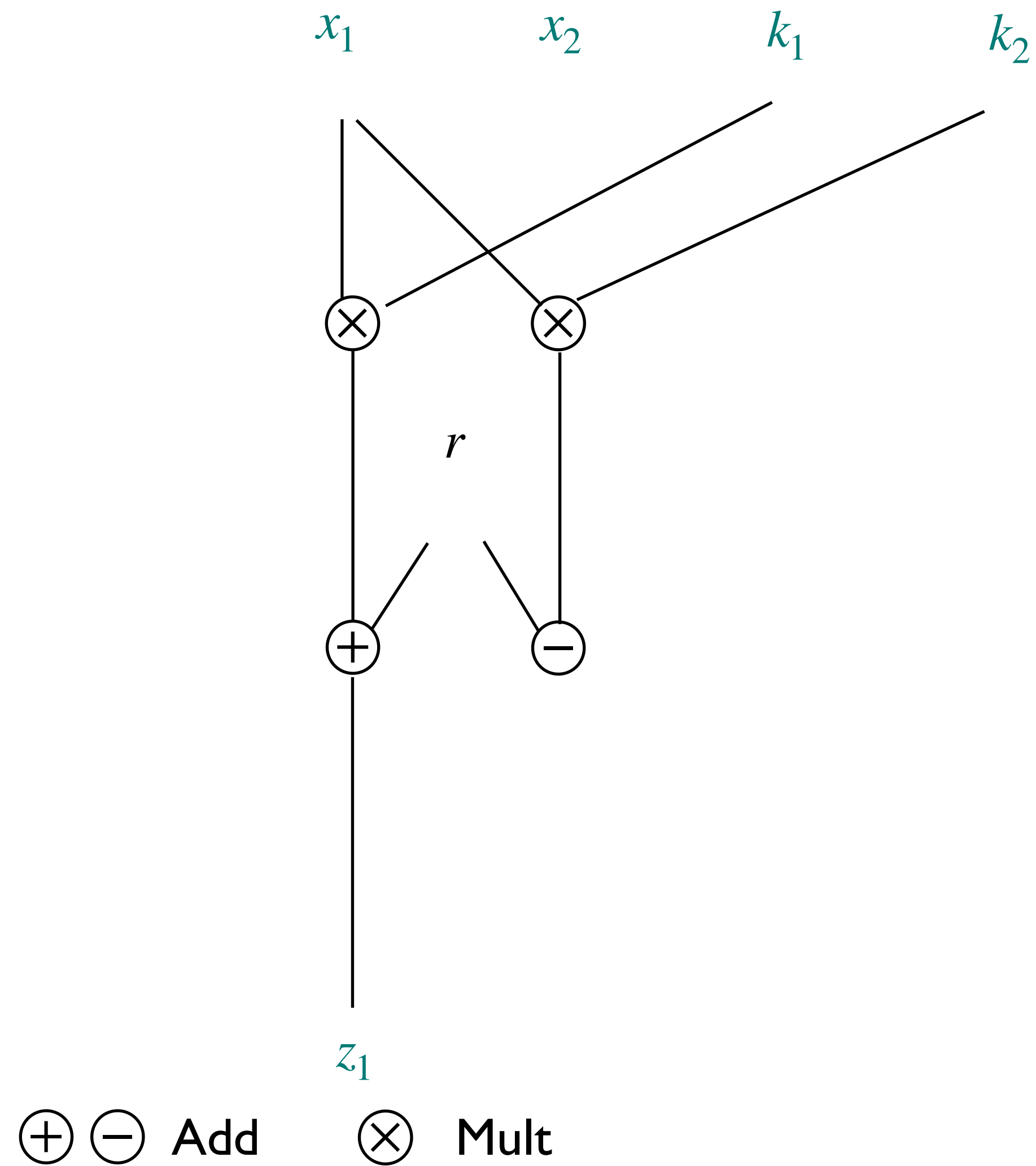
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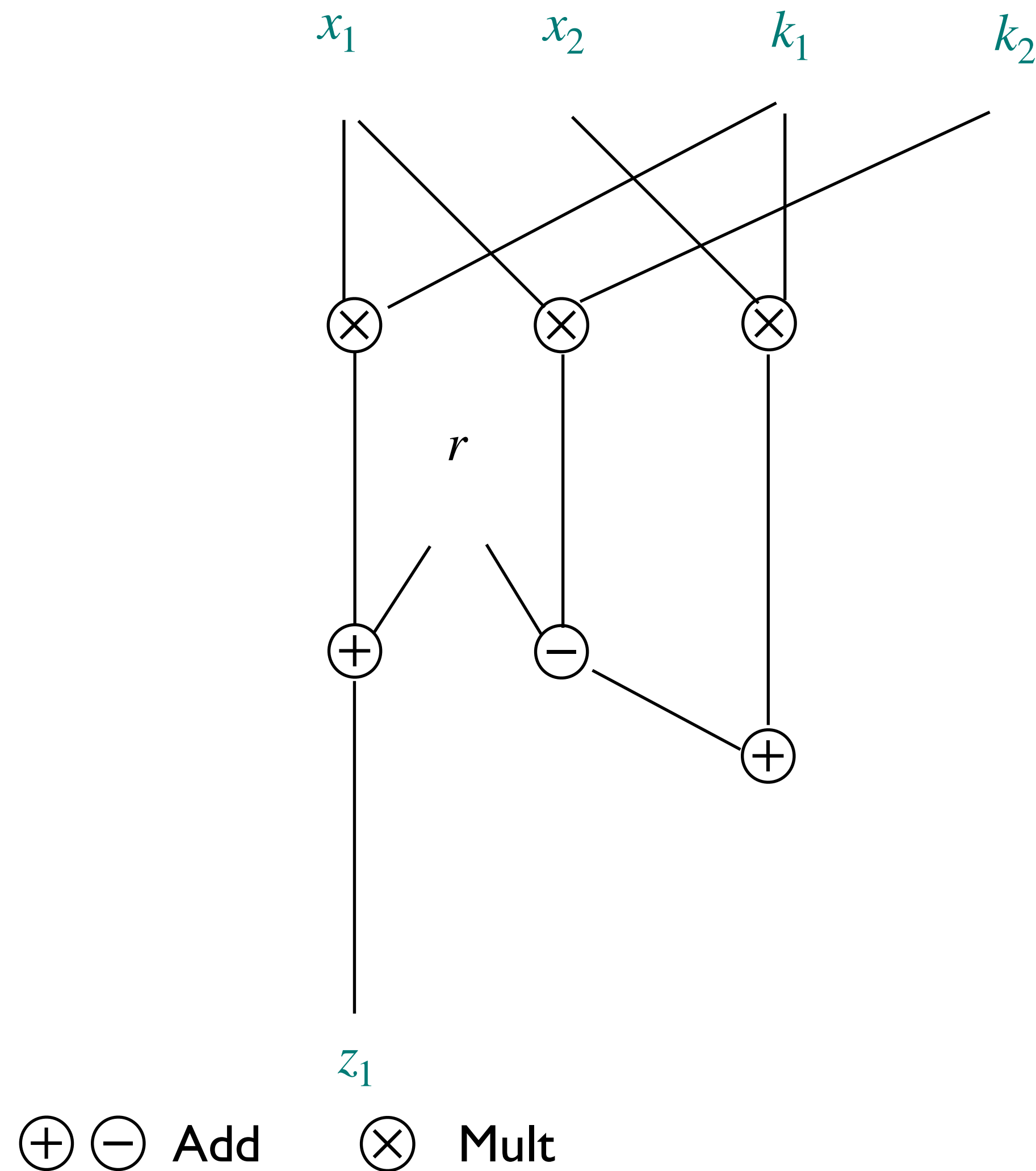
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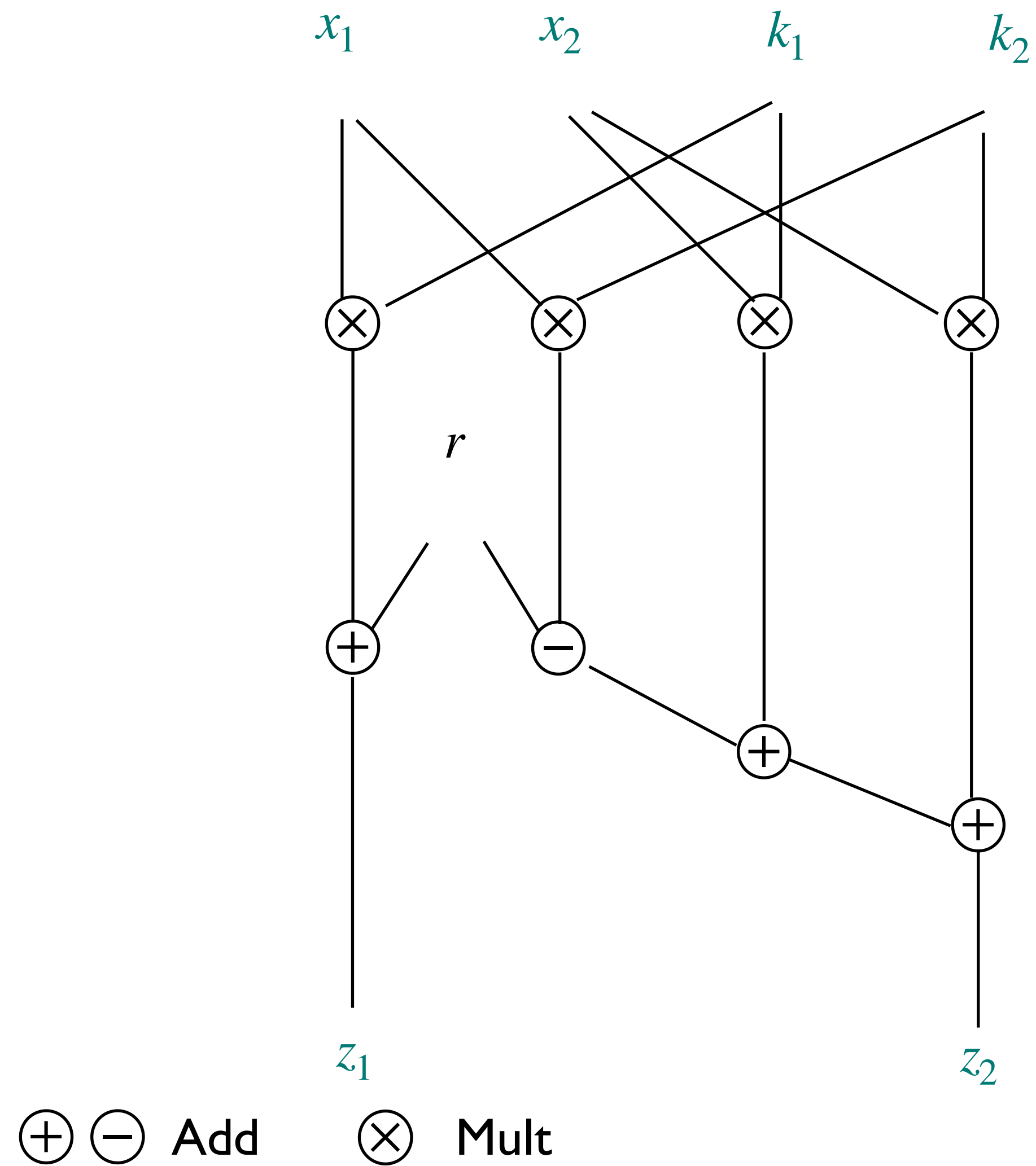
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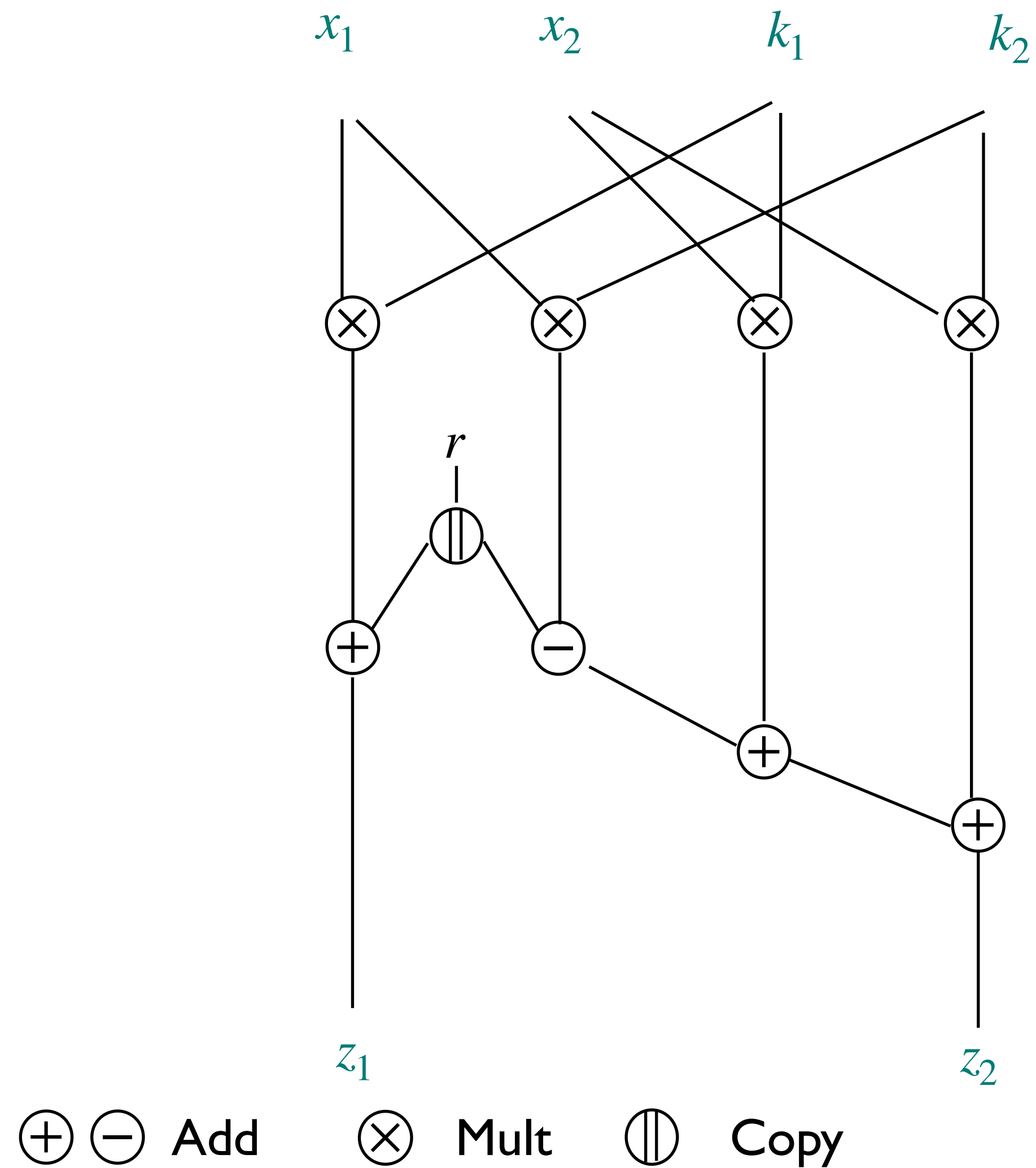
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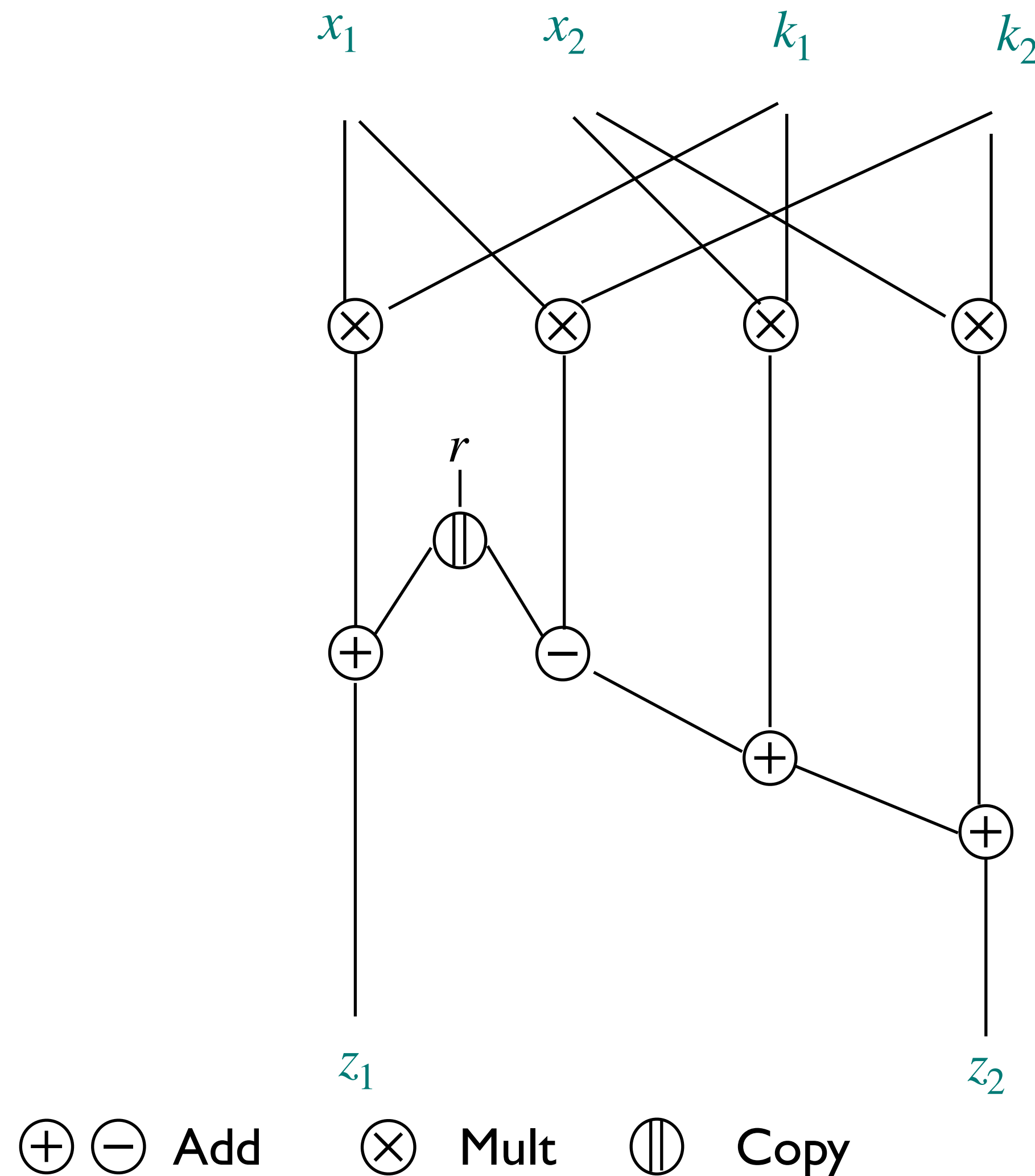
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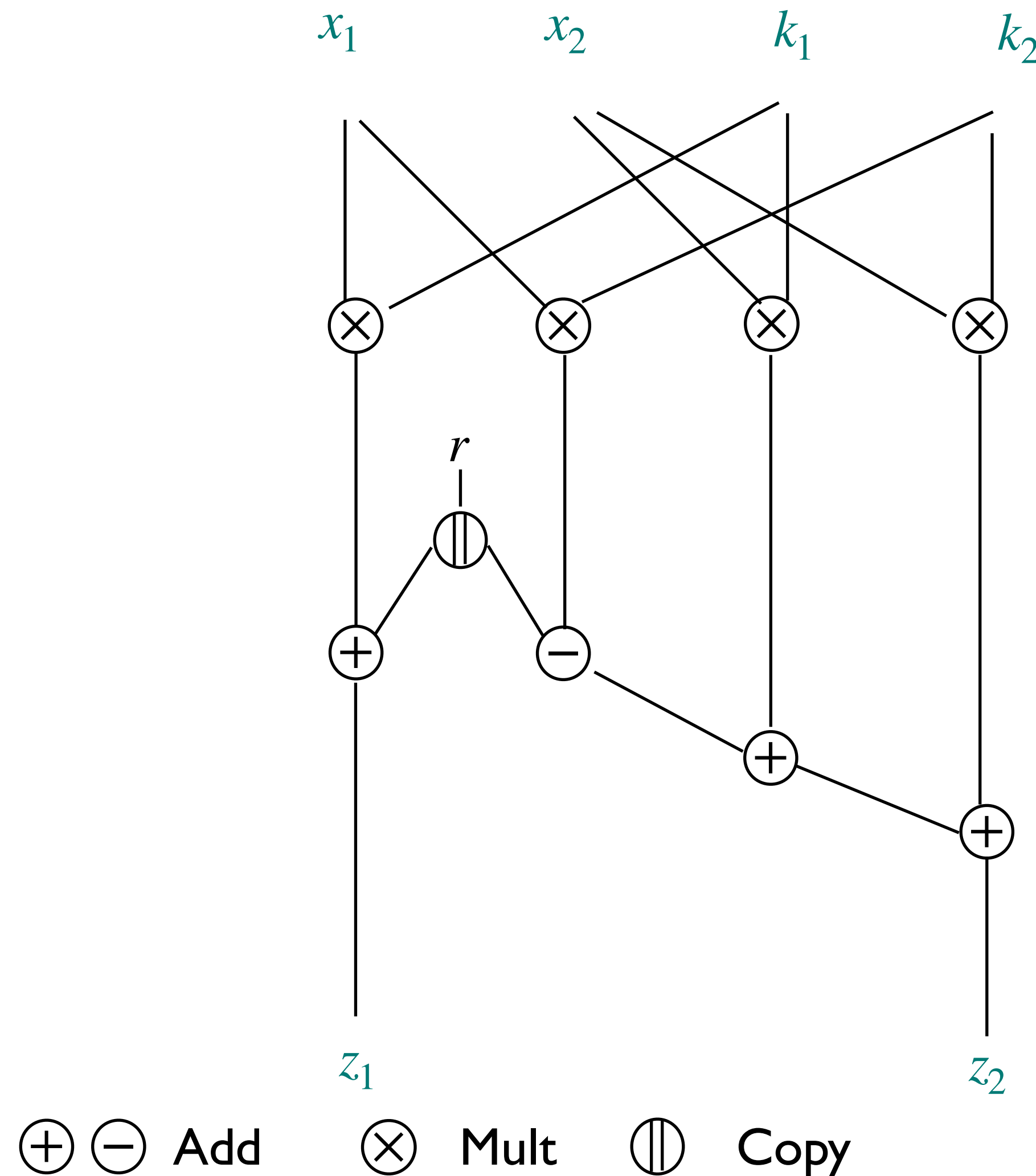
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## Attacker model

The attacker is given the design of the circuit and some **extra information** about the wires. He/she must not recover any information about  $x = \sum x_i$  and  $k = \sum k_i$ .

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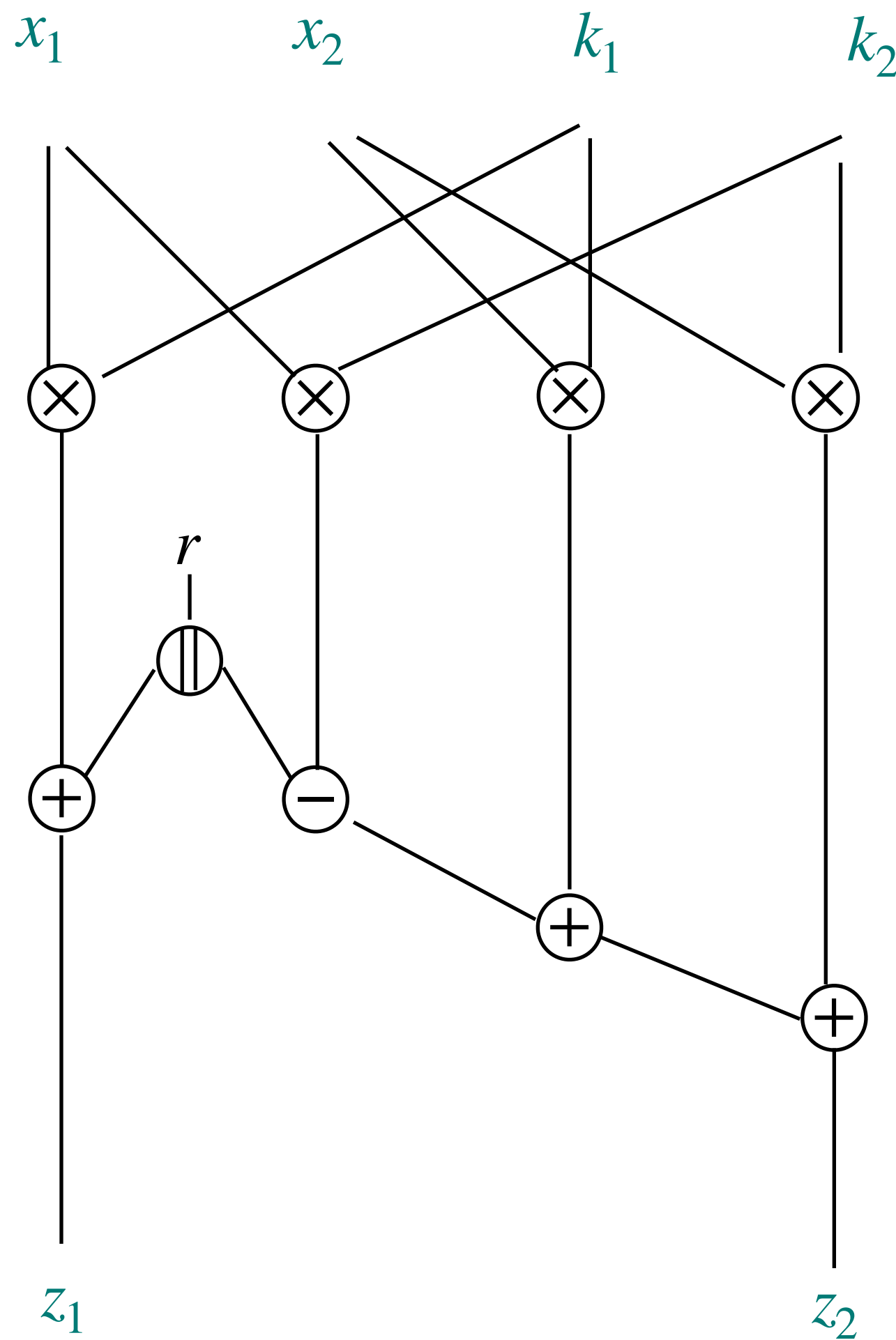
3 flavours

1. t-probing model
2. Random probing model
3. Noisy leakage model

# t-Probing model

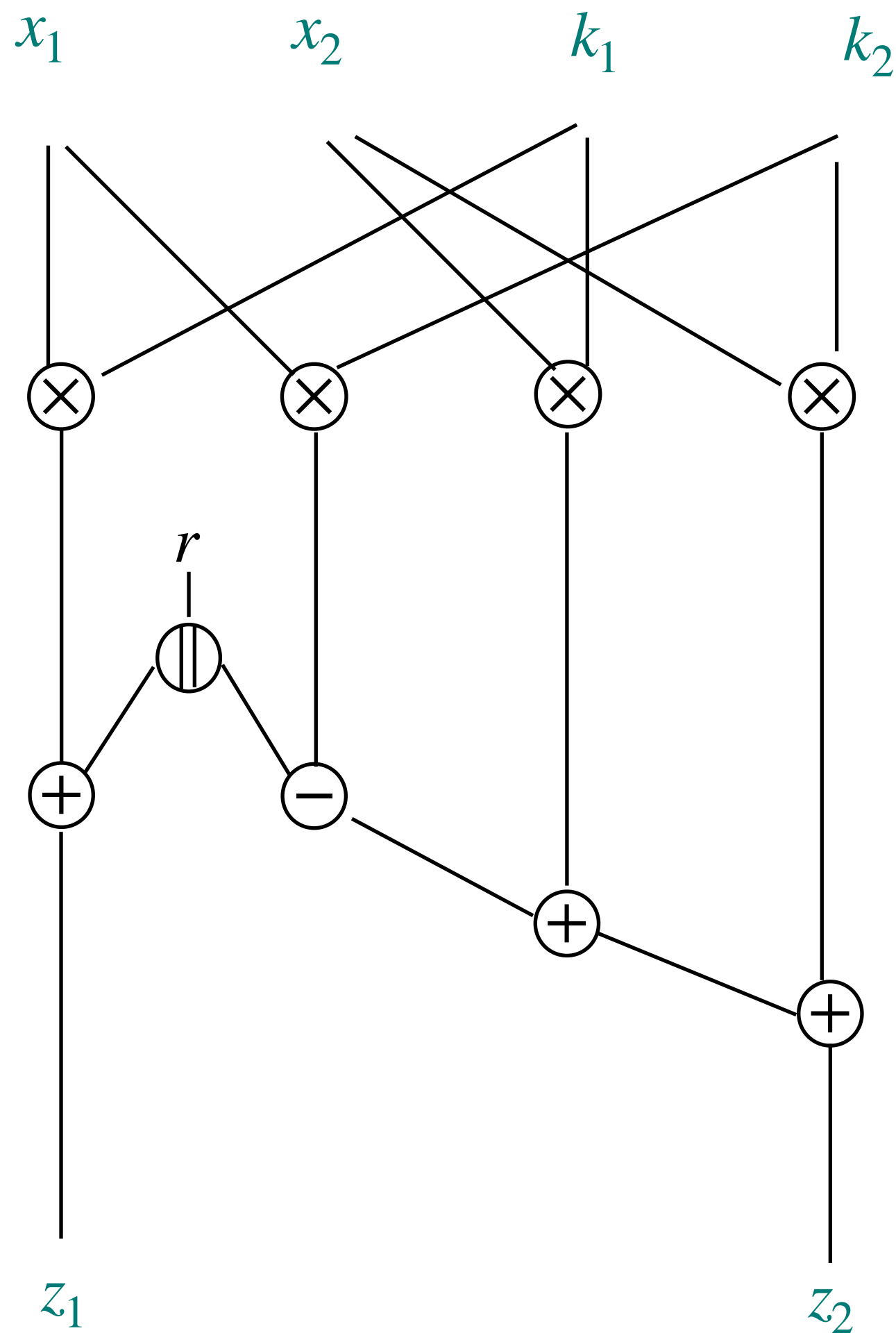
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The attacker can ask for the value of at most  $t$  wires.



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Let  $\mathcal{P}$  be a set of at most  $t$  probes :

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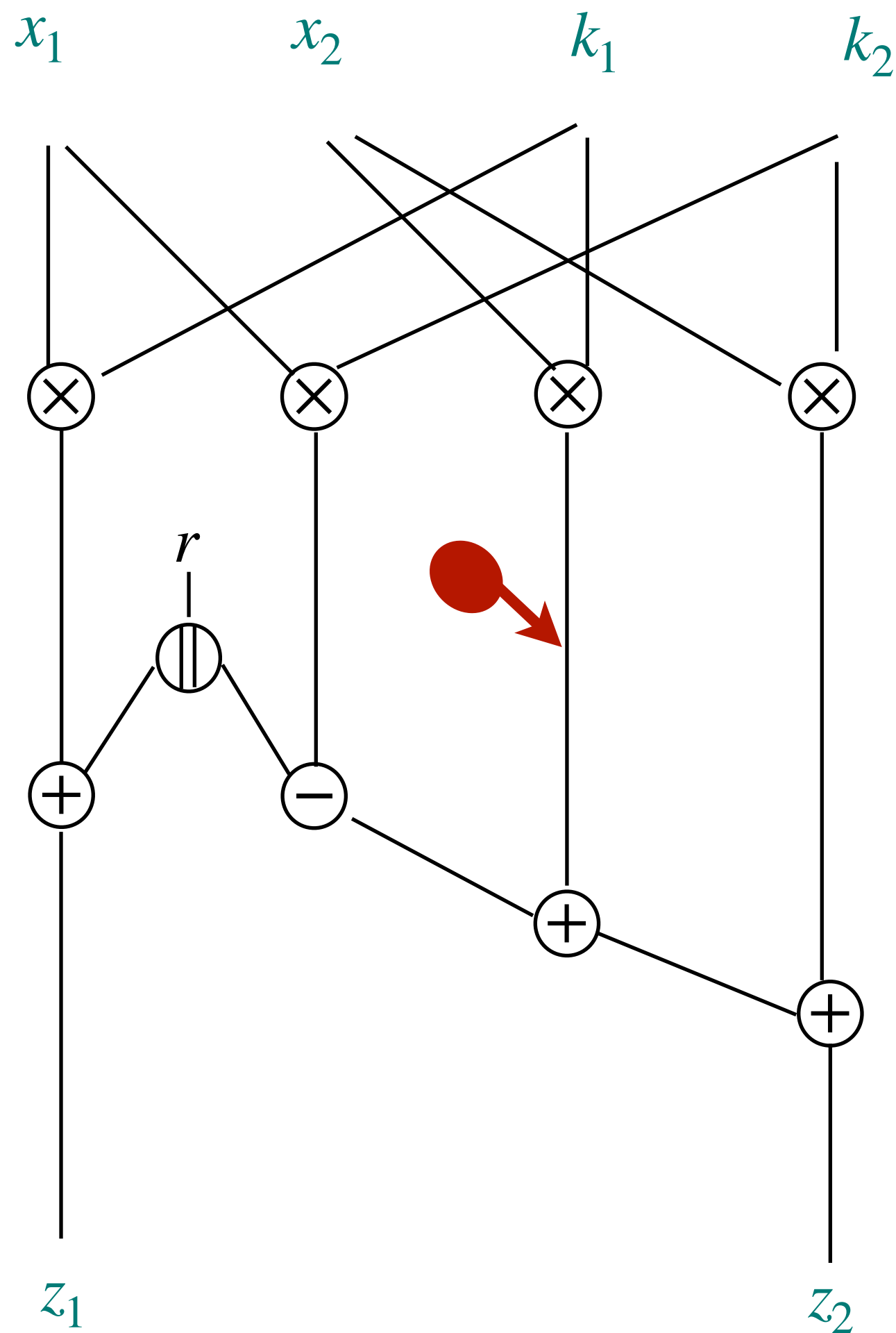
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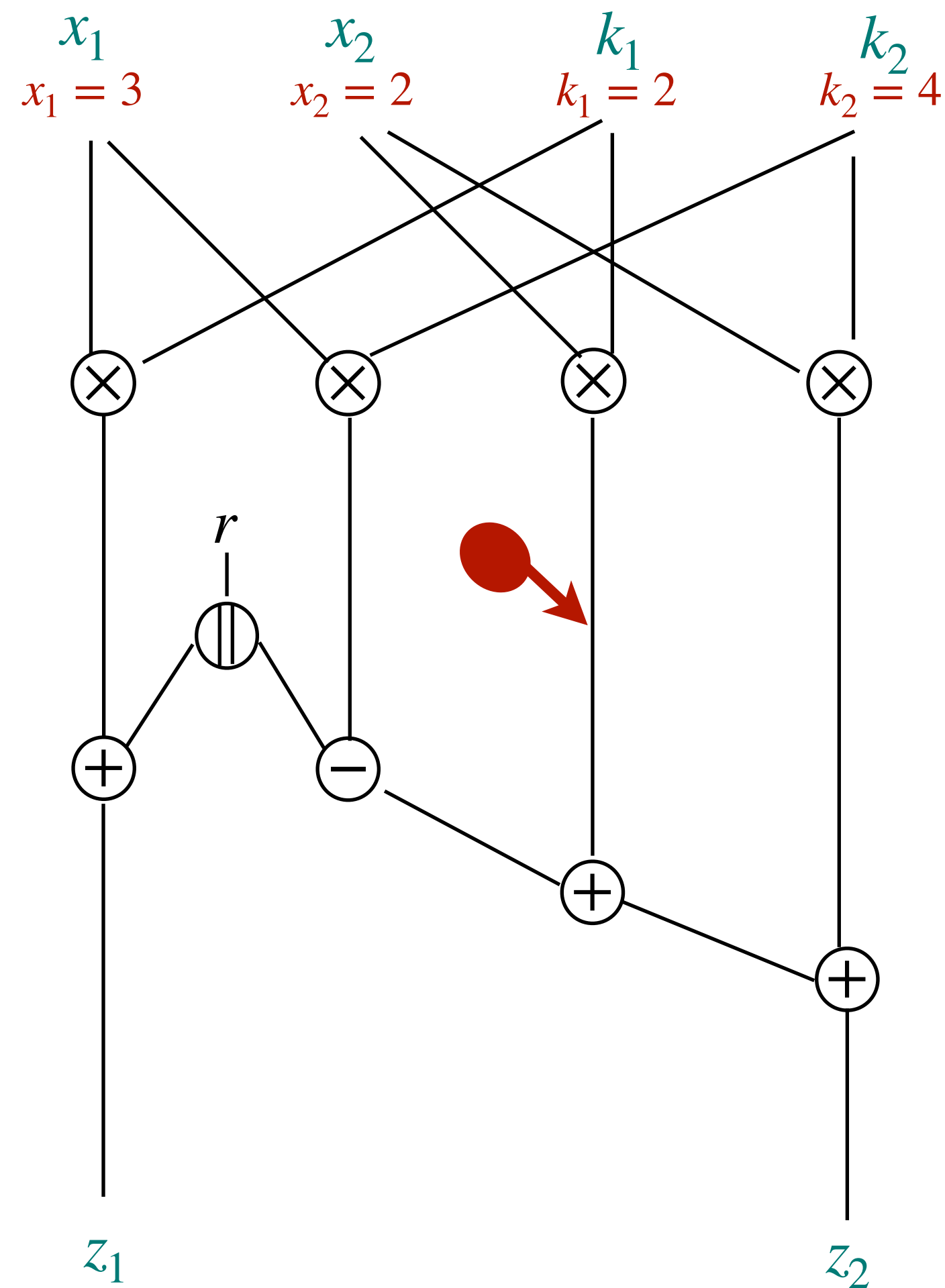
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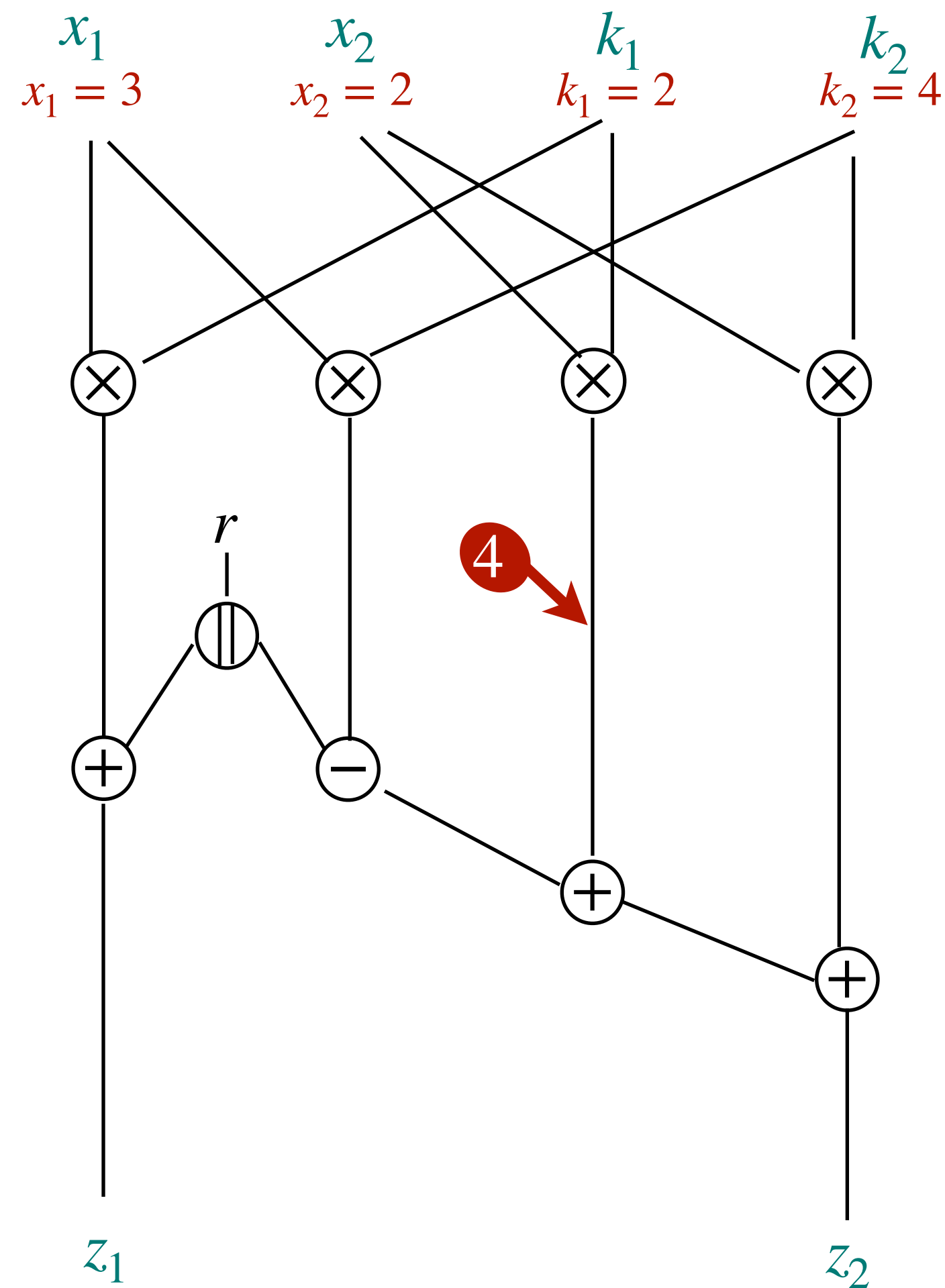
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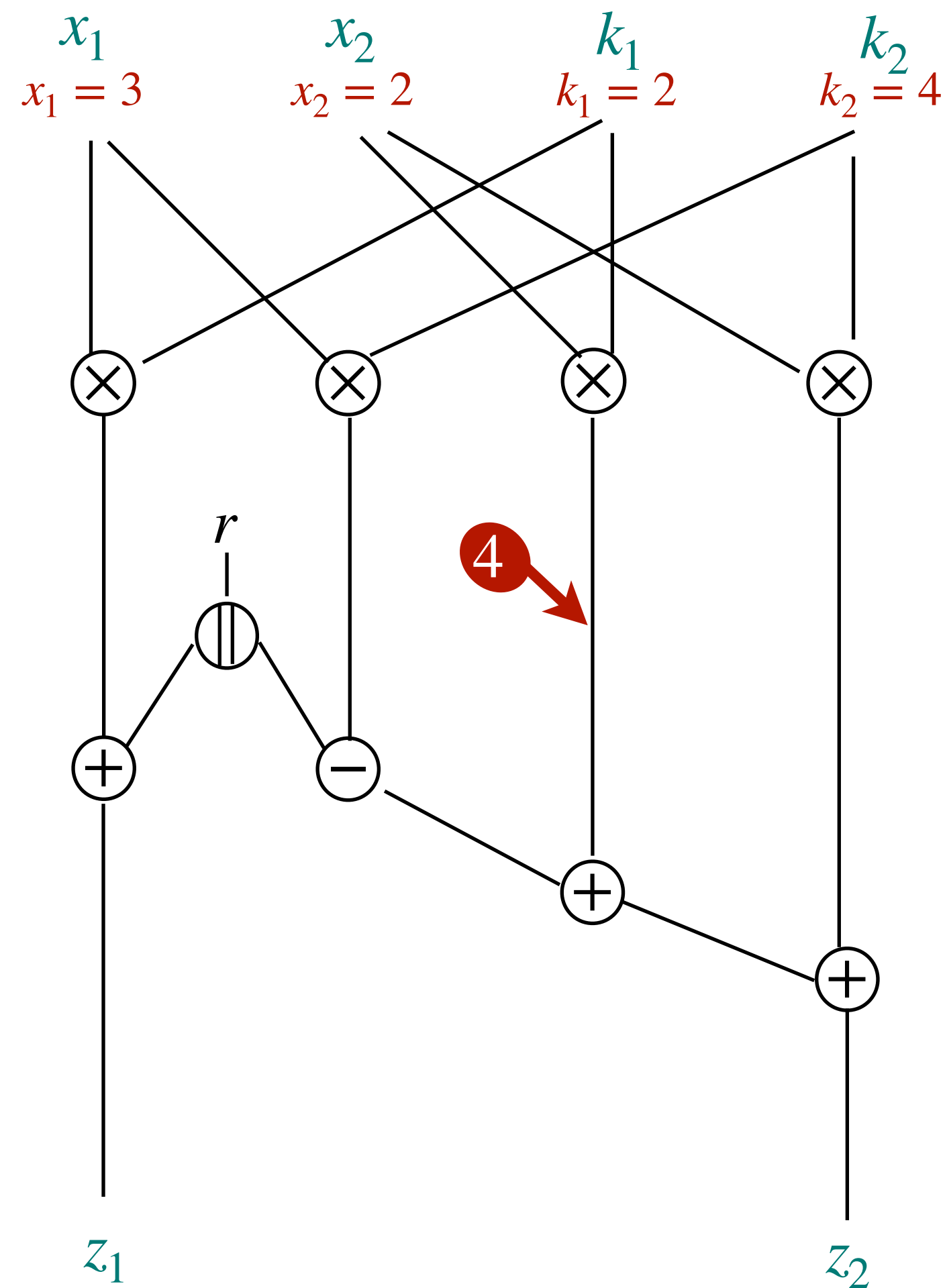
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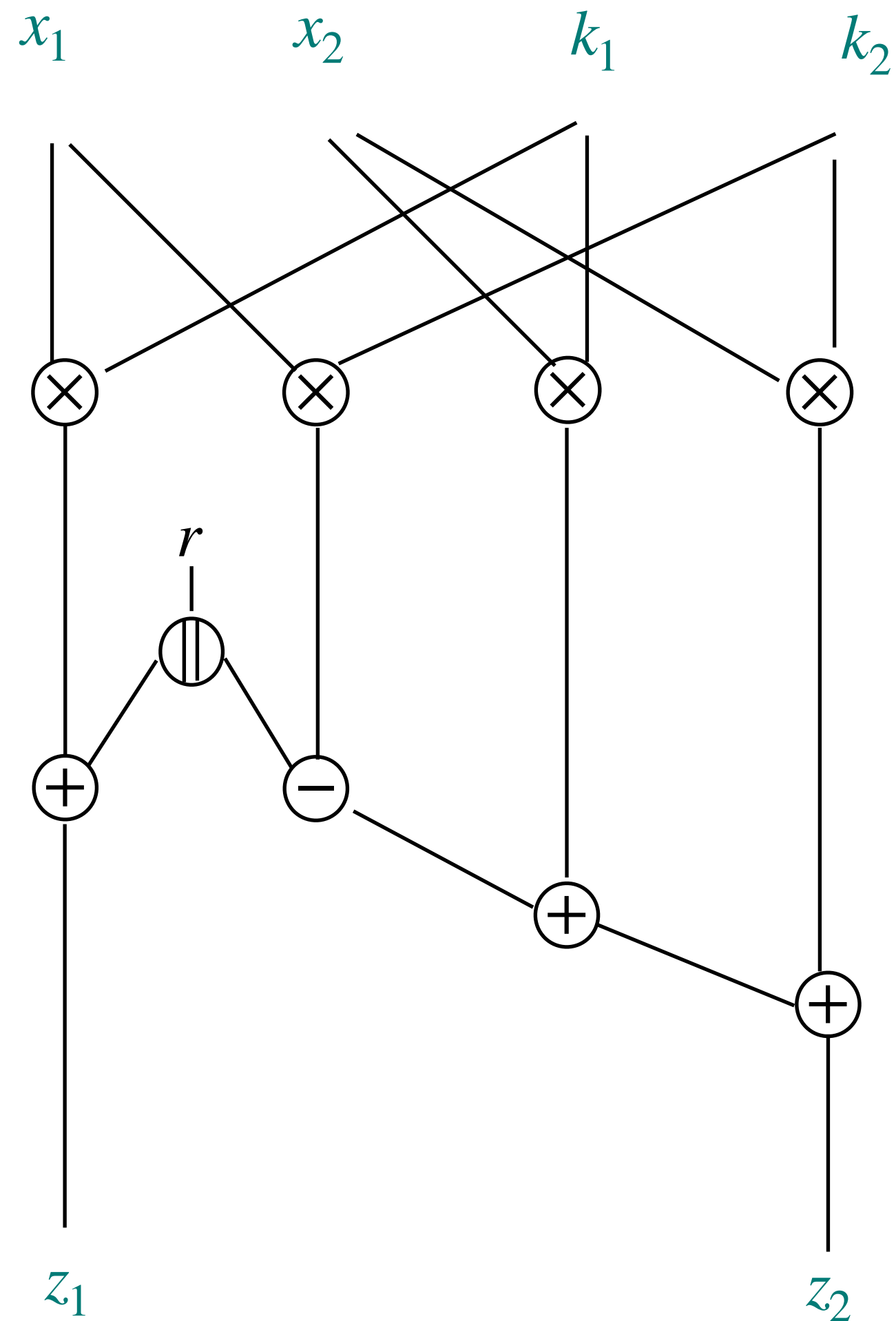
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Knowing  $\mathcal{L} = 4$  the probability of  $(x = 5, k = 6)$  is the same as for any other value.

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# t-Probing Security & composability



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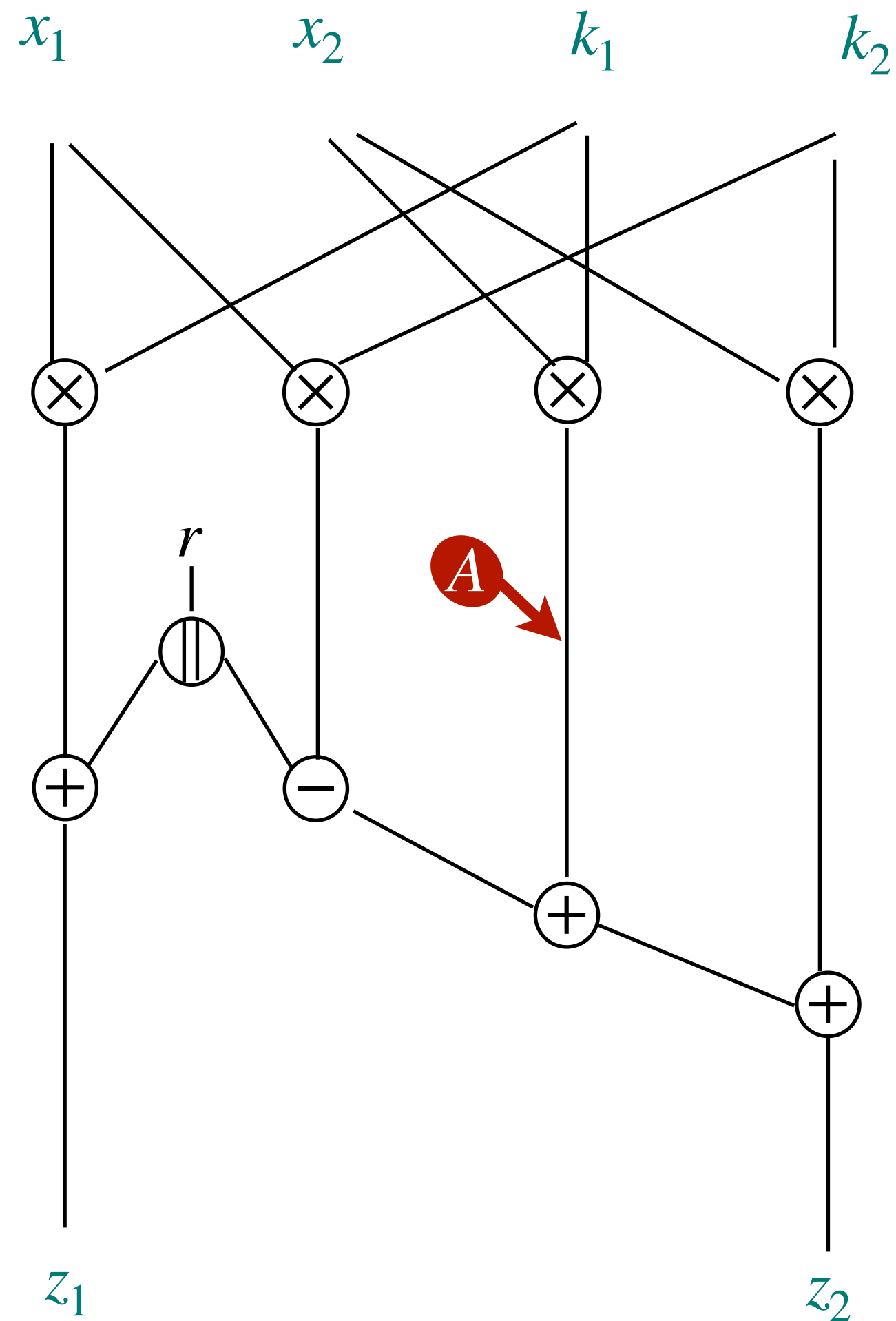
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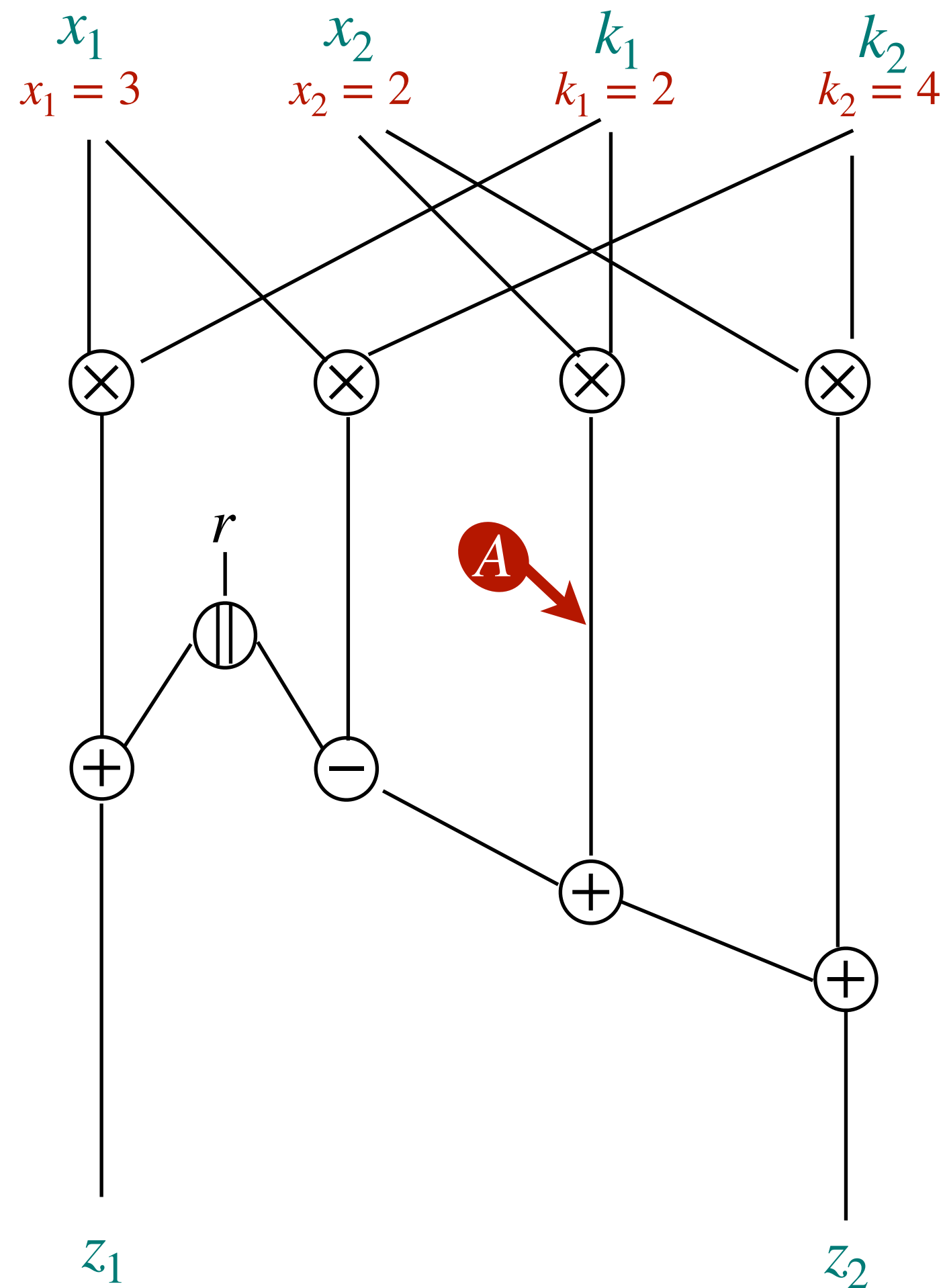
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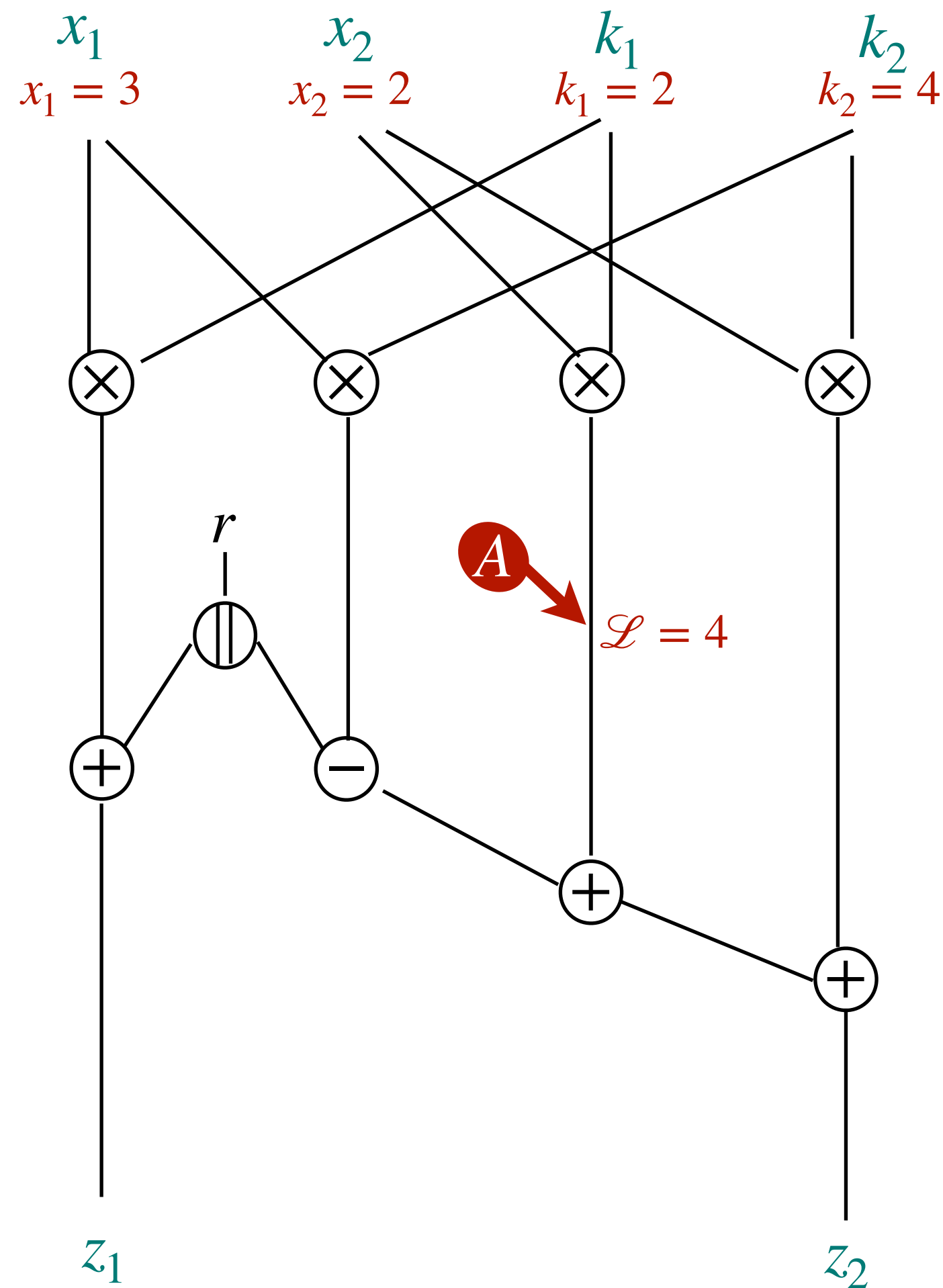
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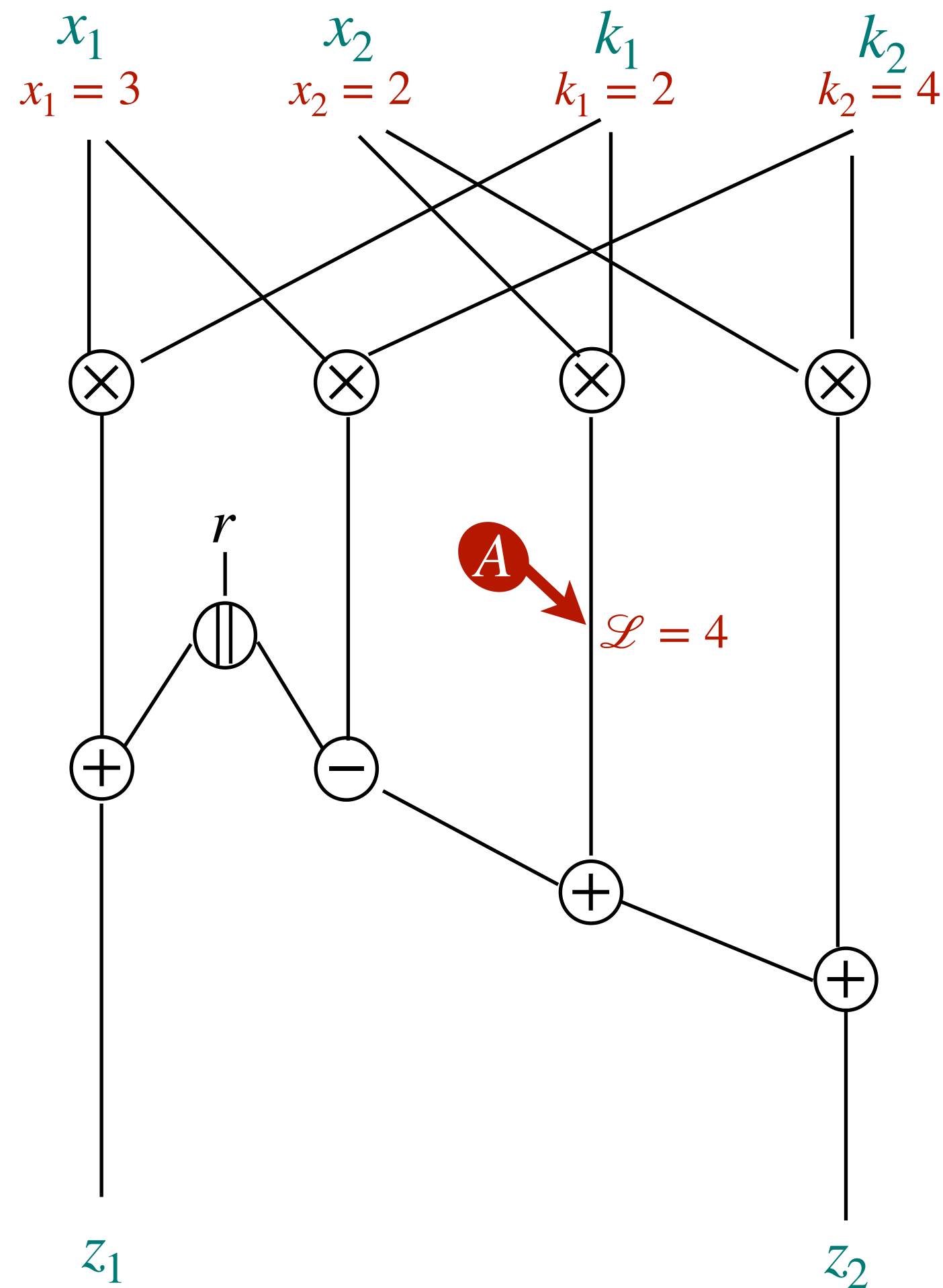
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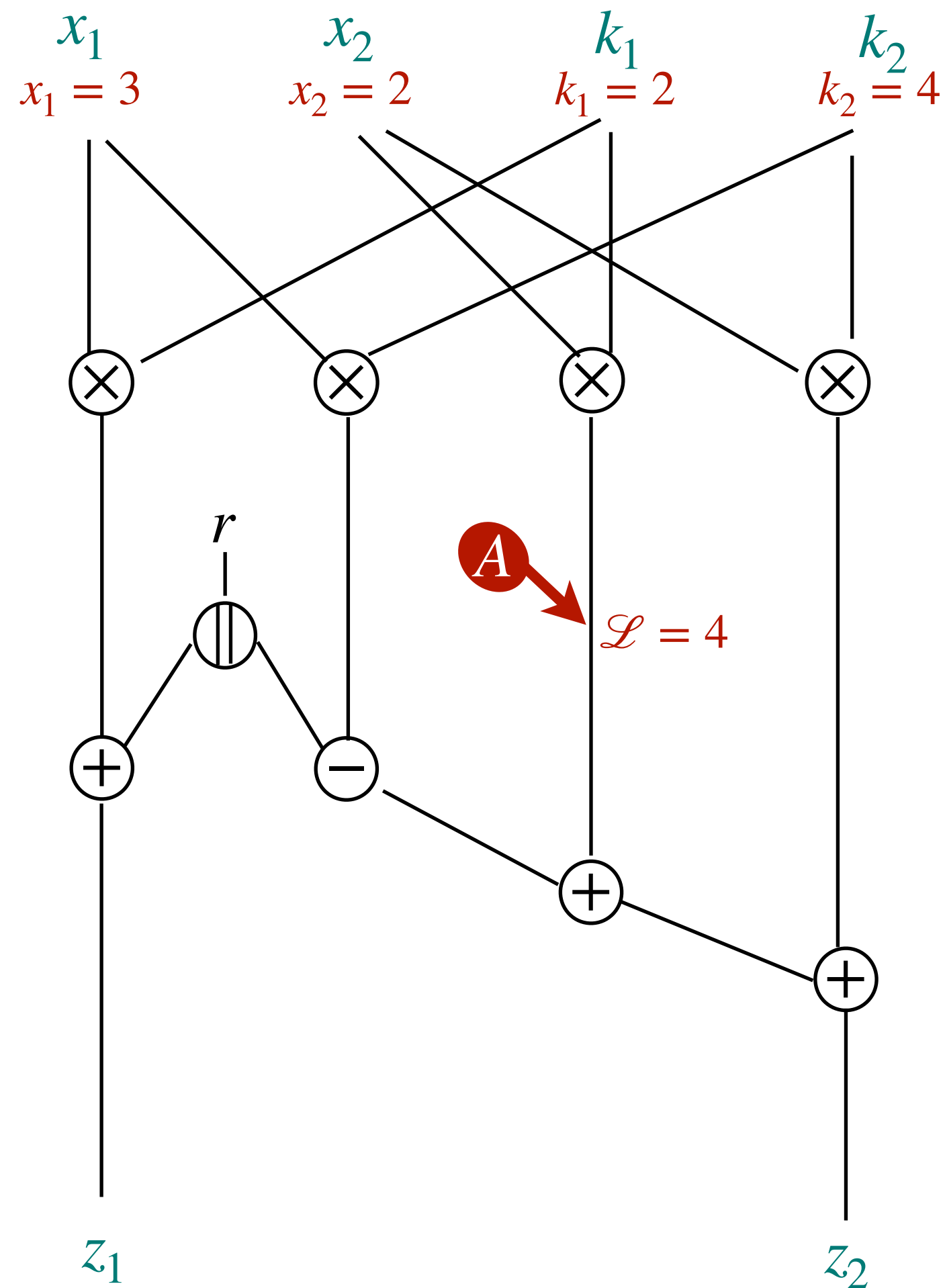
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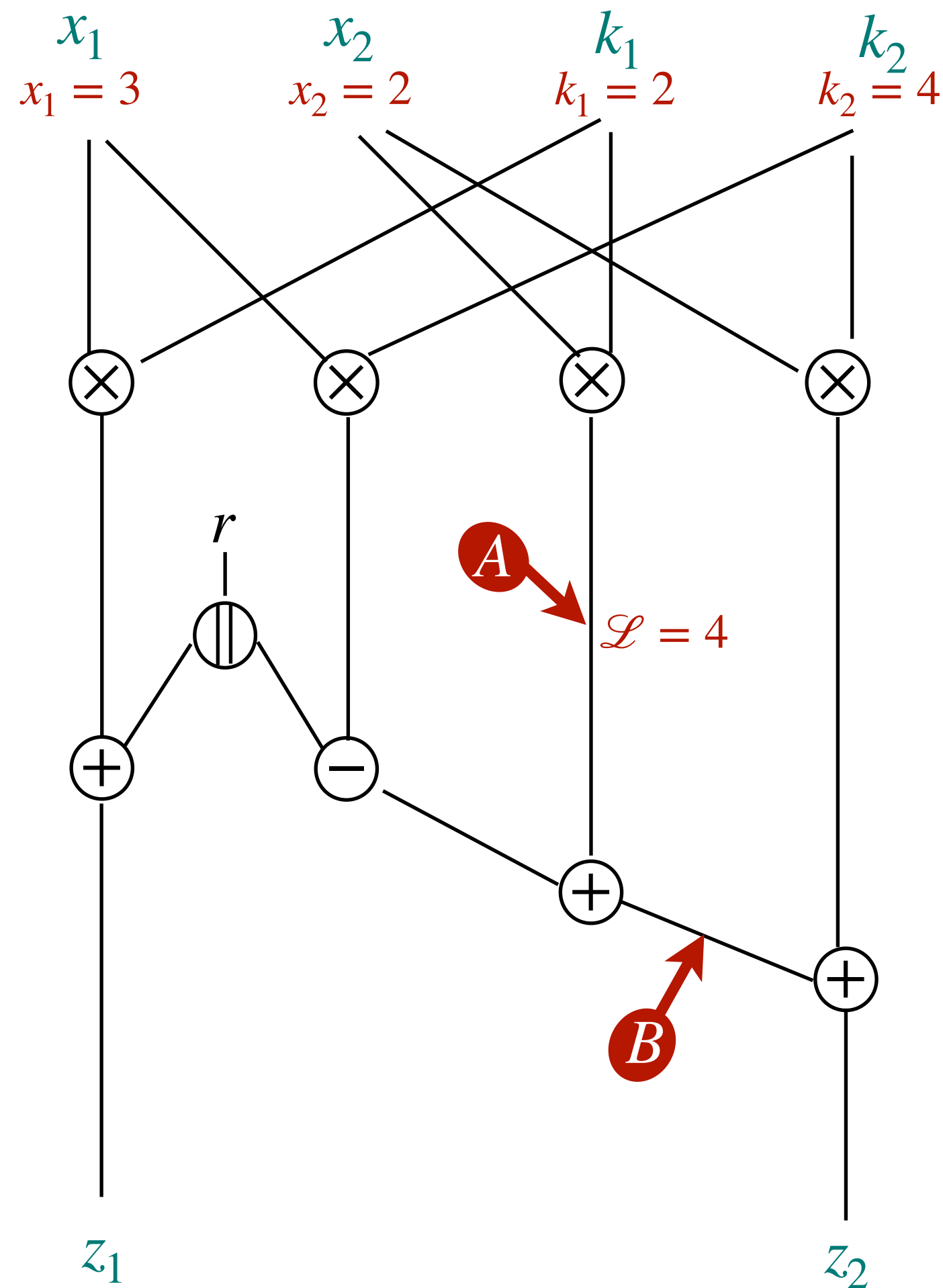
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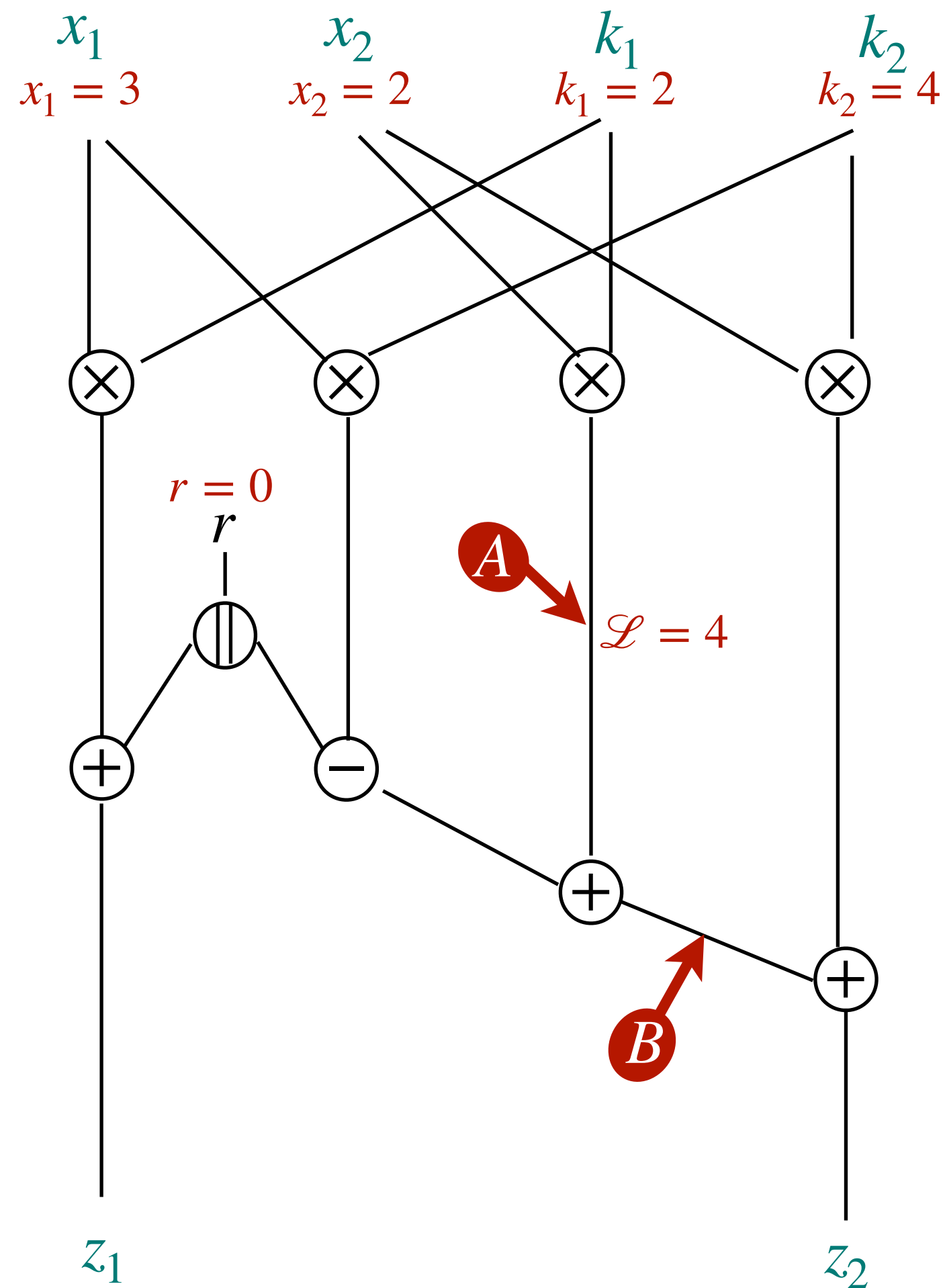
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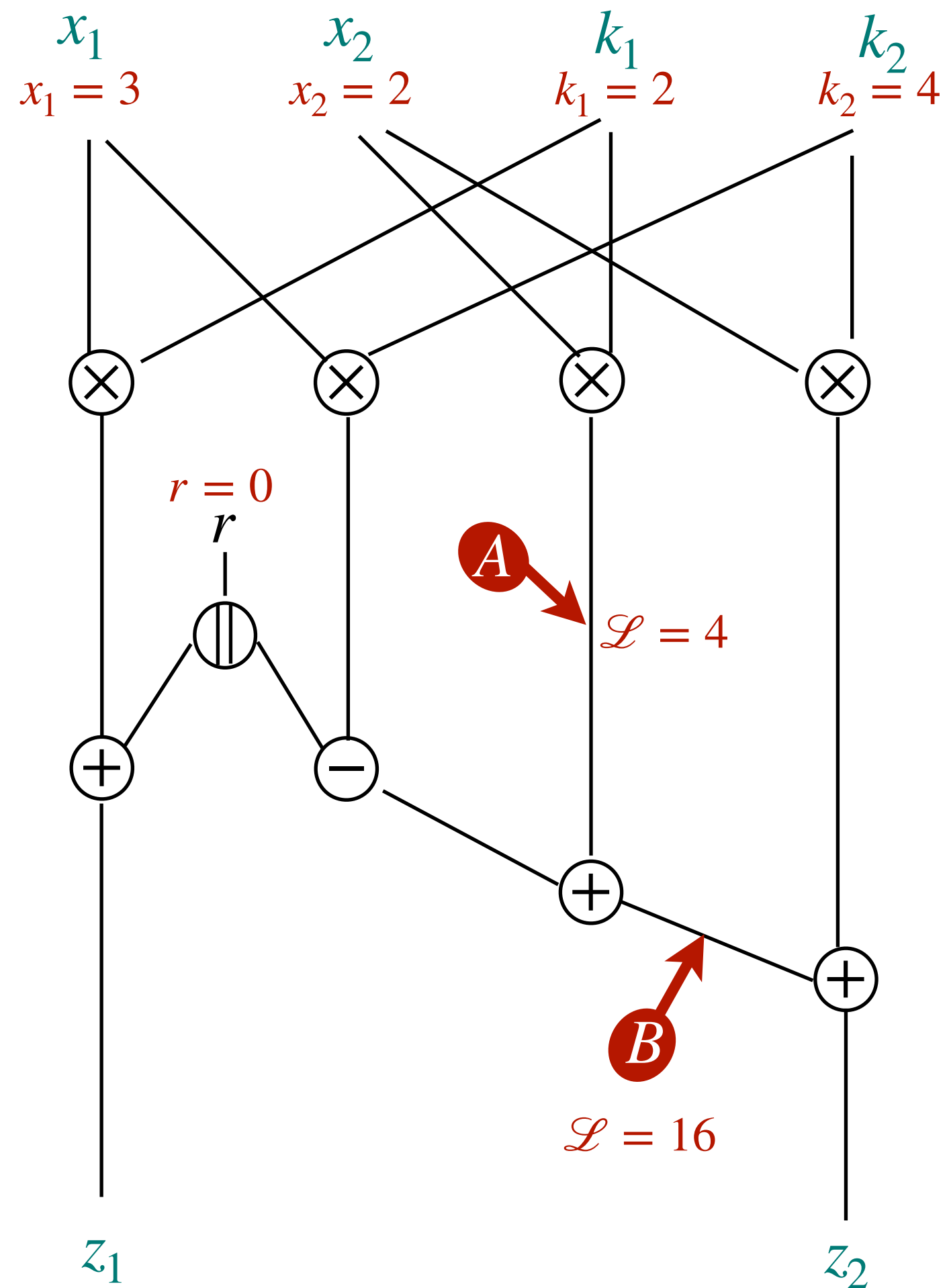
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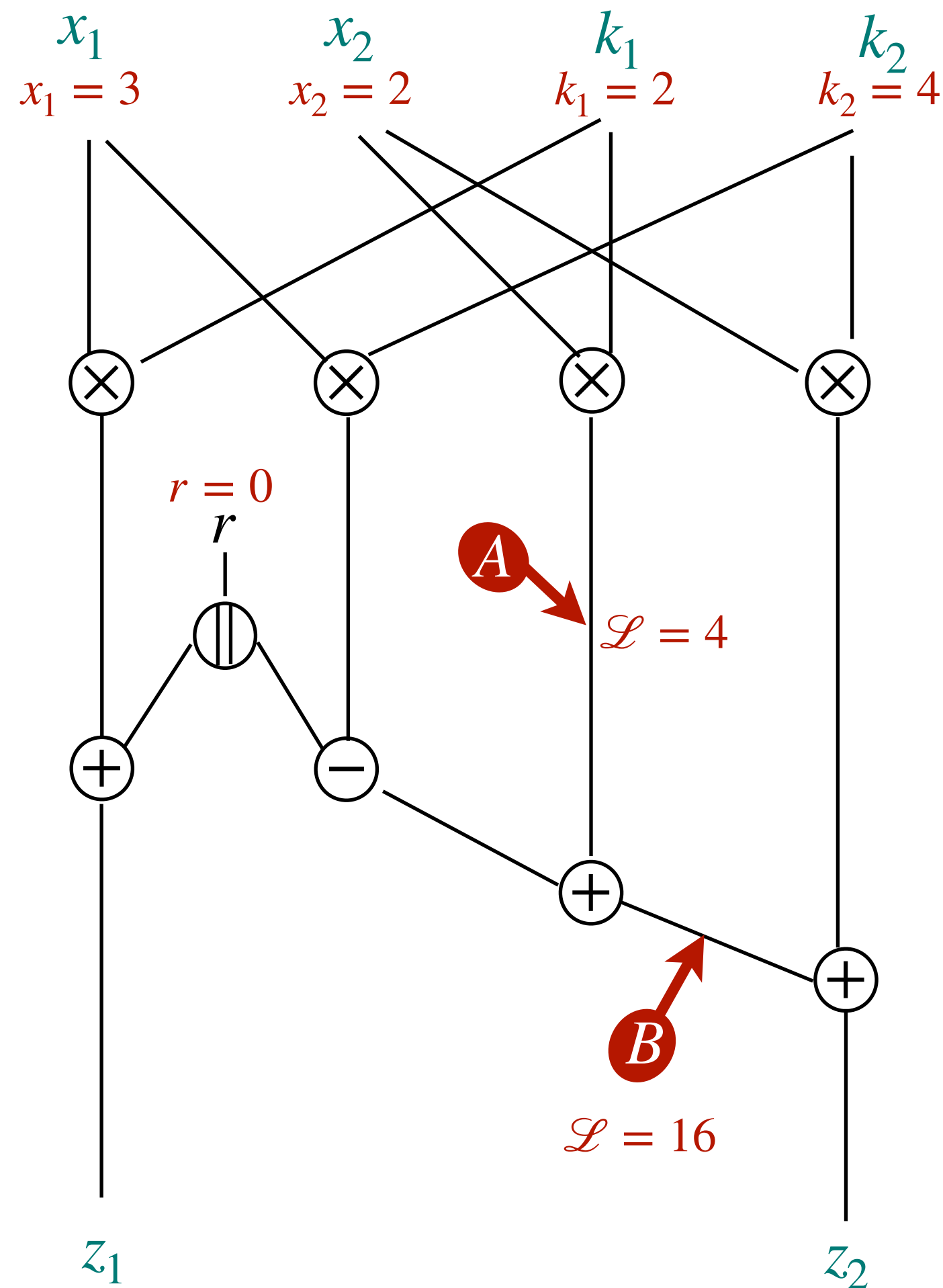
$$\text{and } \text{out} \stackrel{\text{perfect}}{\approx} \mathcal{L}$$

**A**  $I_k = 1 \quad I_x = 2$

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**[BBD+16]** G. Barthe, S. Belaïd, F. Dupressoir, P.-A. Fouque, B. Grégoire, P.-Y. Strub, and R. Zucchini.  
*Strong non-interference and type-directed higher-order masking.* ACM CCS 2016

# t-Probing Security & composability



## Composability : $t$ -Non Interference

Let  $\mathcal{P}$  be a set of at most  $t$  probes :

Let  $(x_1, \dots, x_{t+1}), (k_1, \dots, k_{t+1})$  be encodings of inputs  $x$  and  $k$ .

Let  $\mathcal{L} \leftarrow \text{AssignWires}(\mathcal{P}, (x_1, \dots, x_{t+1}), (k_1, \dots, k_{t+1}))$  be the values taken by the probes.

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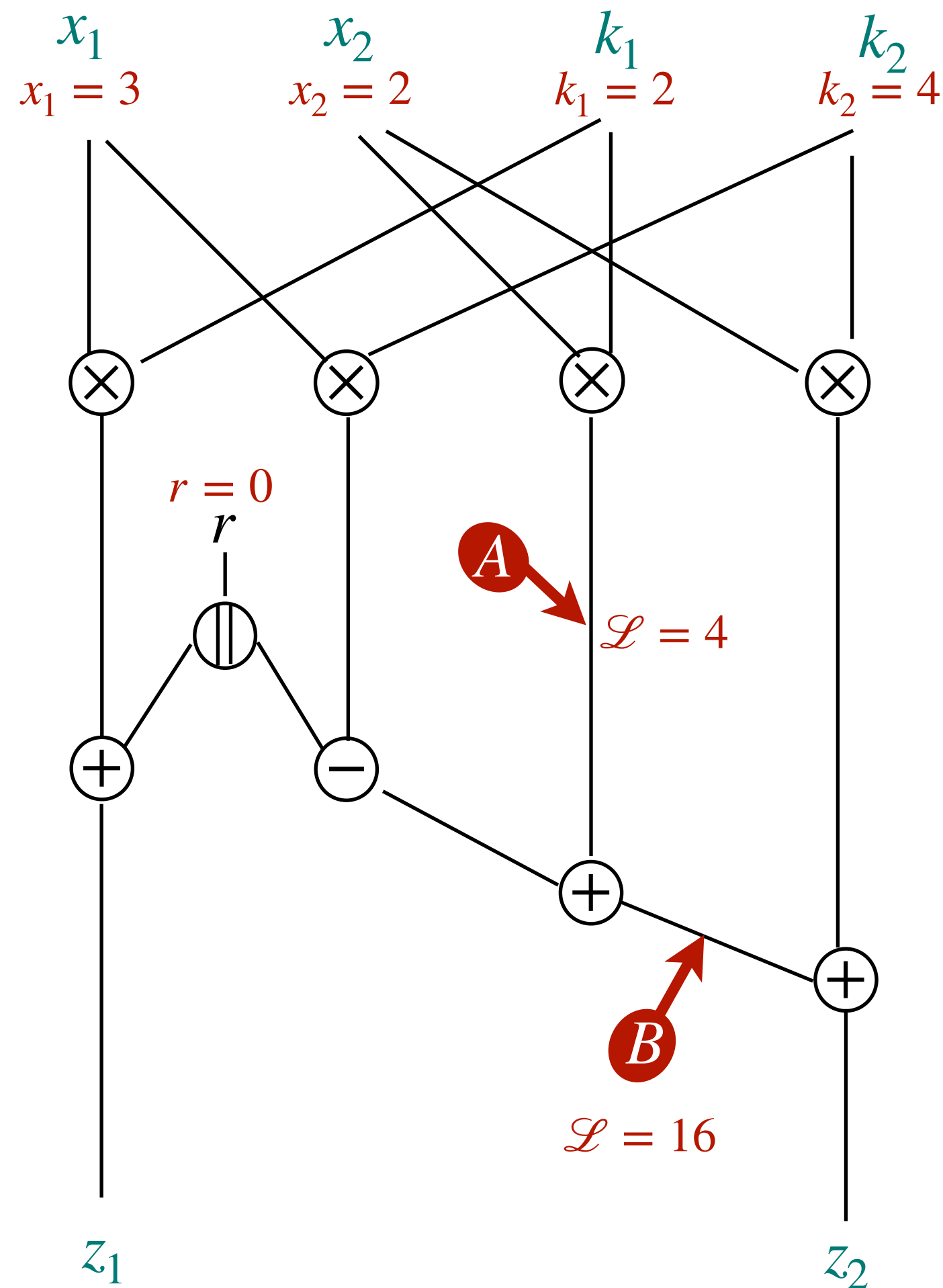
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**B**  $I_x = \emptyset \quad I_k = \emptyset$

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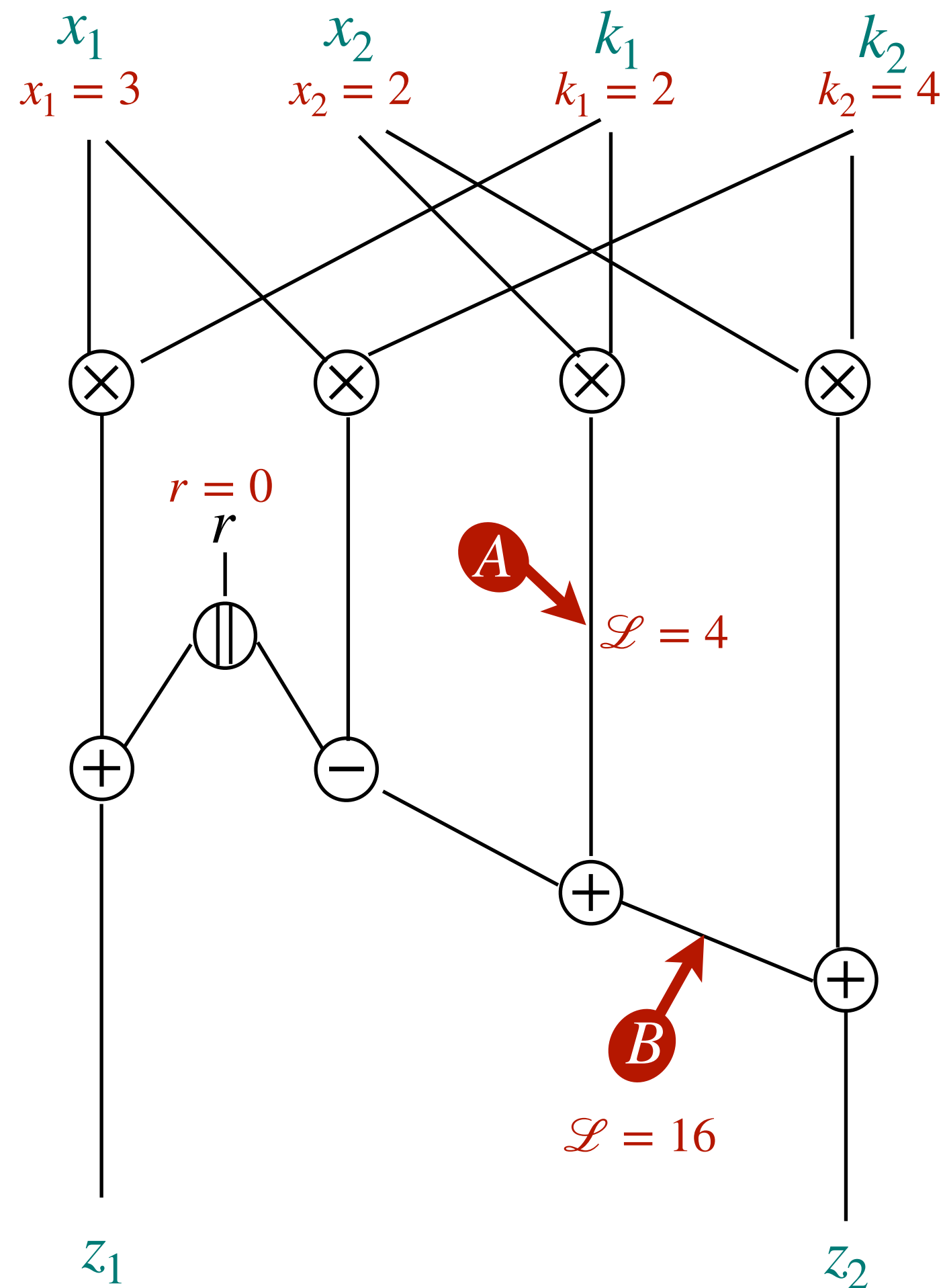
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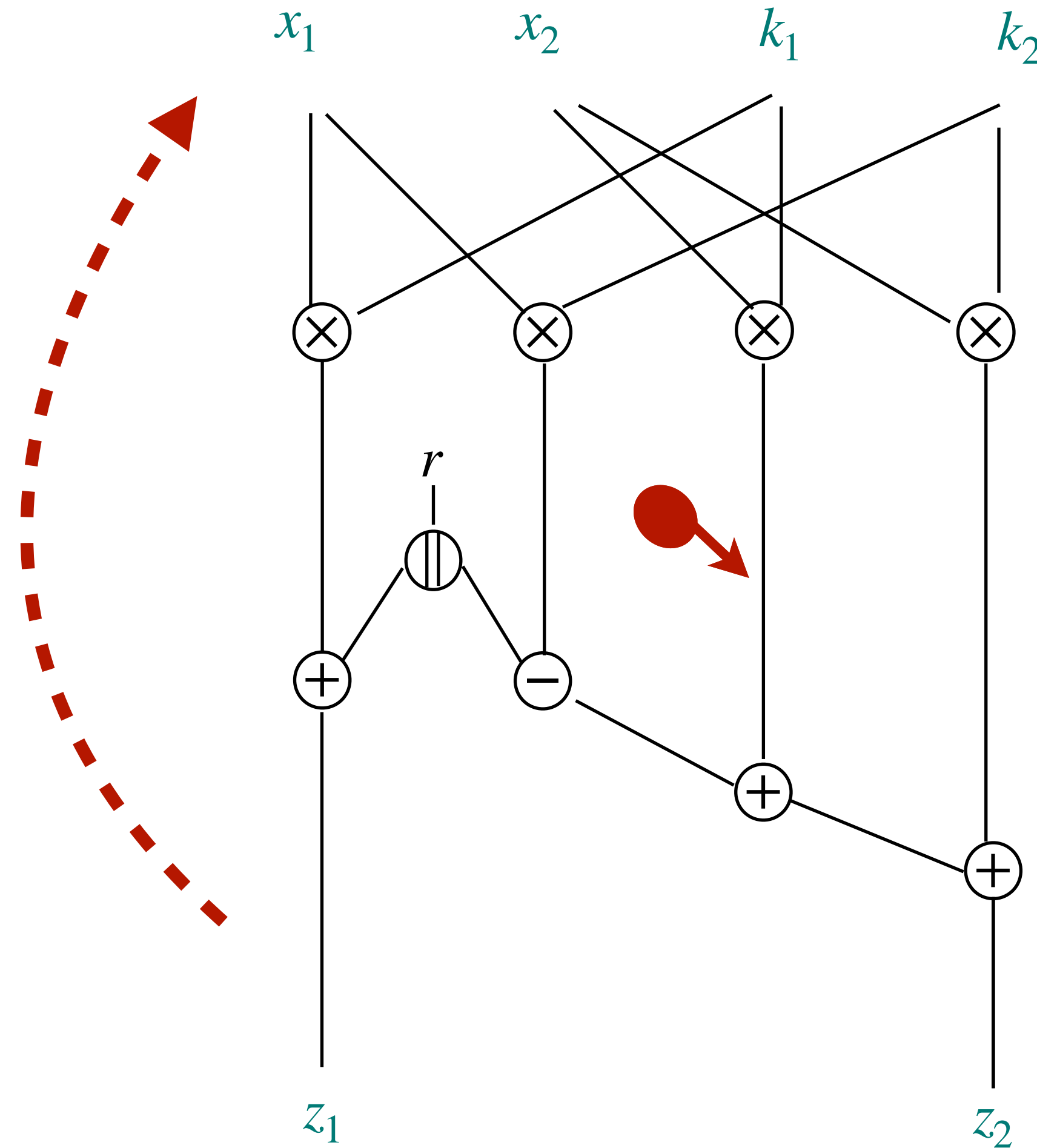
$$\text{out} \leftarrow \$$$

Any out is valid as it corresponds to drawing  $r = \text{out} - x_2 k_1 - x_1 k_2$

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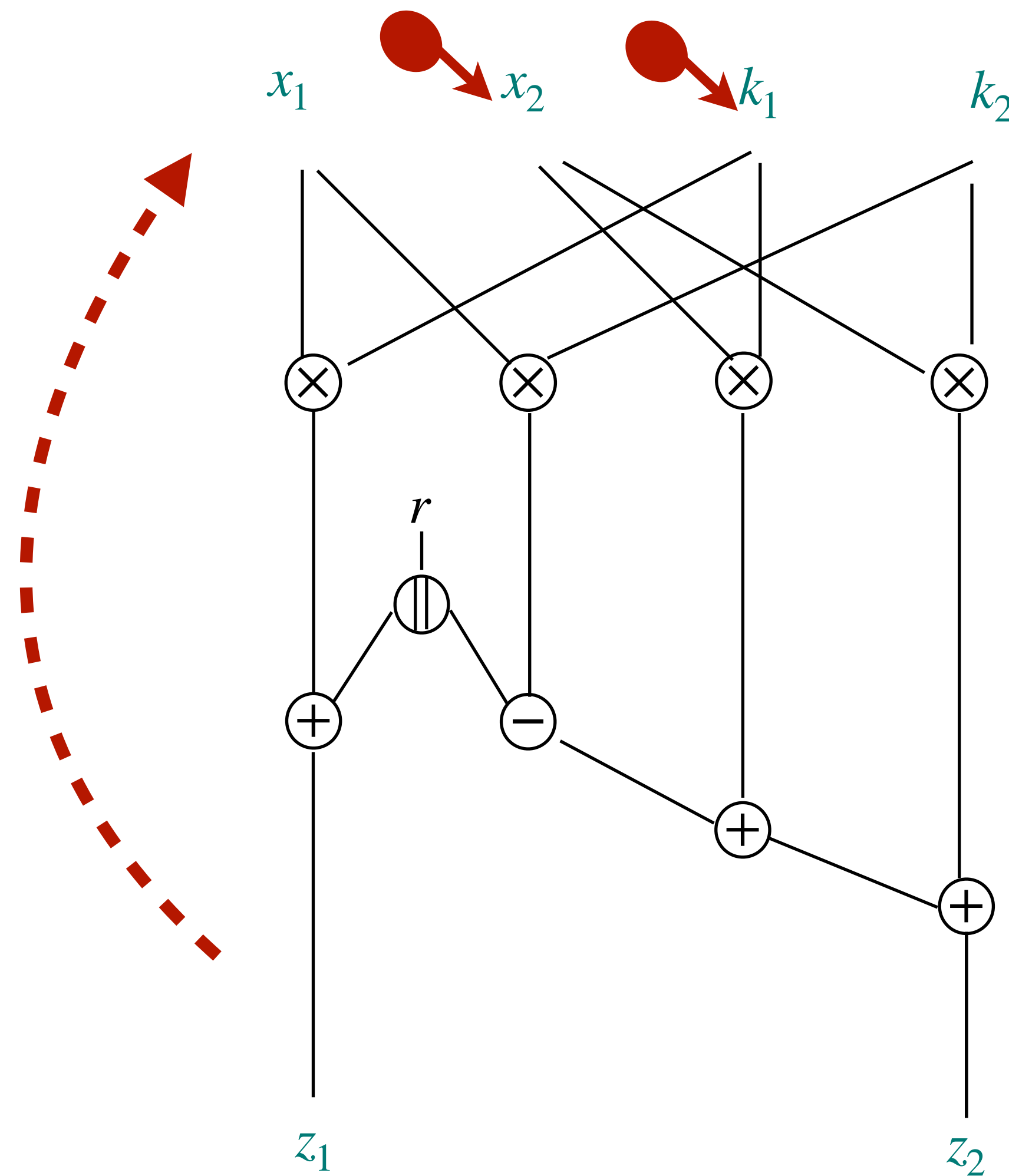
# t-Probing Security & composability

Non Interference:  
Propagation of the simulation  
from inside to gadget to its inputs



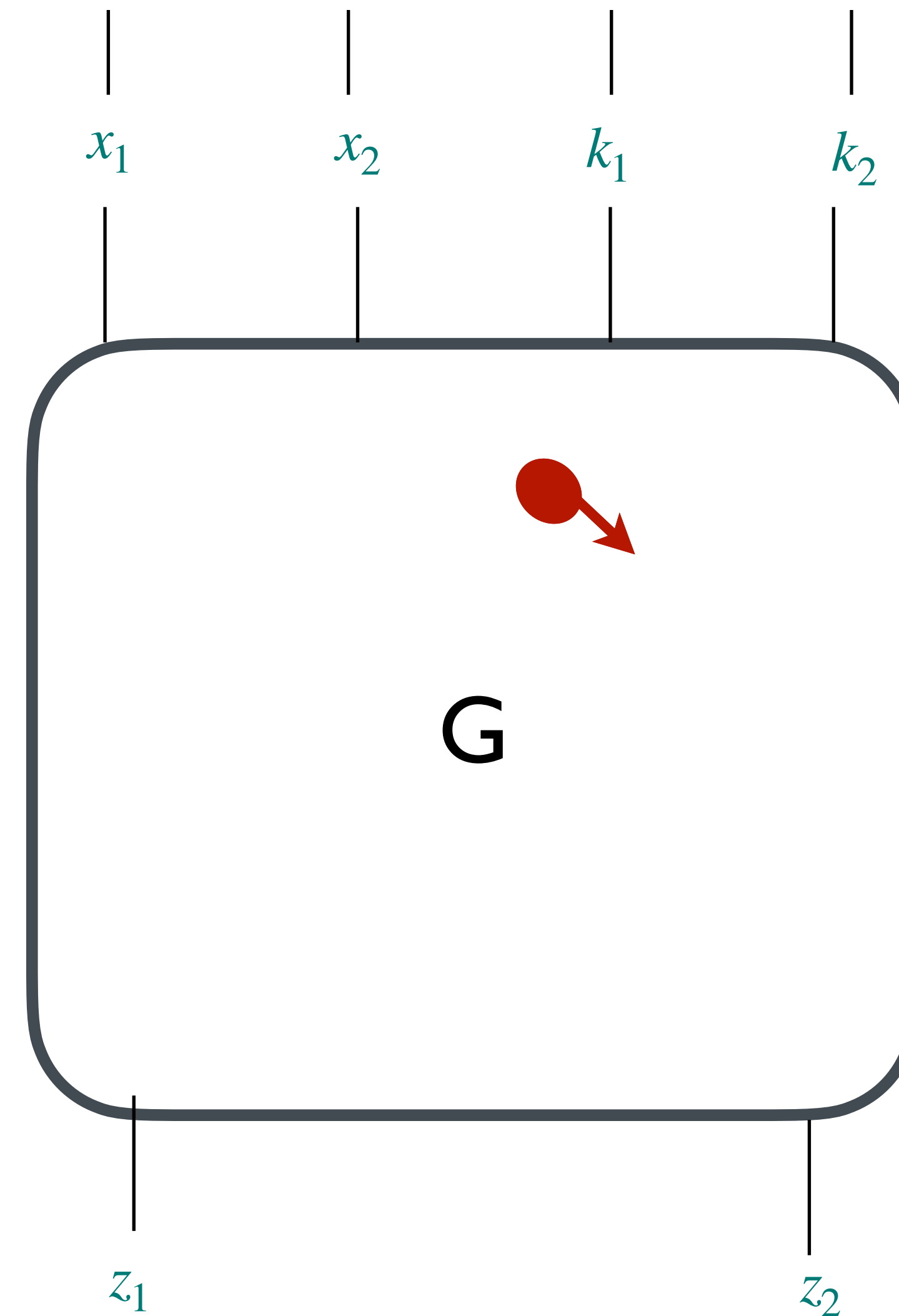
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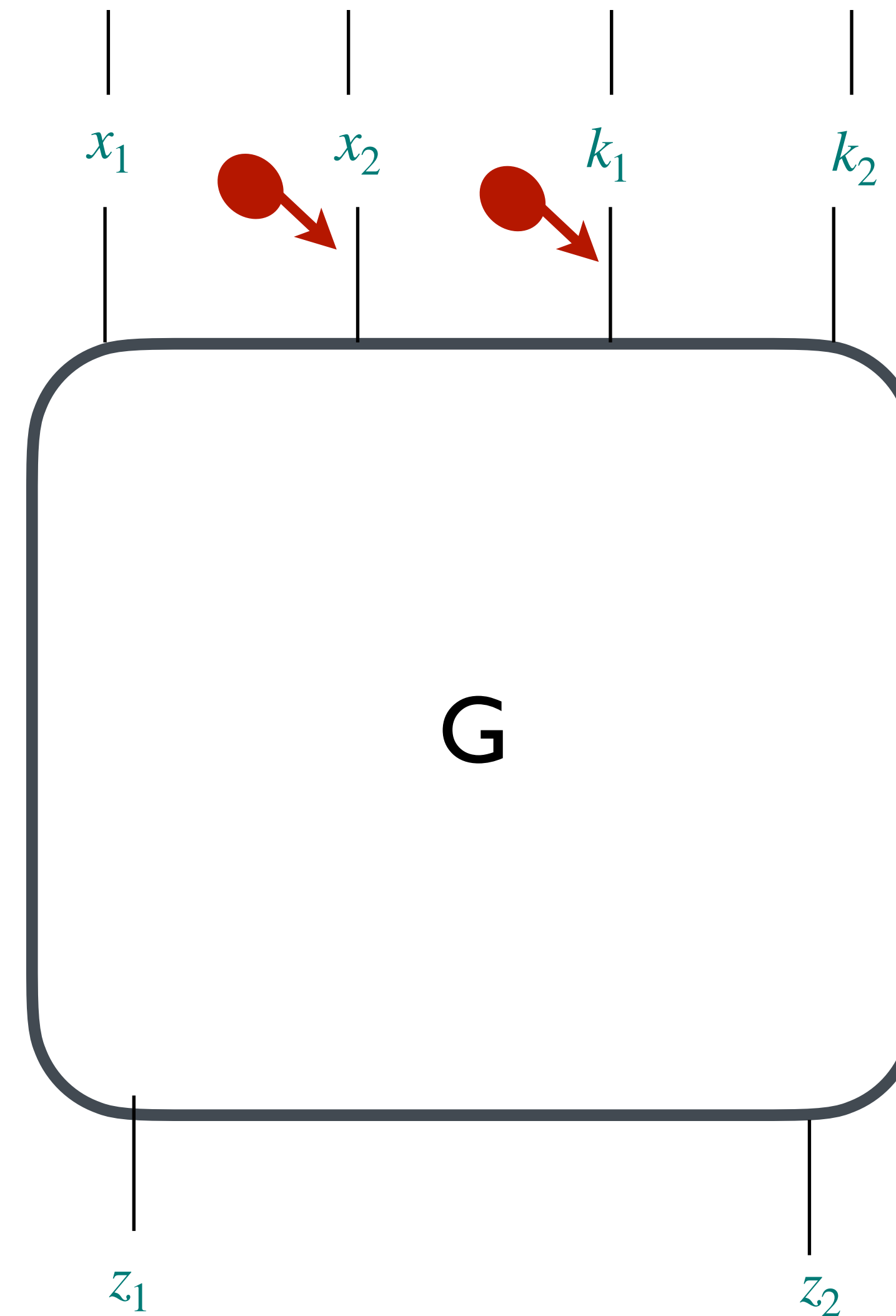
# t-Probing Security & composability

Connecting gadgets in a sequential way



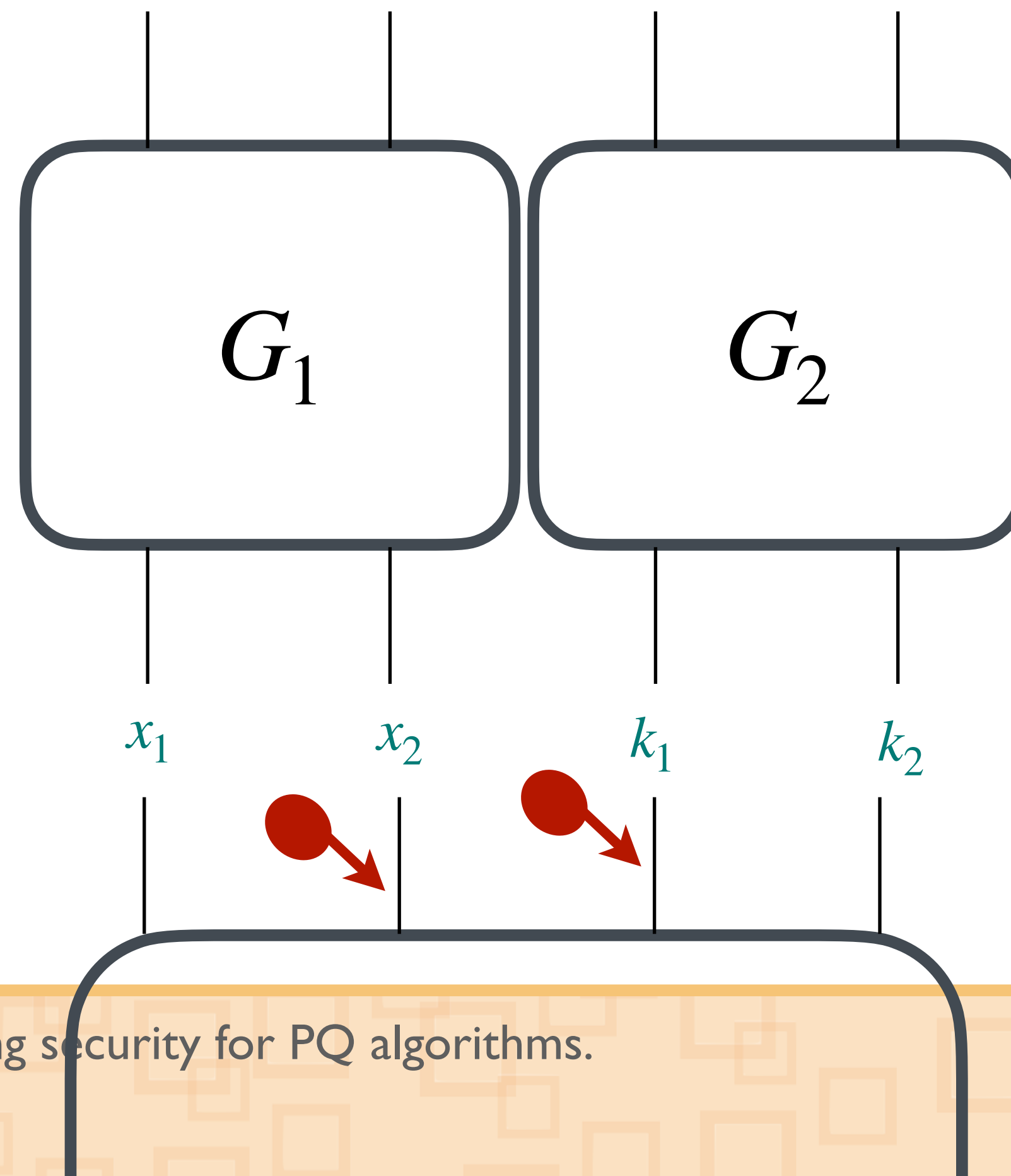
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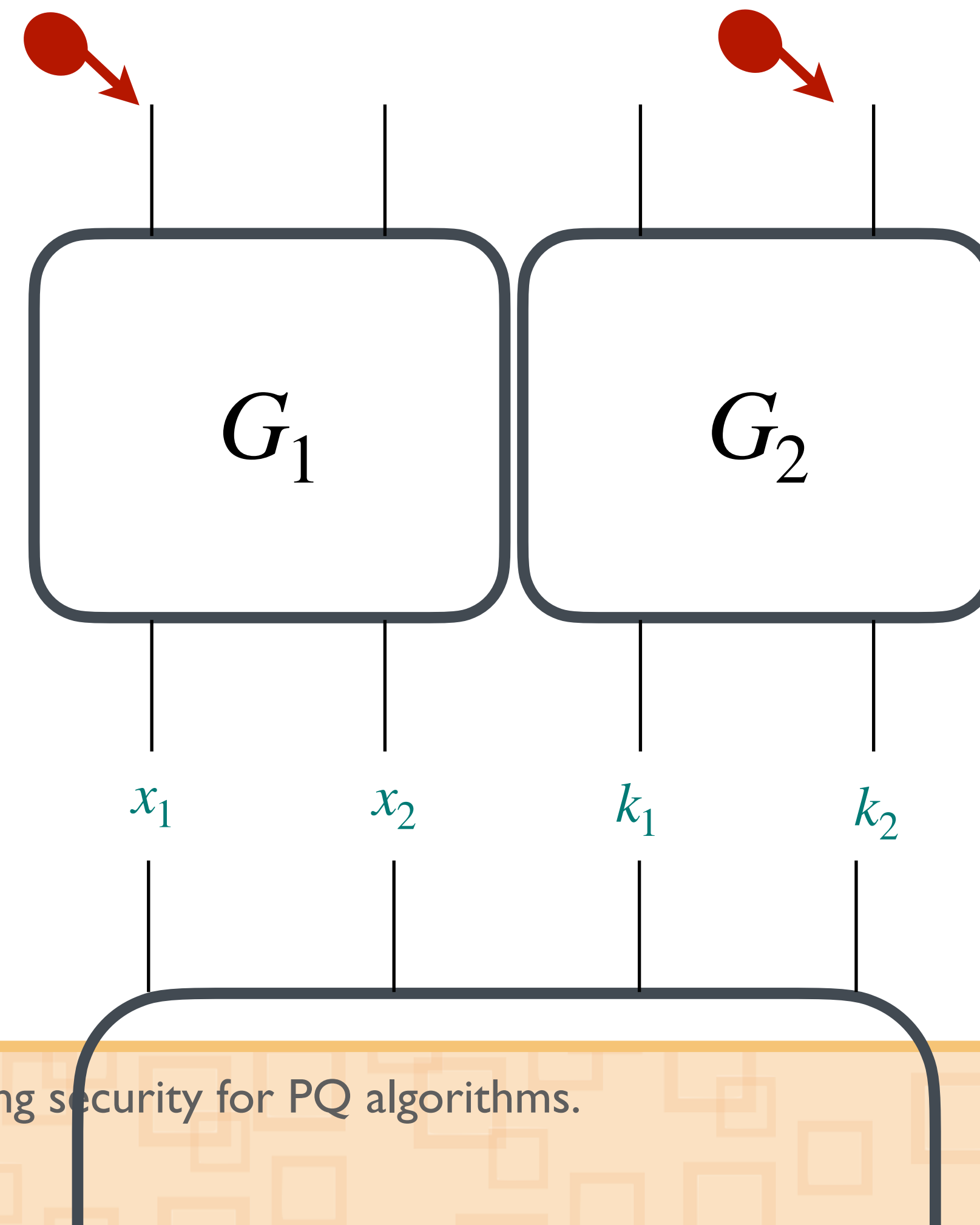
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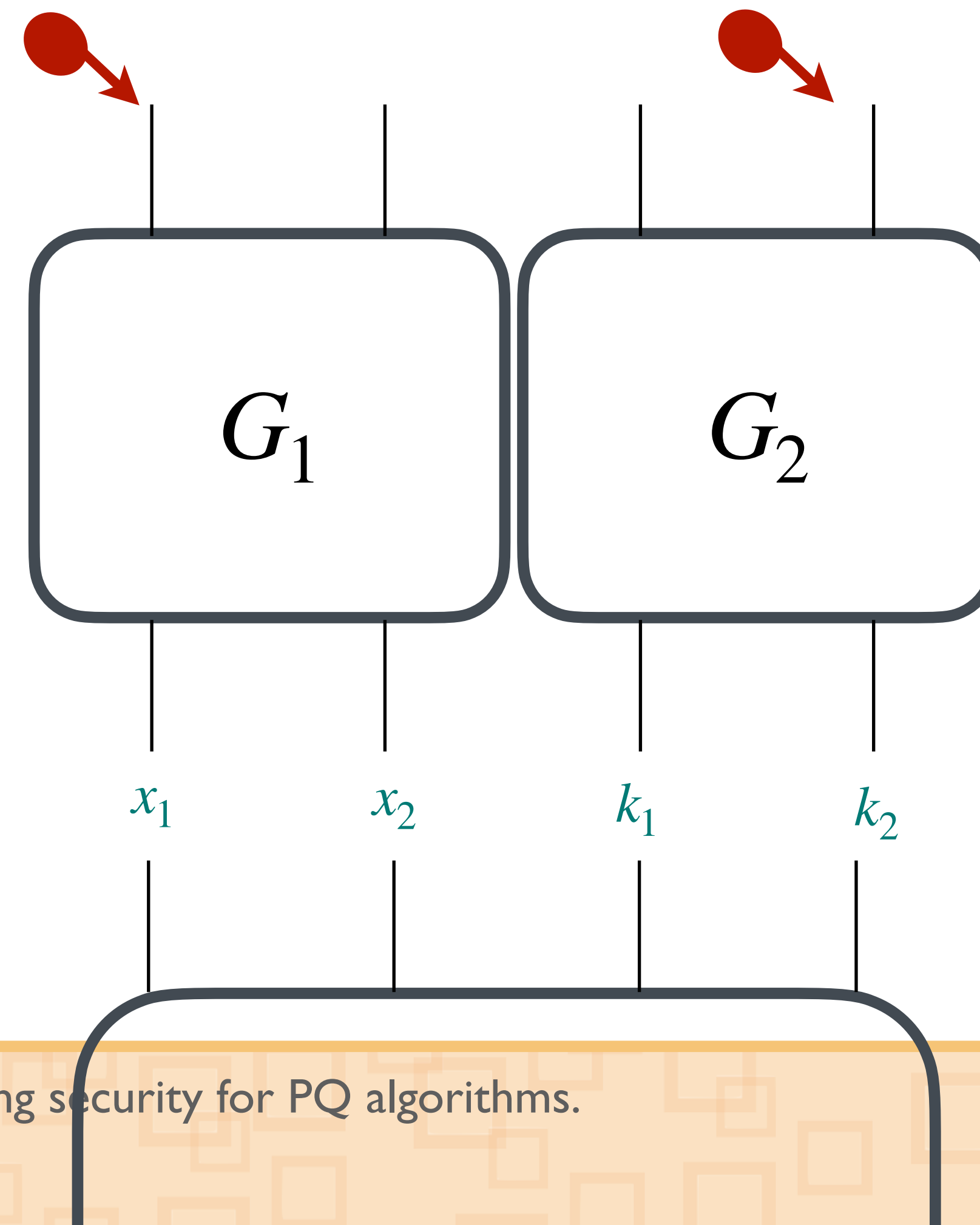
# $t$ -Probing Security & composability

## Connecting gadgets in a sequential way

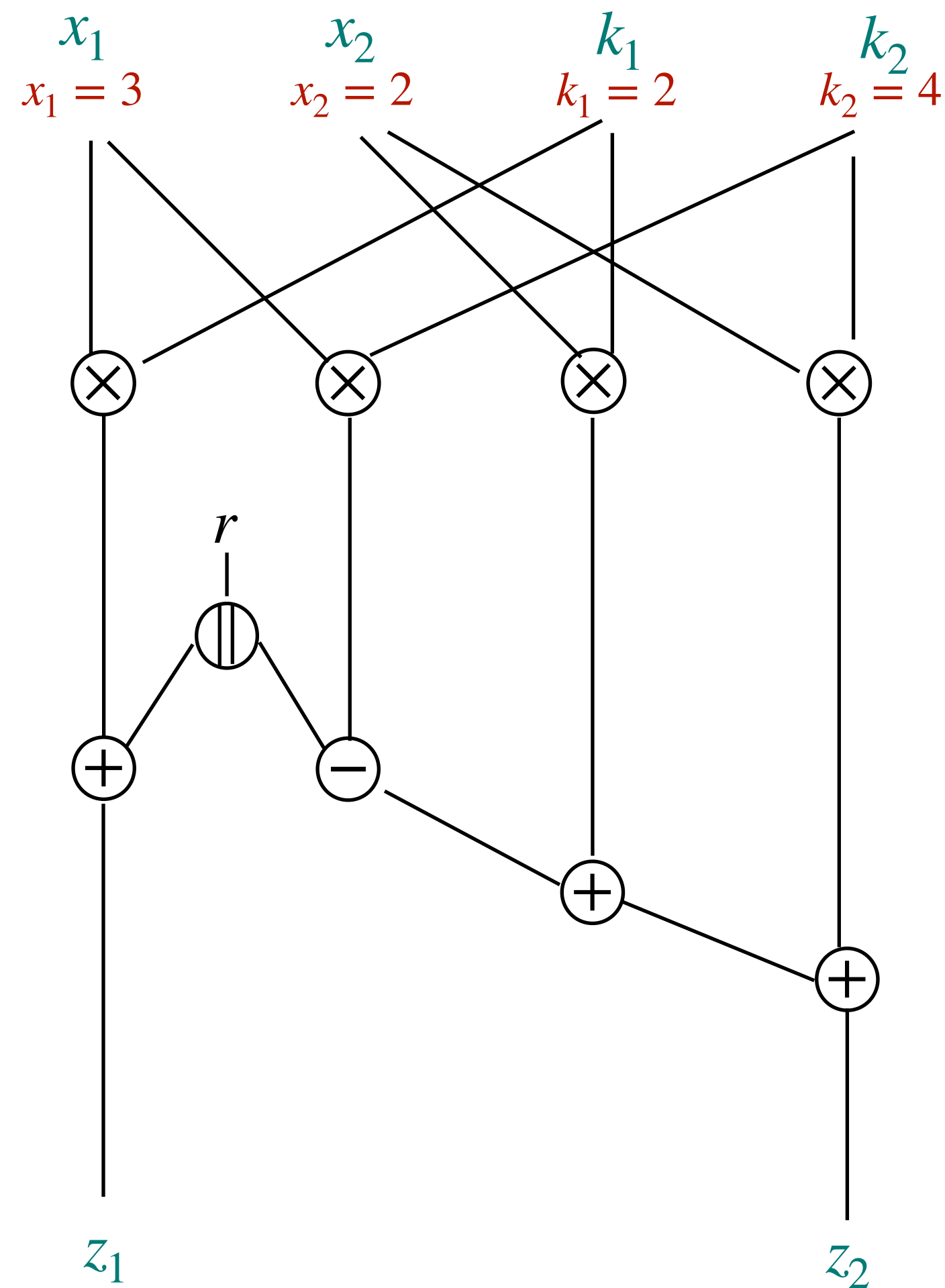
### Composition

A sequential composition of  $t$ -Non interferent gadgets is also  $t$ -Non interferent.  
 $\implies t$ -probing secure with a uniform input encoding.

There is a way to handle non sequential compositions by using refreshes to break dependencies.



# Random Probing Security

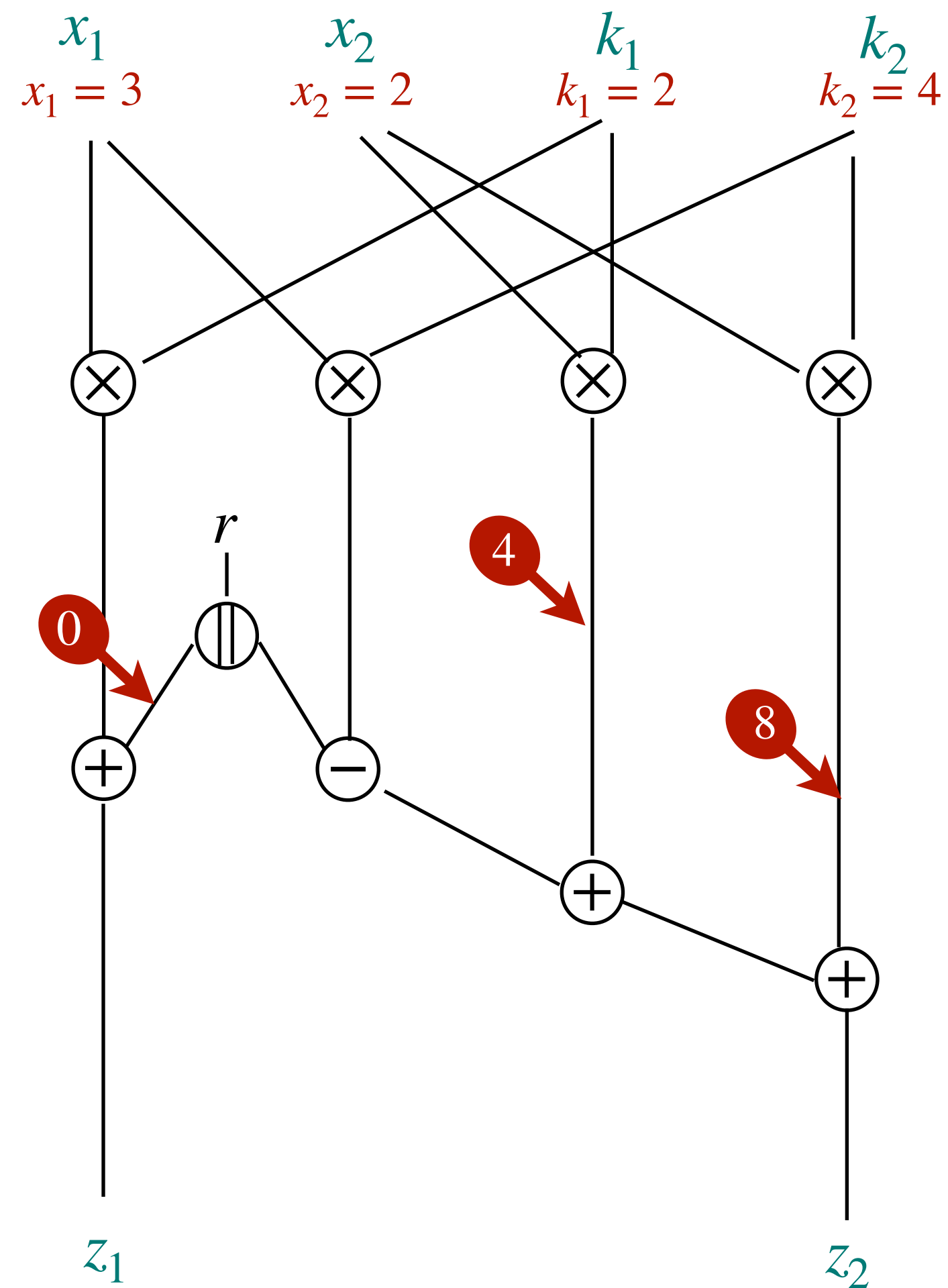


## Attacker model

The attacker is given the value of each wire with probability  $p$ .

[DDF14] A. Duc, S. Dziembowski, S. Faust. *Unifying leakage models: From probing attacks to noisy leakage*. EUROCRYPT 2014

# Random Probing Security

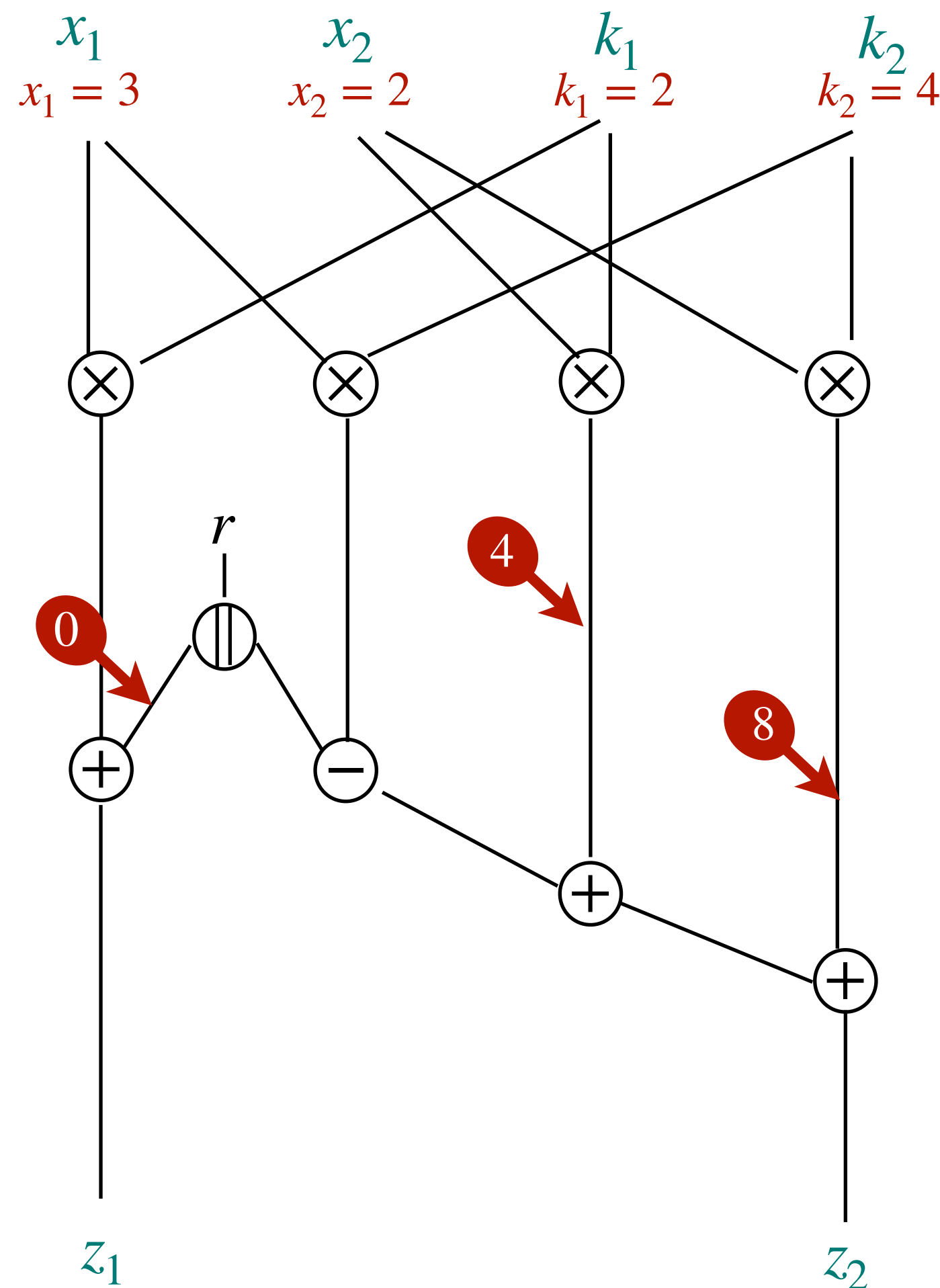


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## $(p, \epsilon)$ -random-probing security

Let  $\mathcal{W}$  be a set of wires that are drawn with **prob.**  $p$ .

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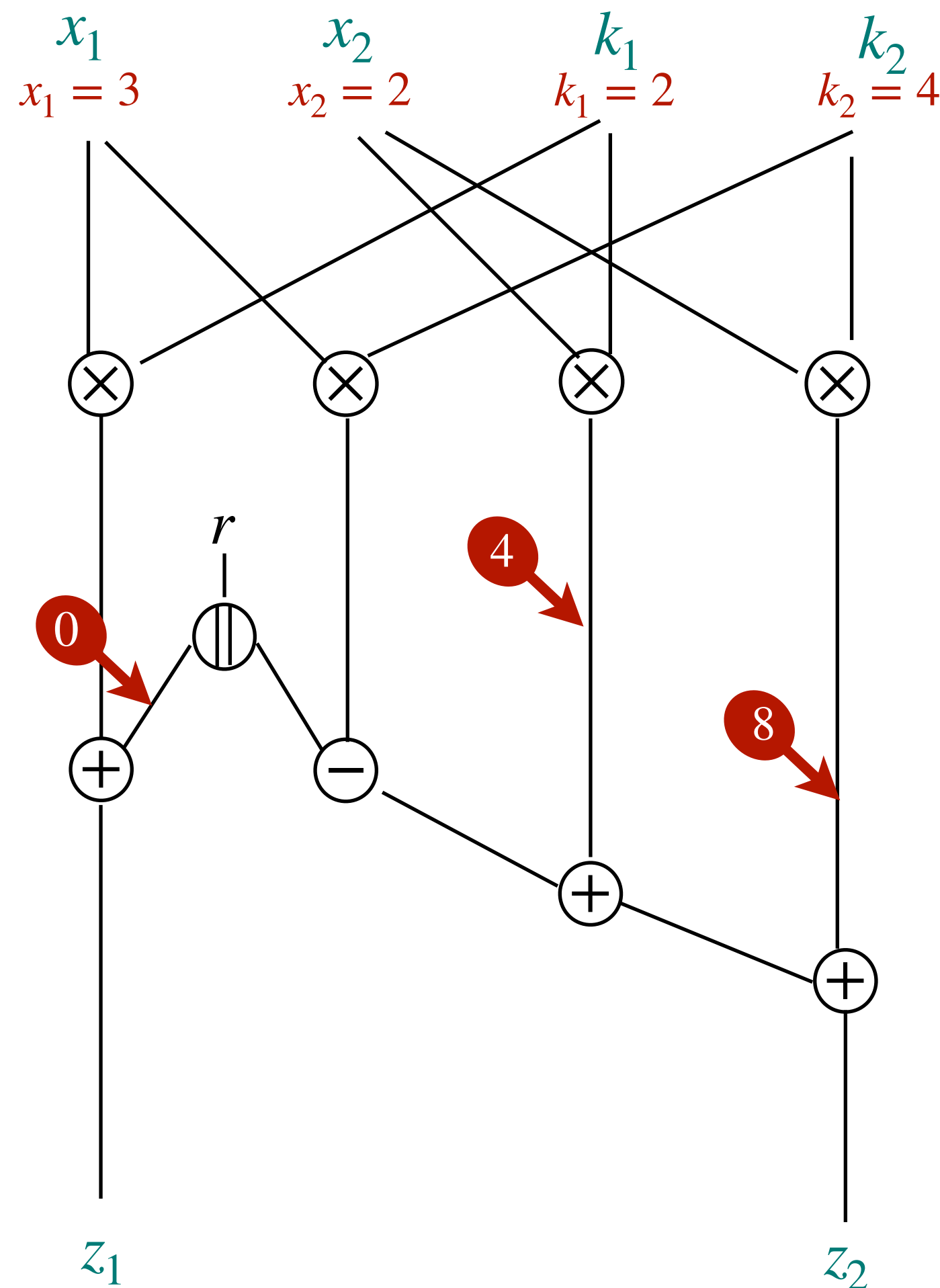
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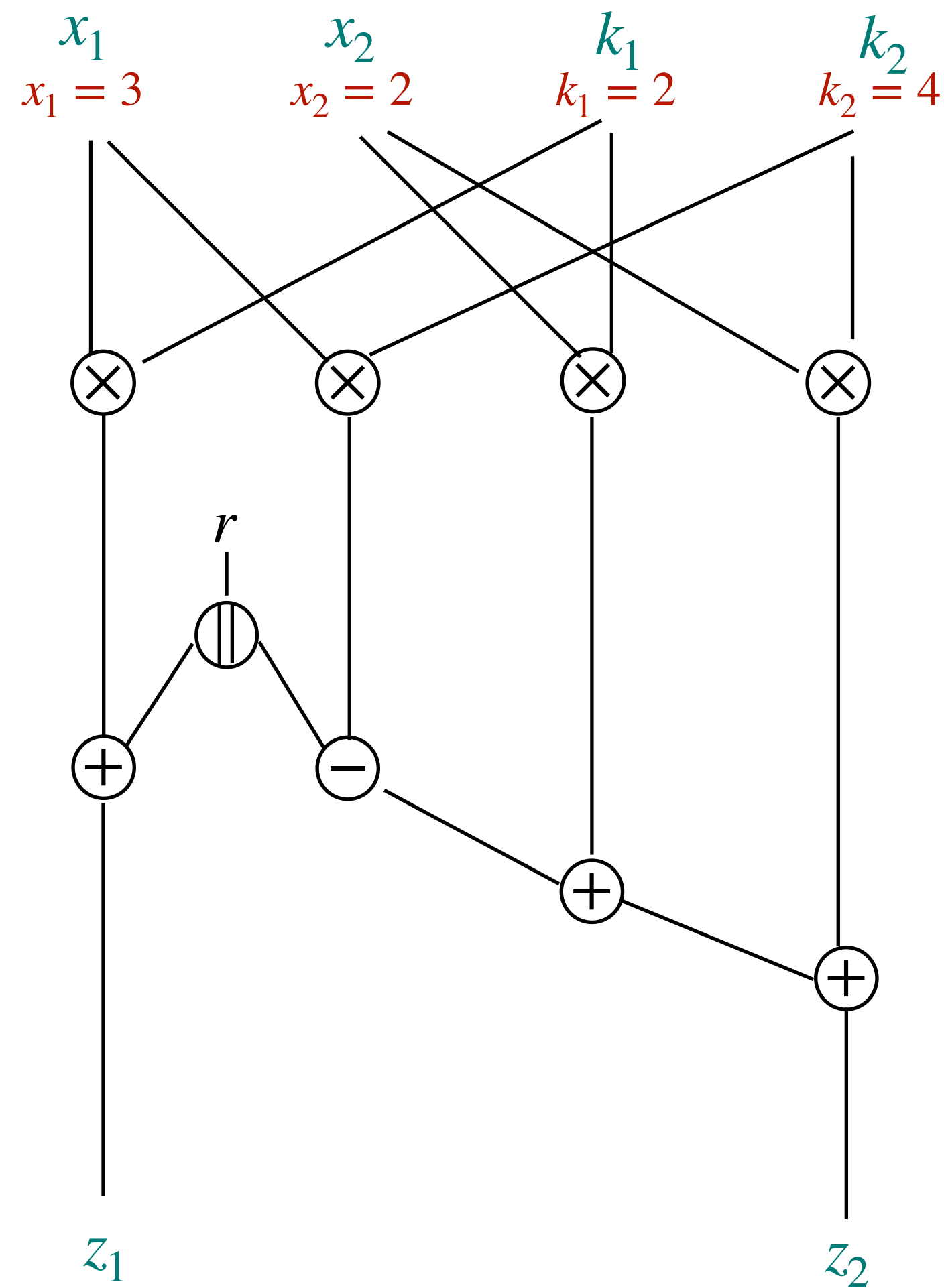
There exists a simulator such that

$\mathcal{L}$  can contain up to 19 values, one for each wire !

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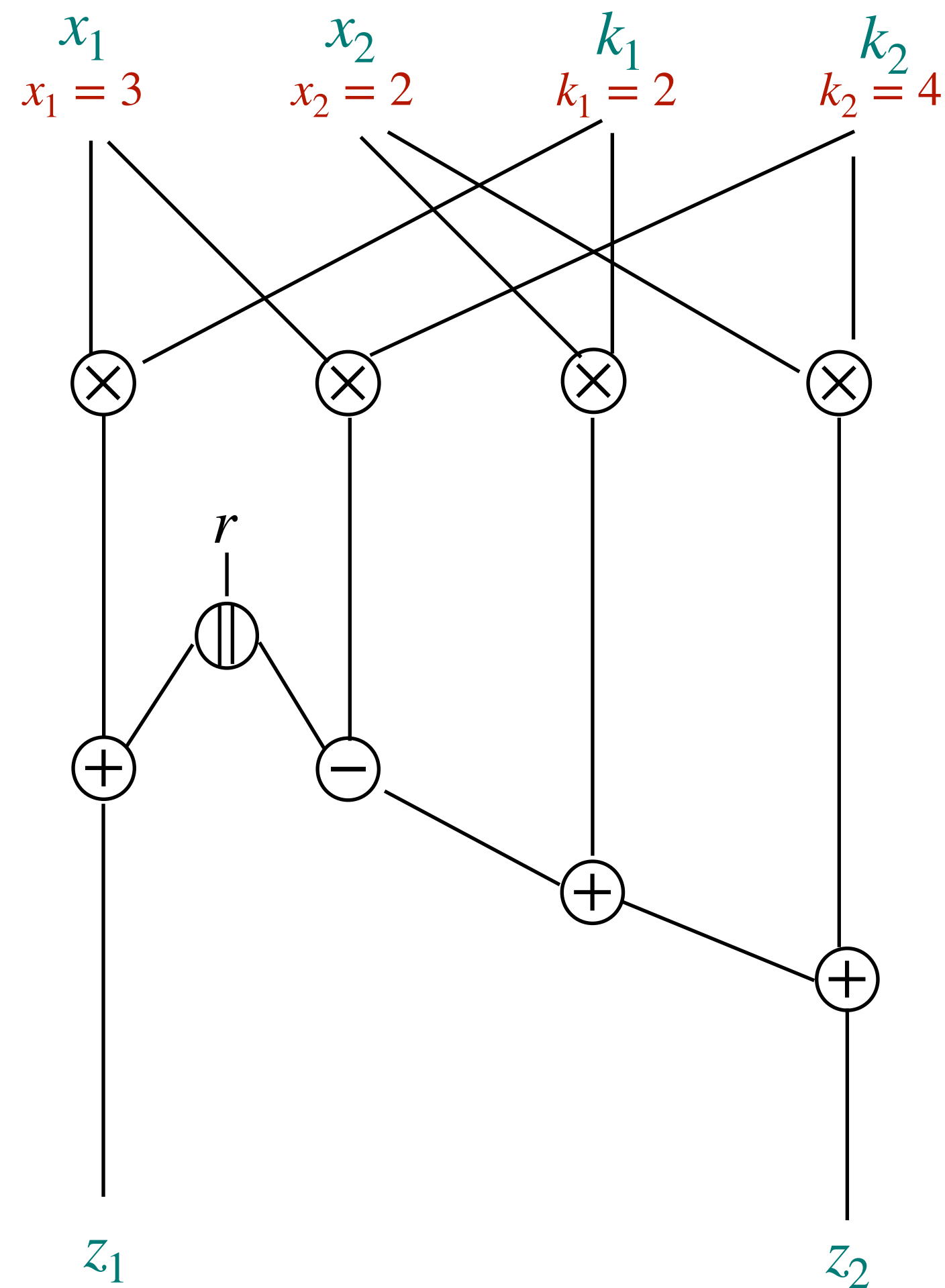
# Random Probing Security



Reality

Simulation

# Random Probing Security

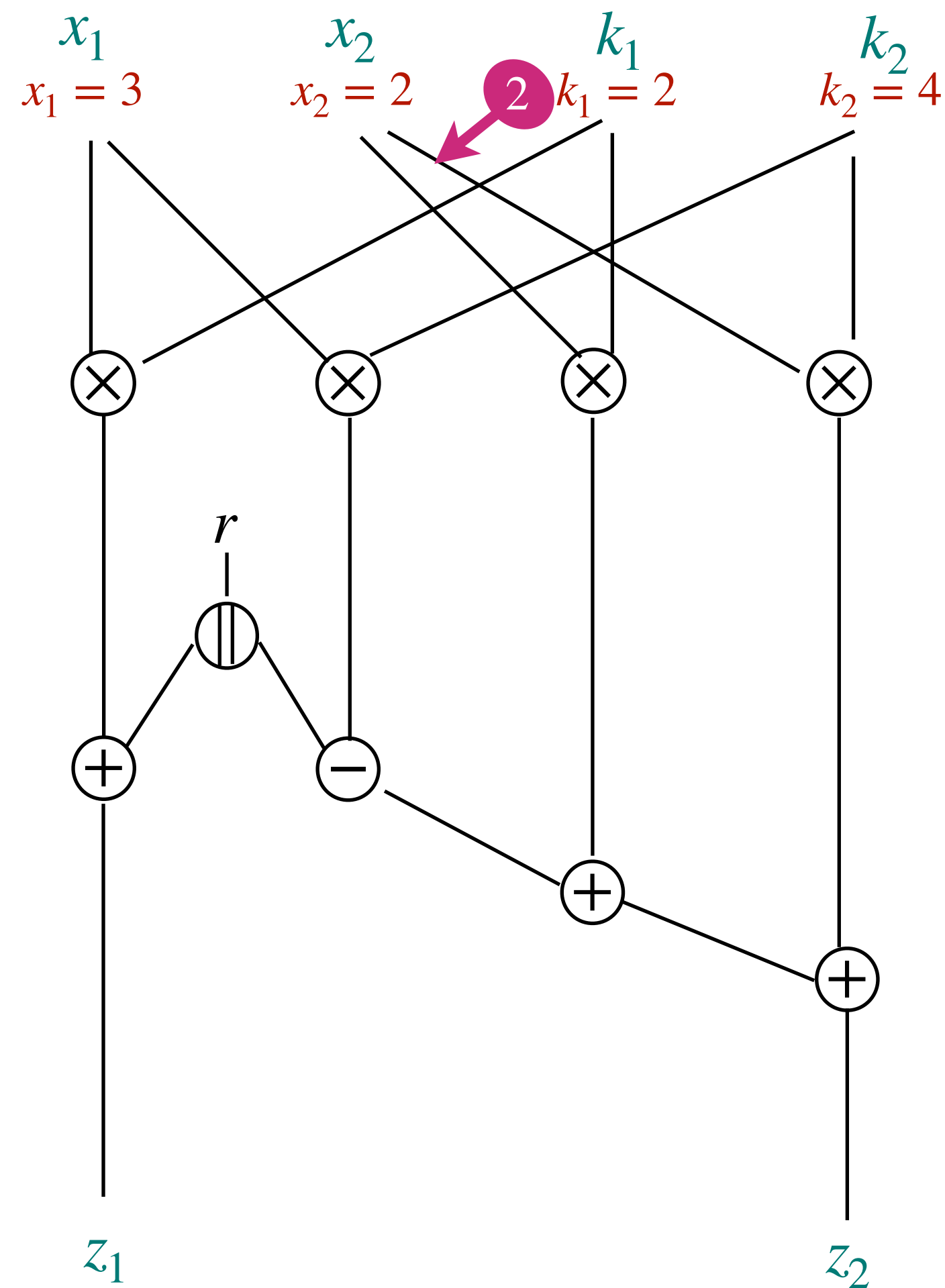


Reality

$\mathcal{W} = \emptyset$  with proba  $(1 - p)^{19}$

Simulation

# Random Probing Security



Reality

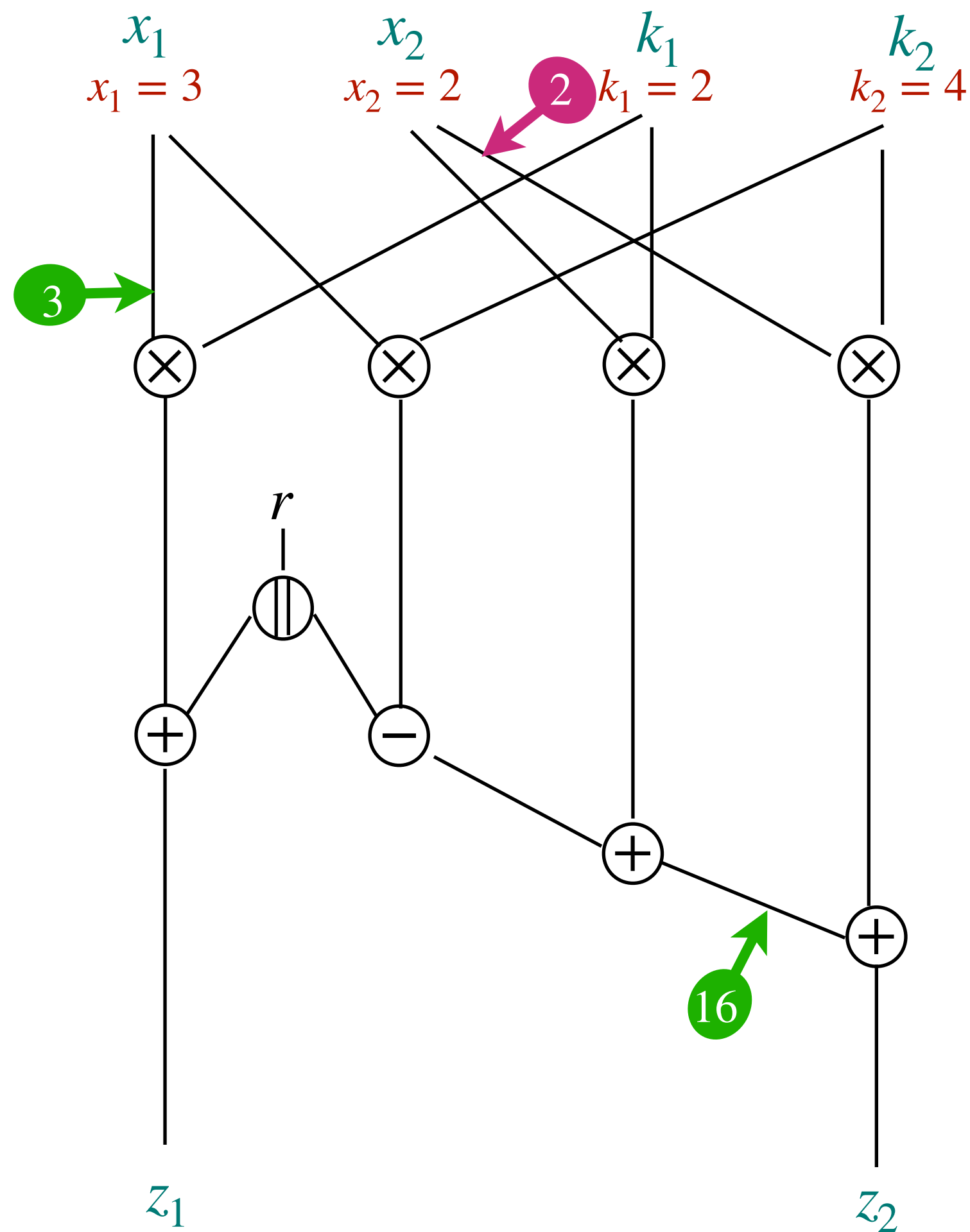
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$\mathcal{W} = \{x_2\}$  with proba  $p(1 - p)^{18}$

$\mathcal{L} = \{2\}$

Simulation

# Random Probing Security



Reality

Simulation

$\mathcal{W} = \emptyset$  with proba  $(1 - p)^{19}$

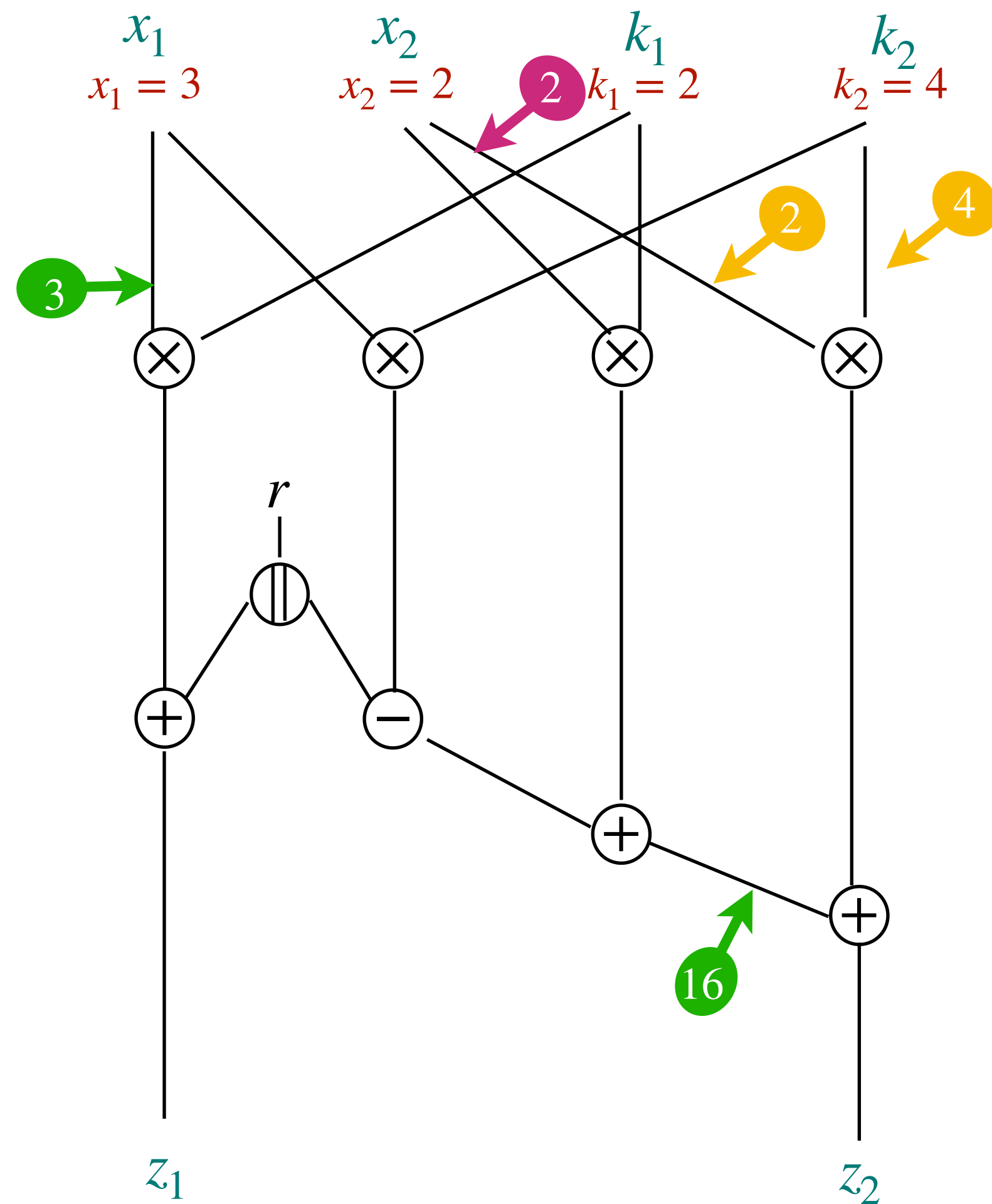
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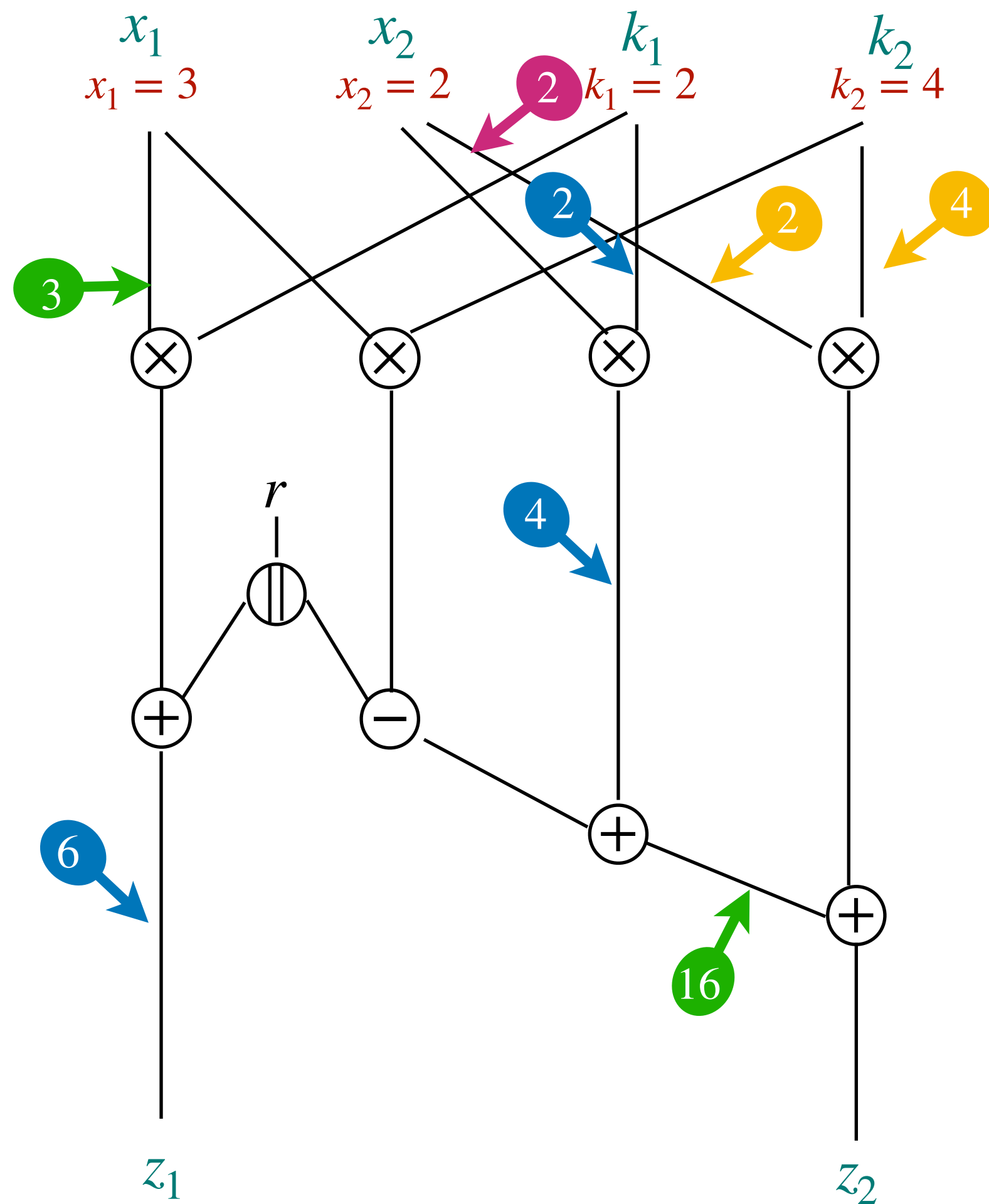
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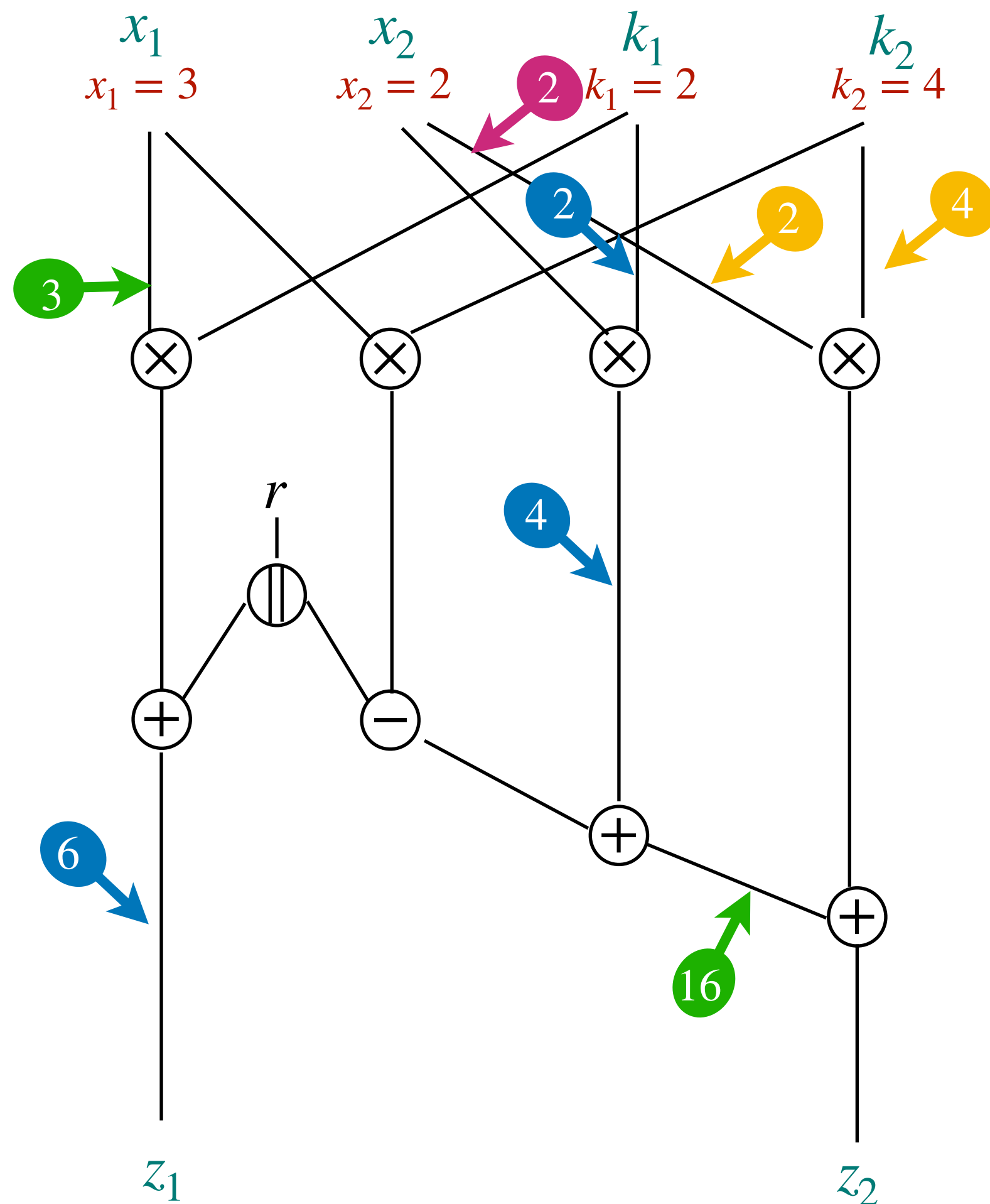
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$\mathcal{W} = \{x_1 k_1 + r, x_2 k_1, k_1\}$  with proba  $p^3(1 - p)^{16}$

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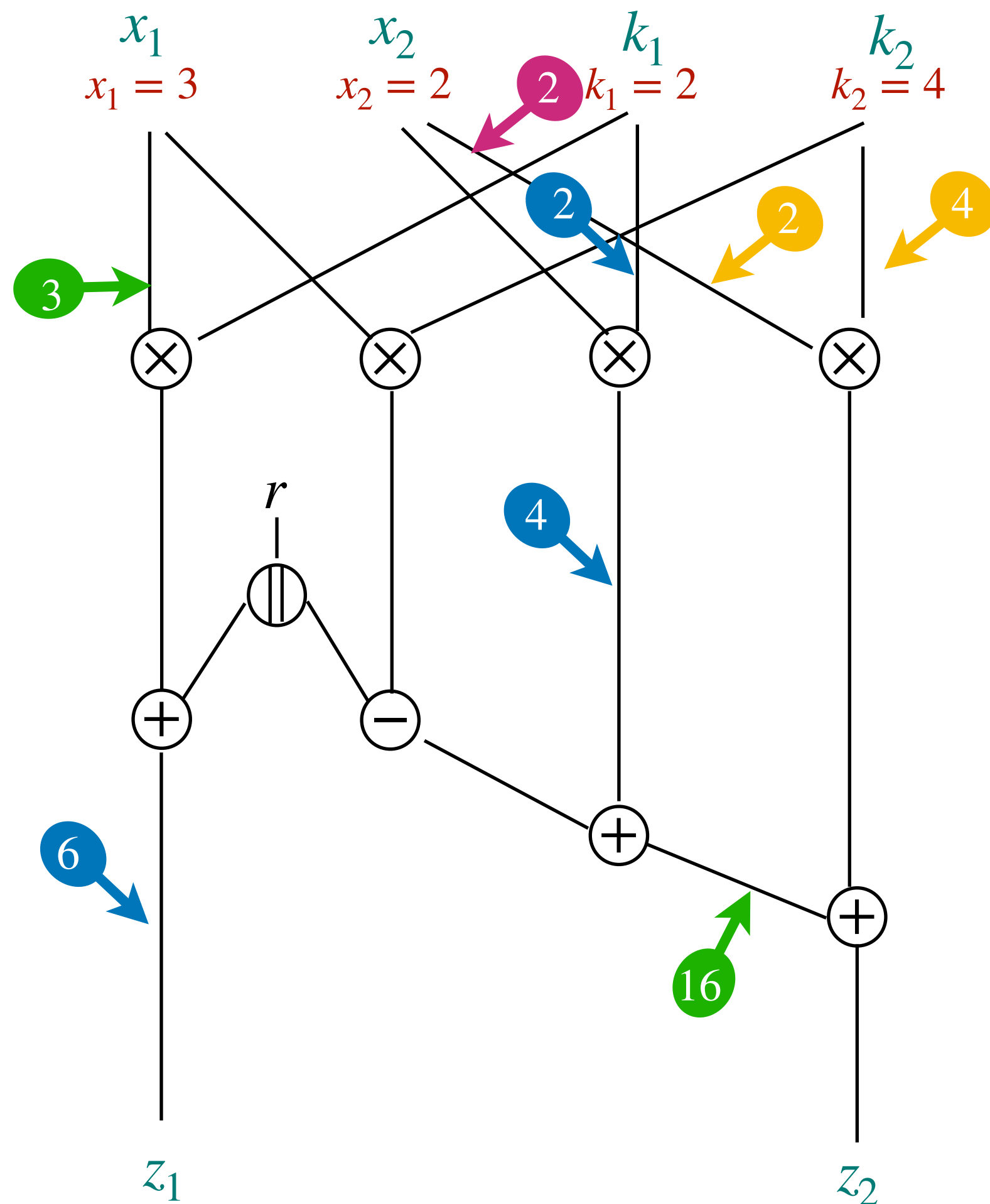
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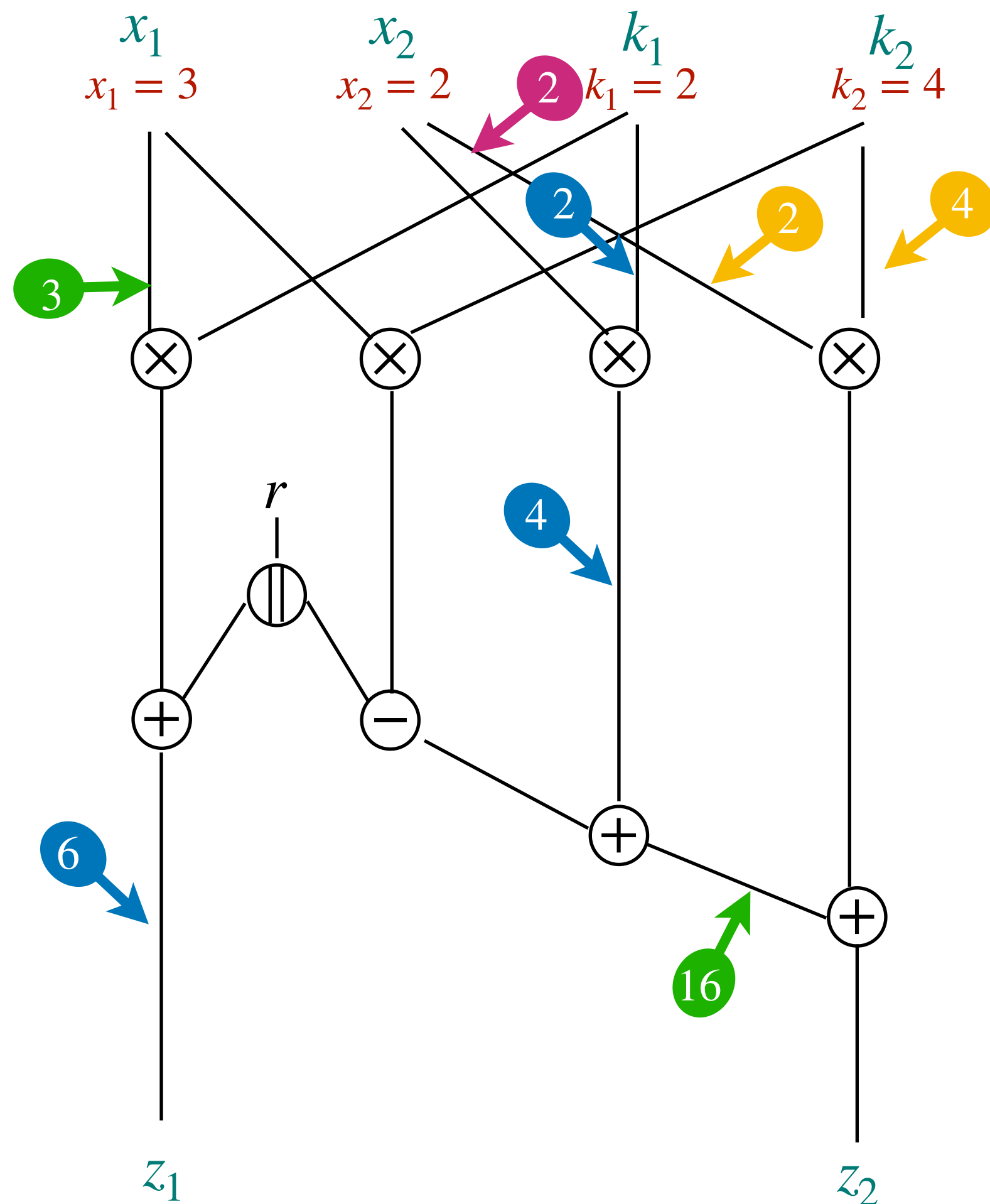
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1. Draw  $\mathcal{W}$
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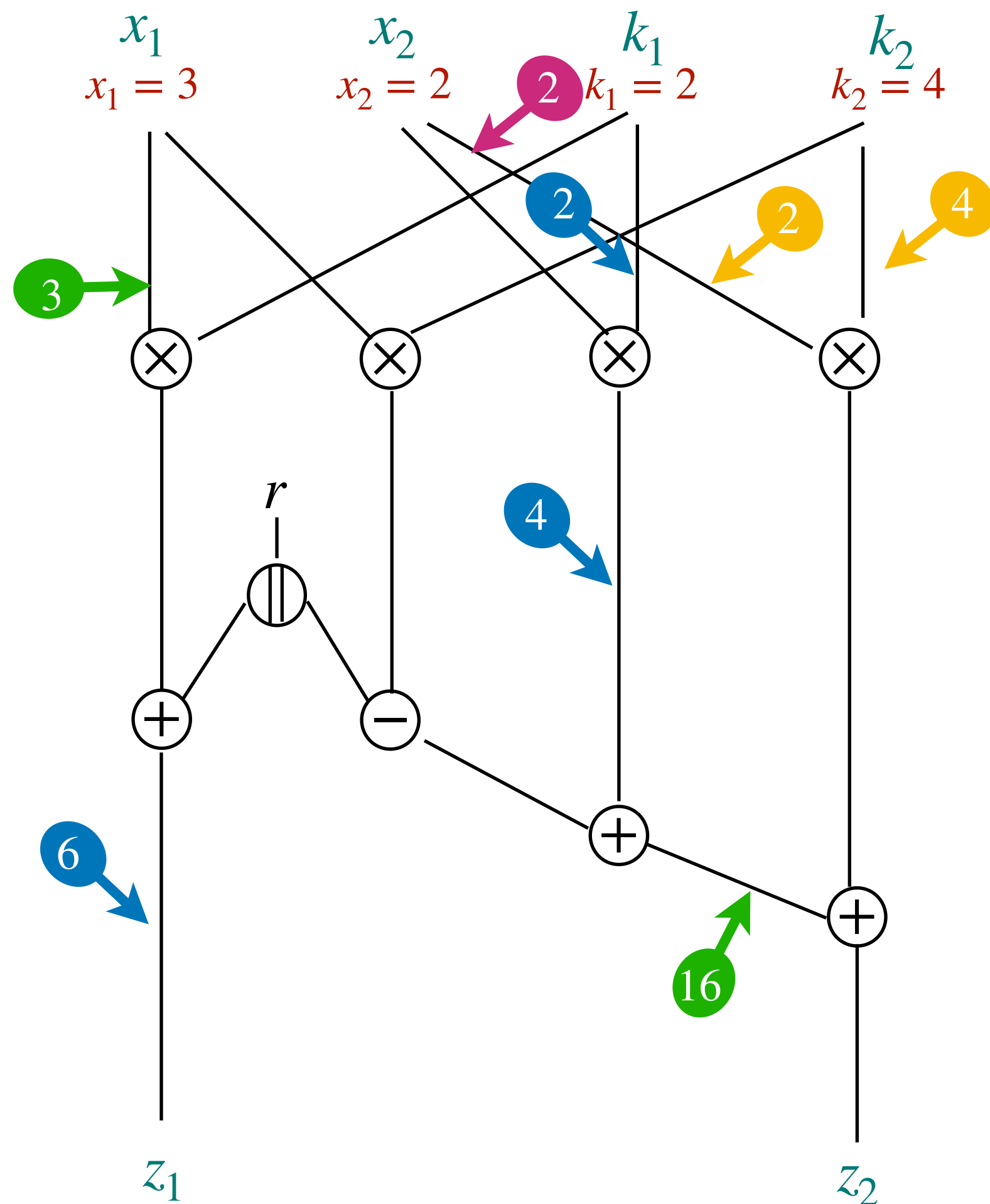
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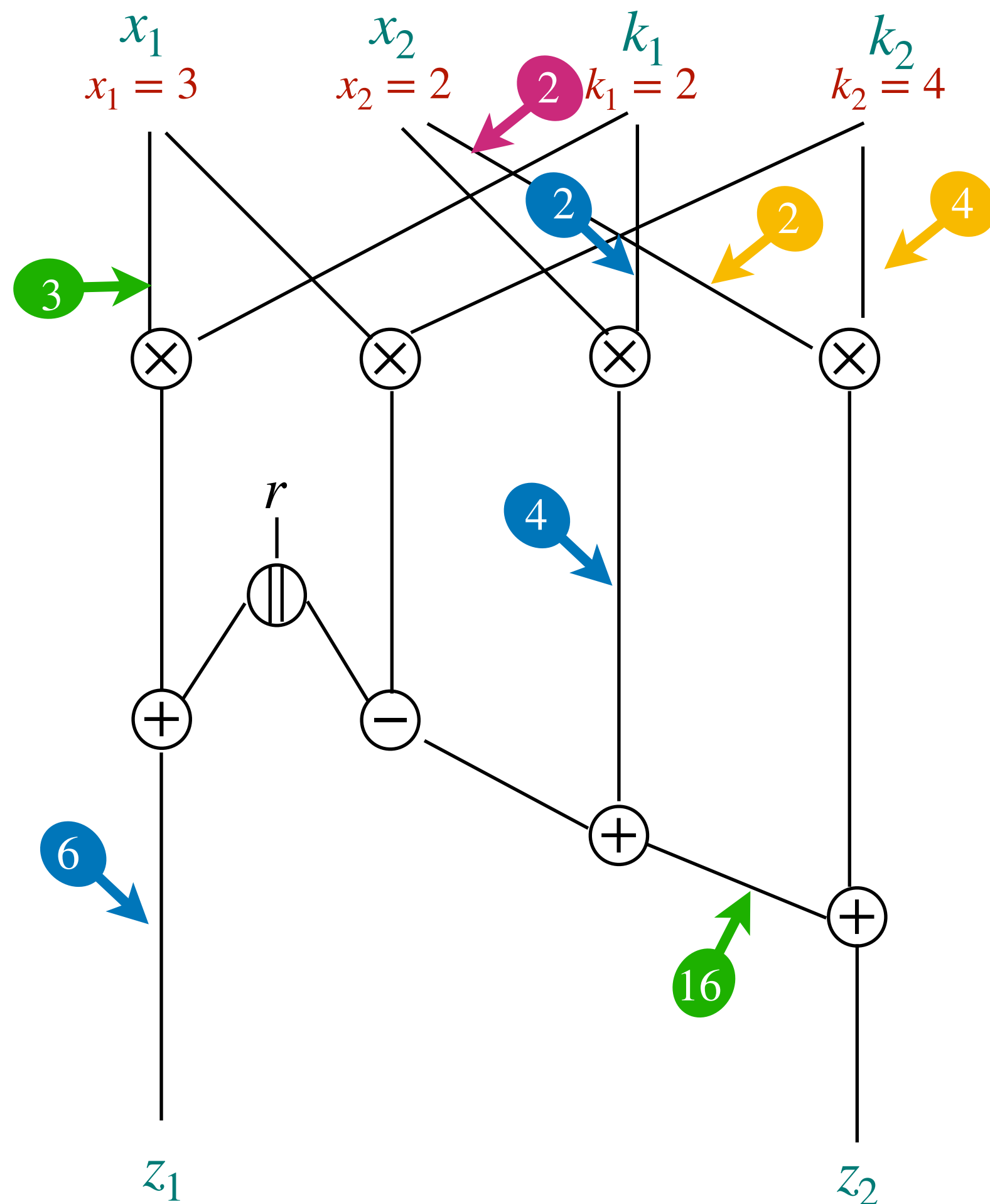
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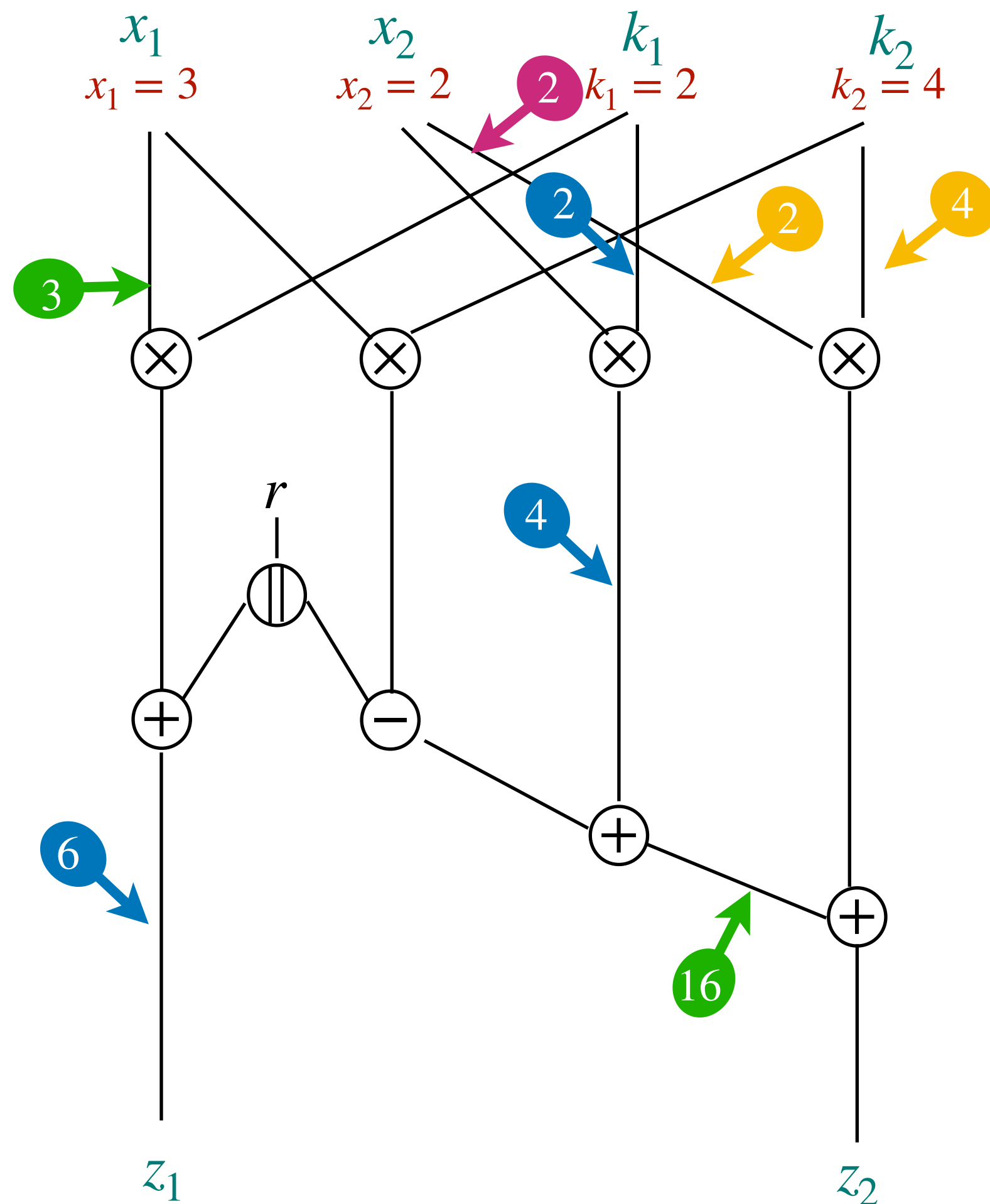
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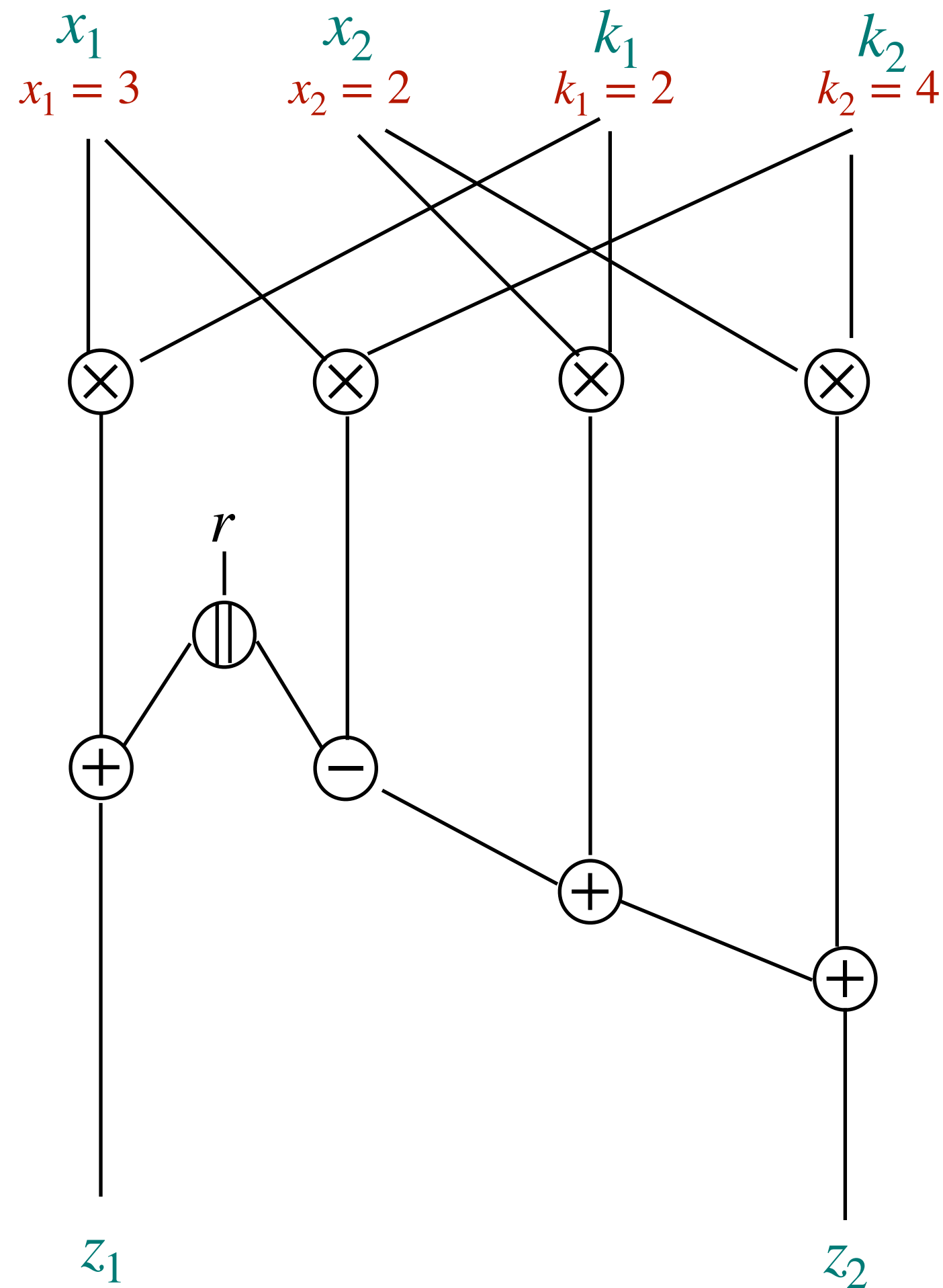
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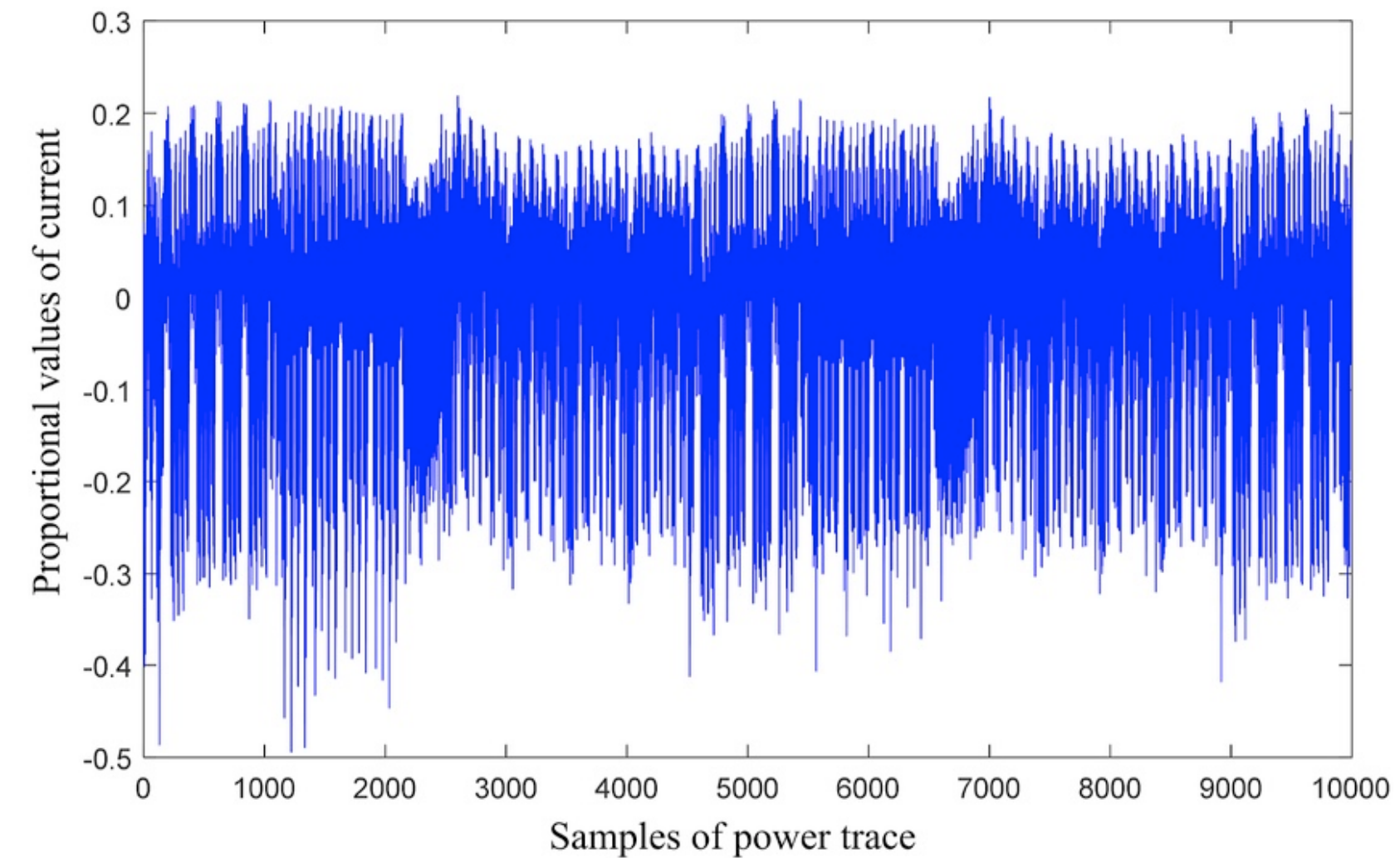
$\epsilon = 2^{-128} \implies p \geq \text{some bound}$

# Noisy leakage model



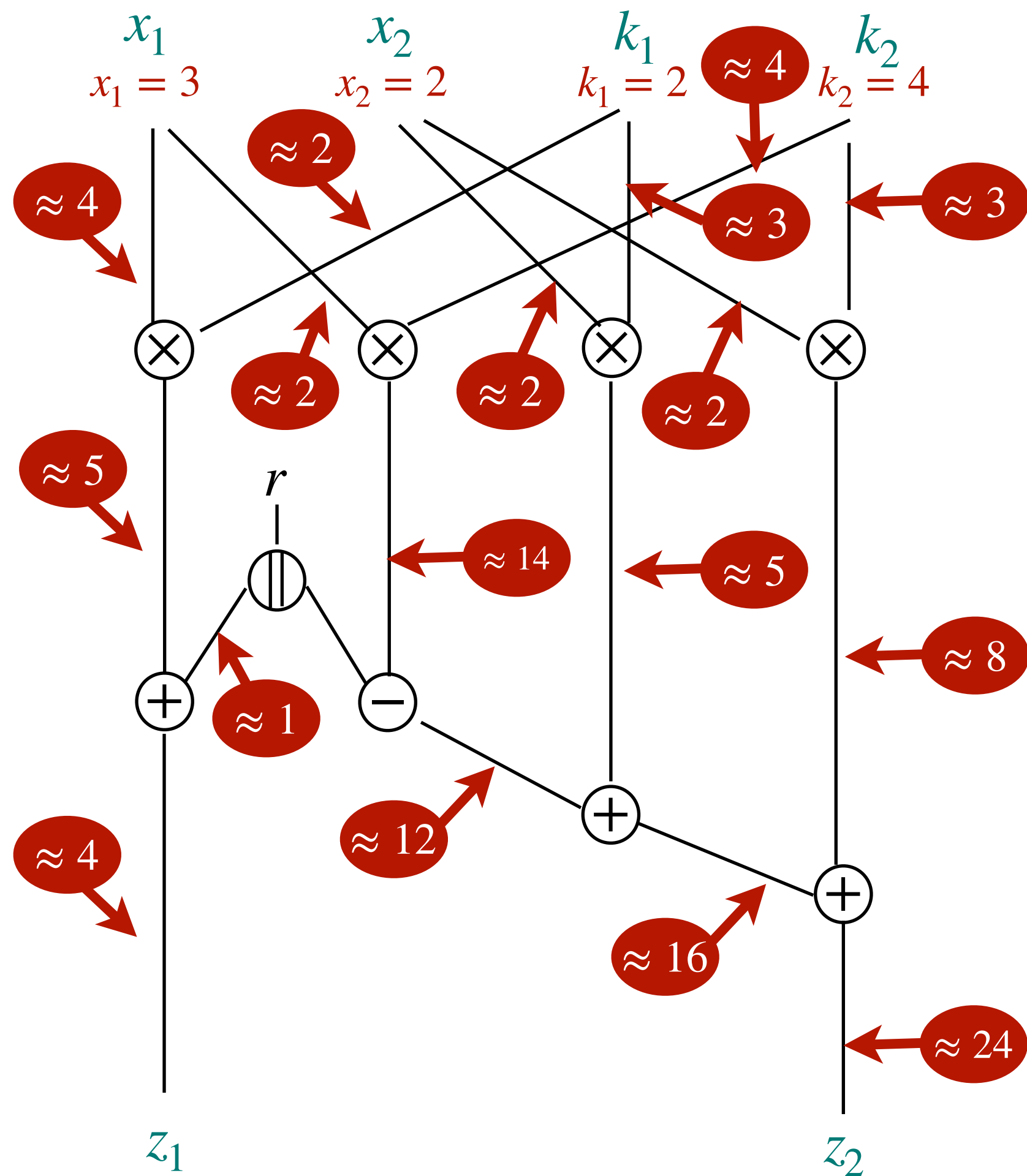
## Attacker model

The attacker is given the value of each wire with a certain noise. More precisely, the attacker gets  $\|_i (f(v_i) + \eta)$  for each wire  $v_i$ , noise  $\eta_i$  and a leakage function  $f$ .



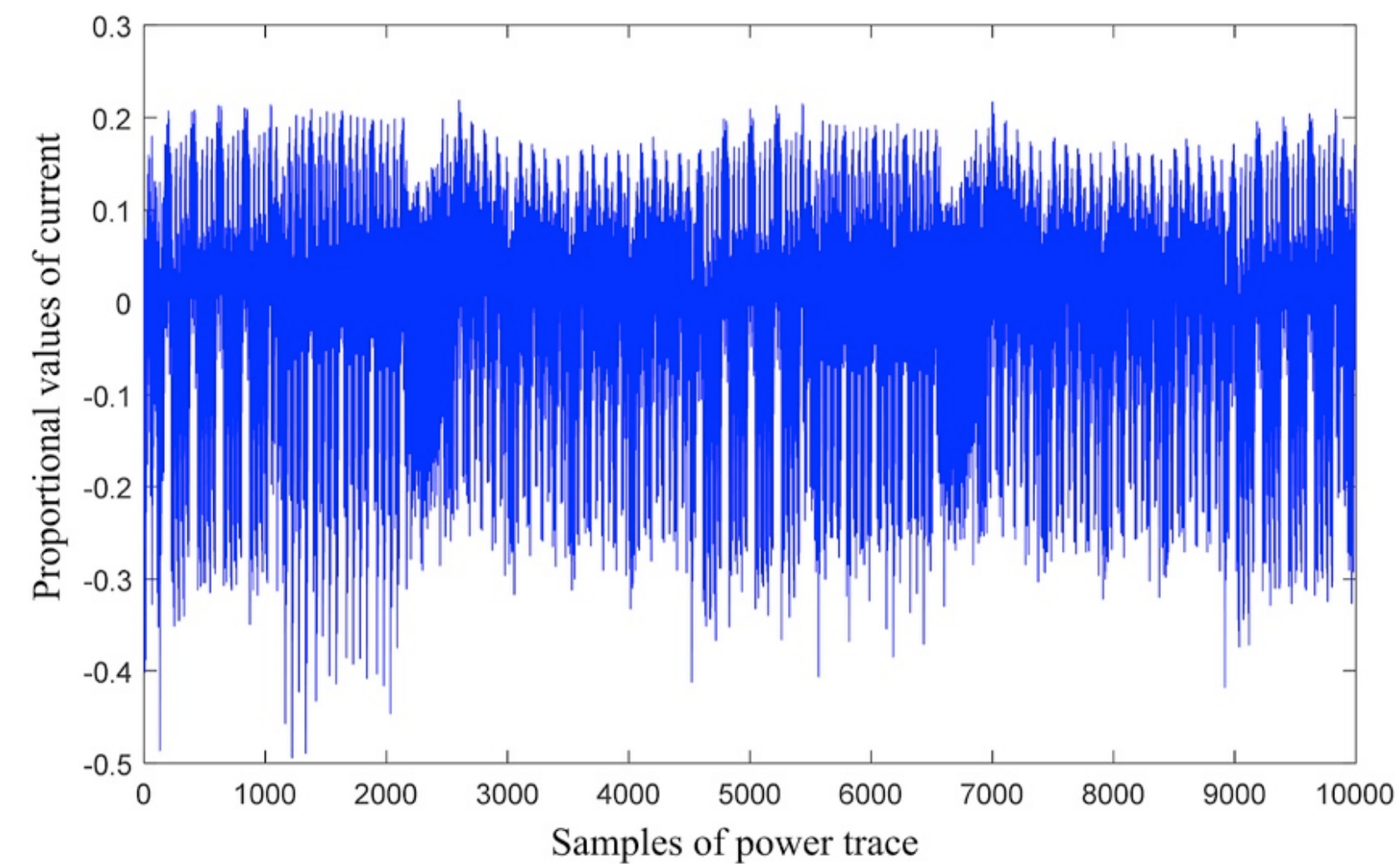
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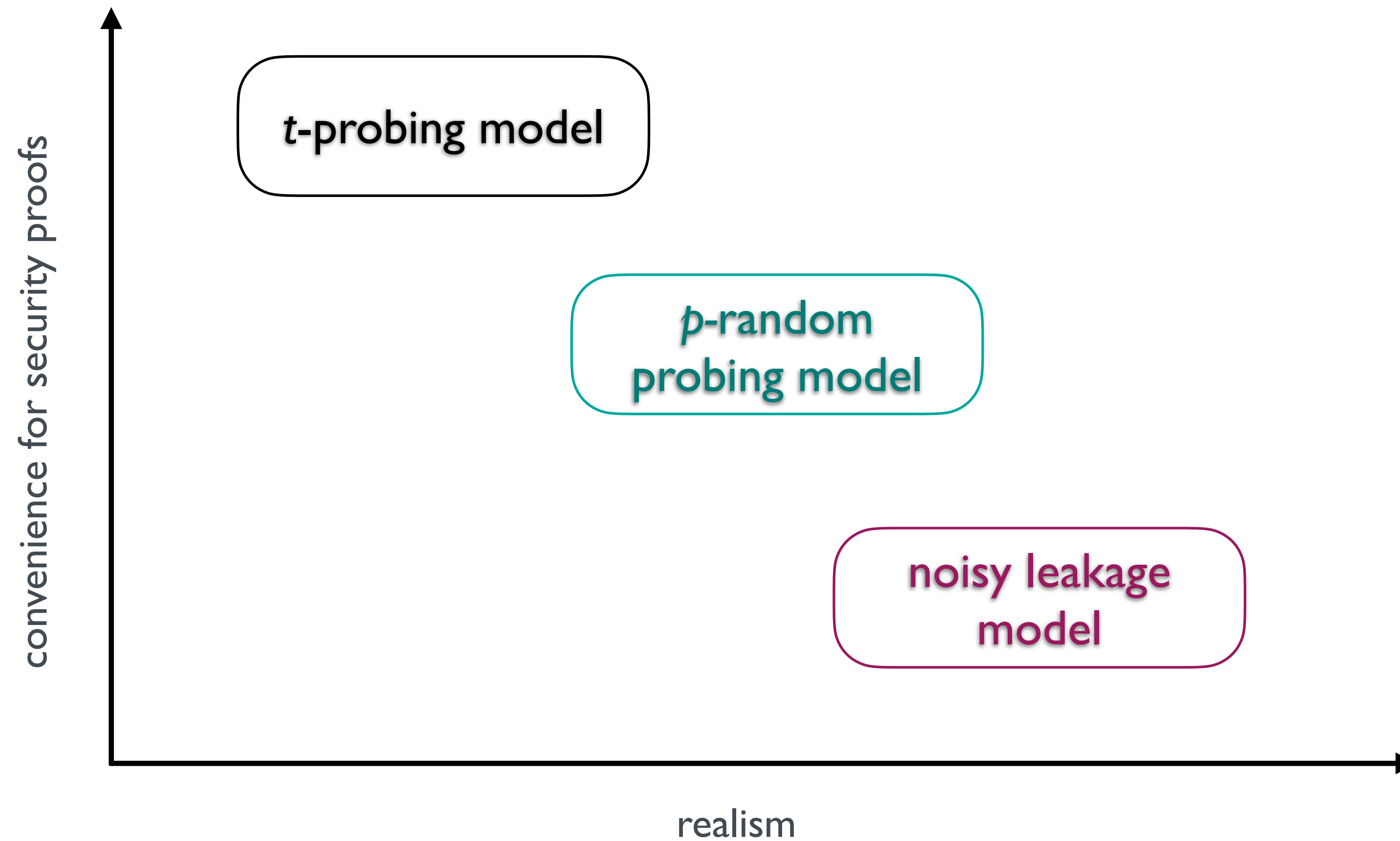
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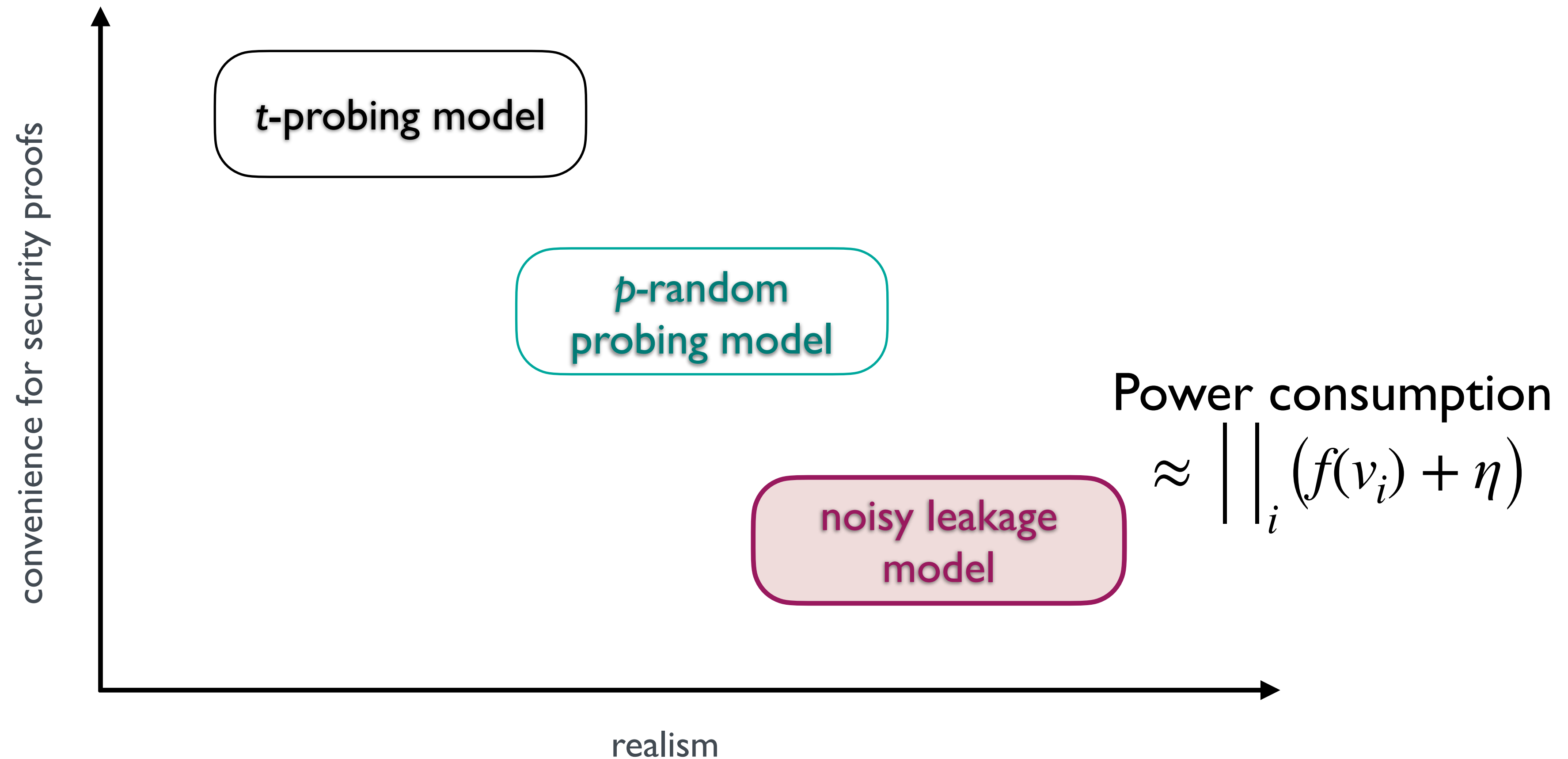


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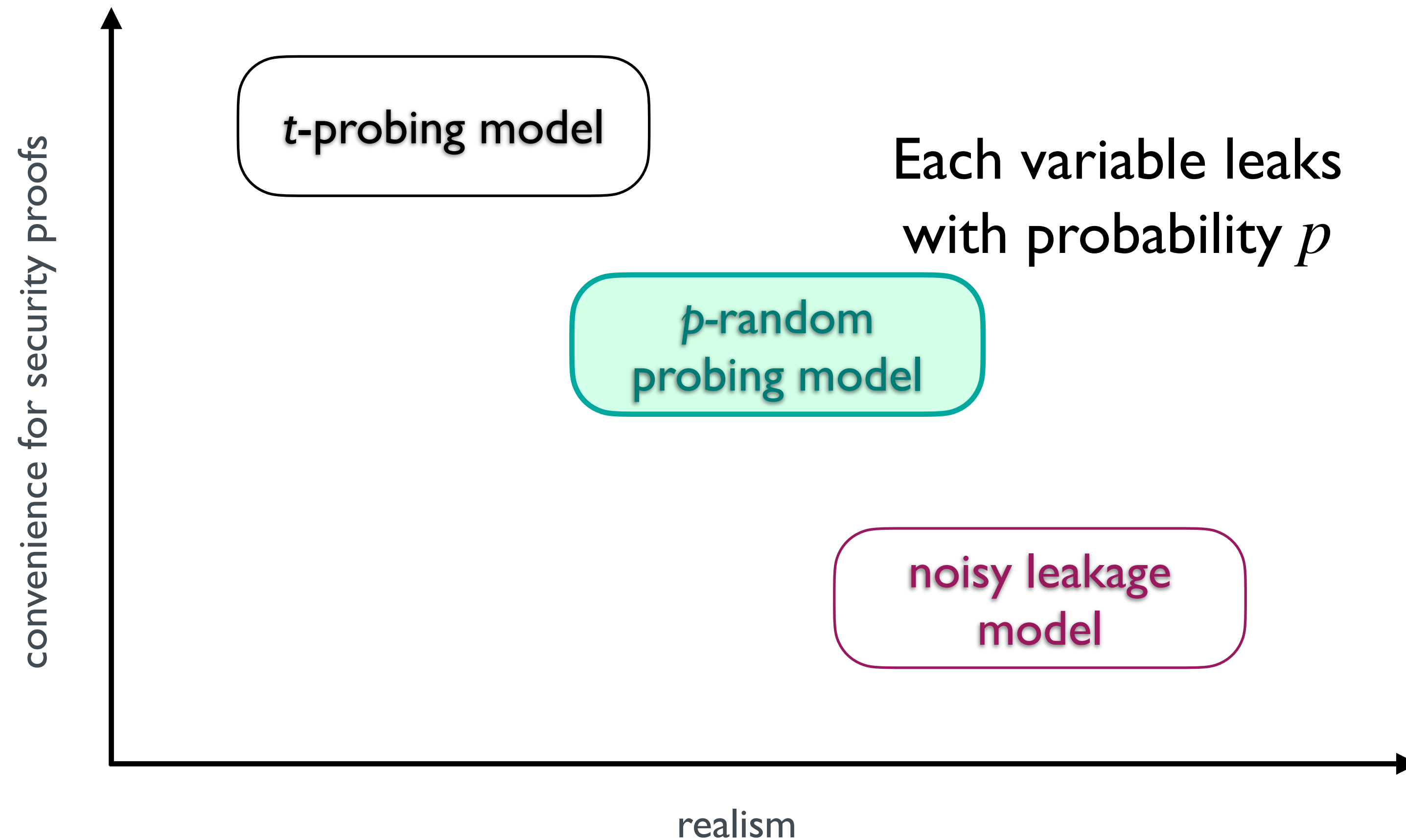
# Leakage Models



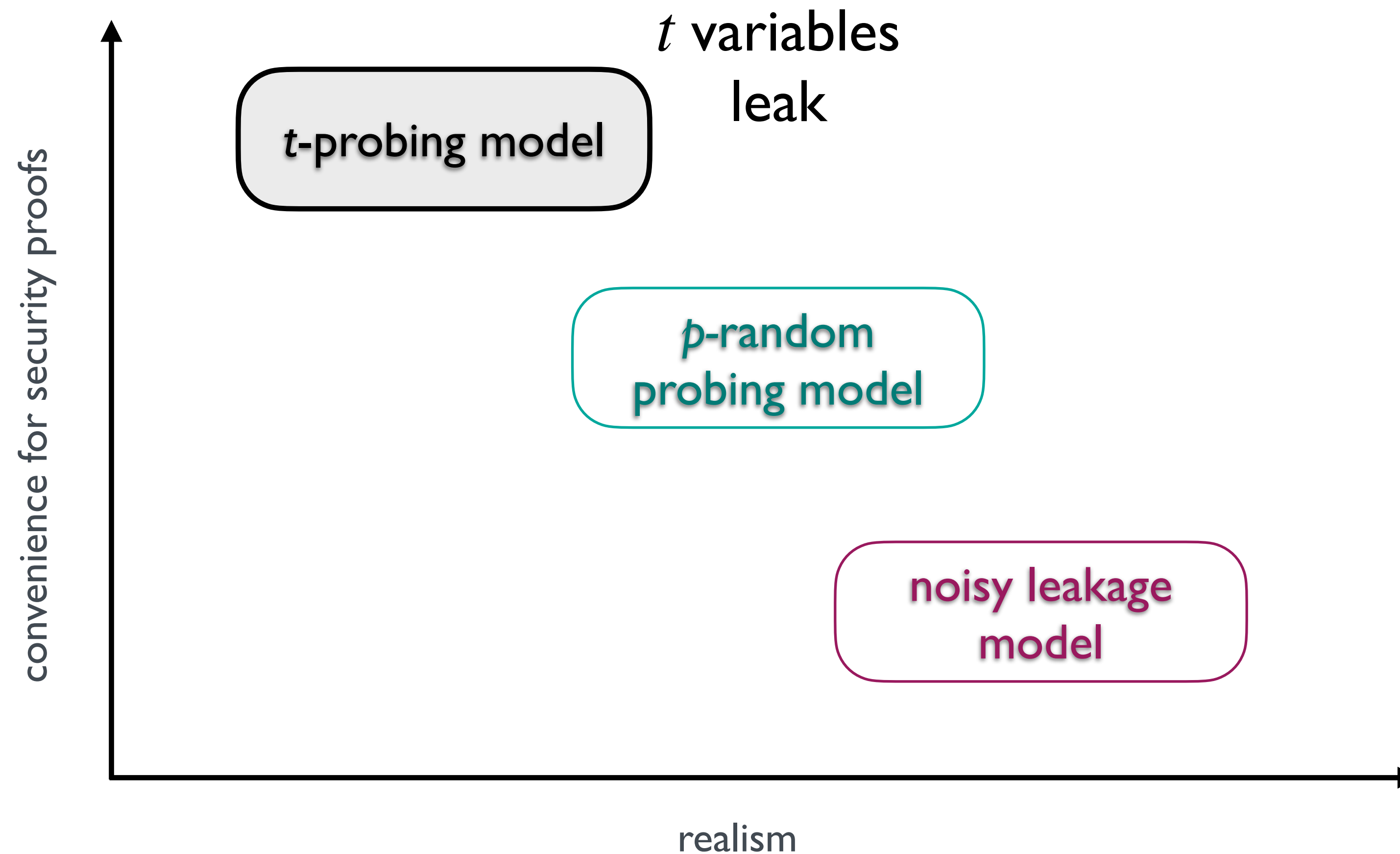
# Leakage Models



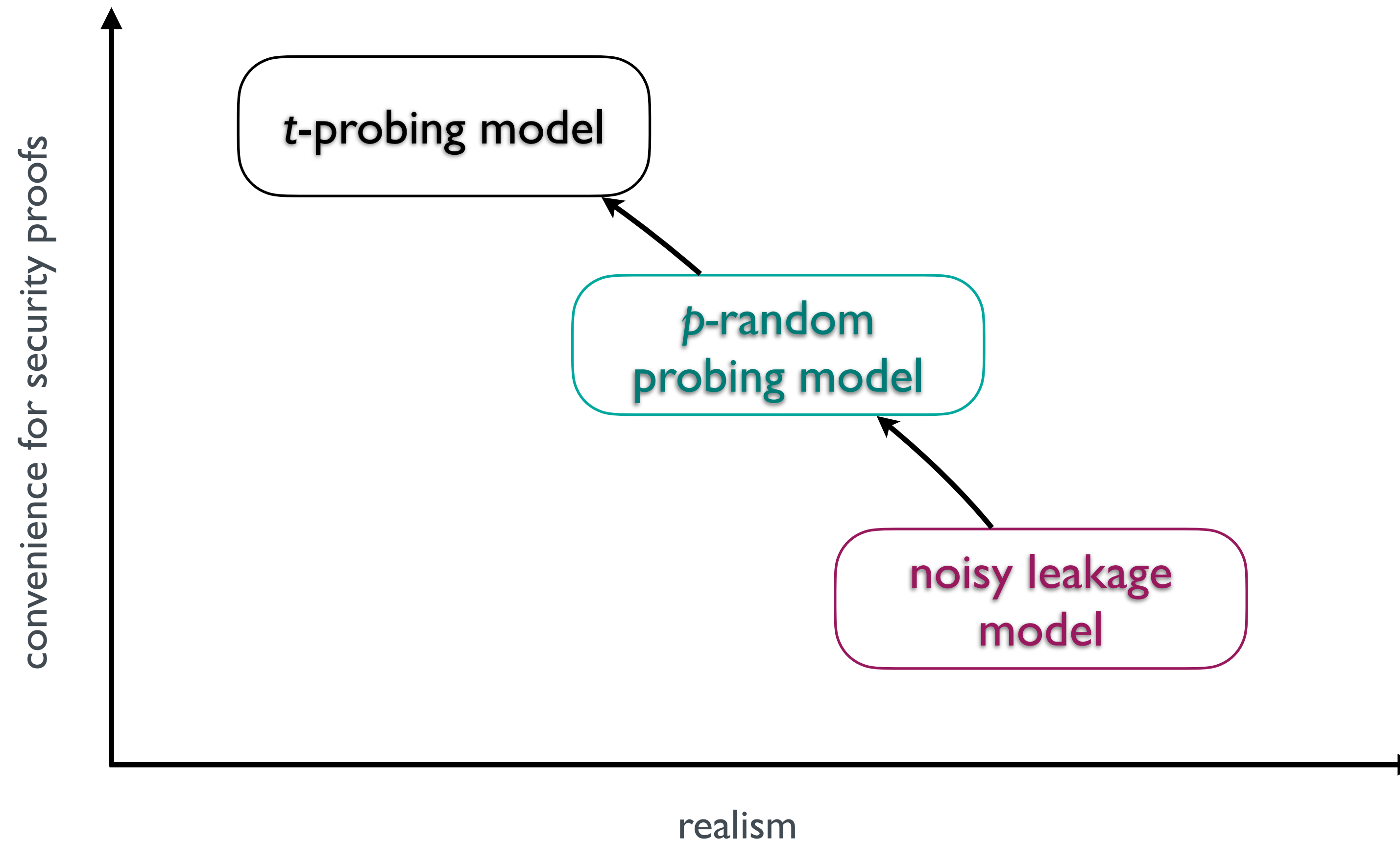
# Leakage Models



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[DDF14] *Unifying Leakage Models: From Probing Attacks to Noisy Leakage*. Alexandre Duc, Stefan Dziembowski, Sebastian Faust. Eurocrypt 2014



✓ Perfect simulation, can be immediately plugged into the black-box security.

➔ Extra information can be handled (e.g. [dPKPR24] , [BBEF+19] )

✓ Comprehensive toolbox for proofs: many gadgets and composition techniques.

❑ Loose reduction to the noisy leakage model

➔ Even with a perfectly identified leakage of a chip, the required masking order is prohibitively high.

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**t-probing model**

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➔ Masked implementations are provably secure up to a certain leakage probability  $p$ . For concrete chips,  $p$  can lie between  $2^{-15}$  to  $2^{-7}$  ([BCMRRST25])

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## $t$ -probing model

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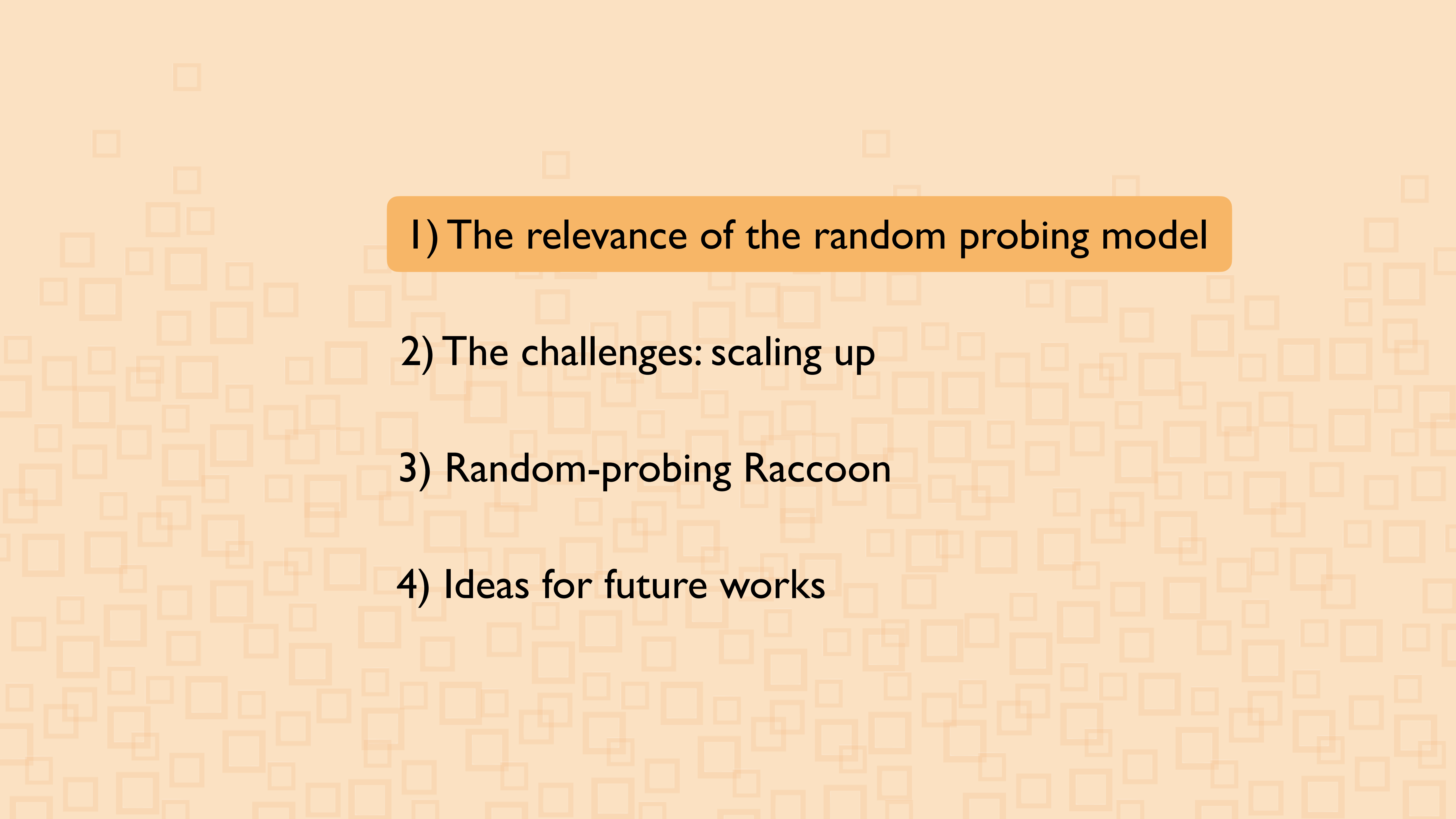
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1) The relevance of the random probing model

2) The challenges: scaling up

3) Random-probing Raccoon

4) Ideas for future works

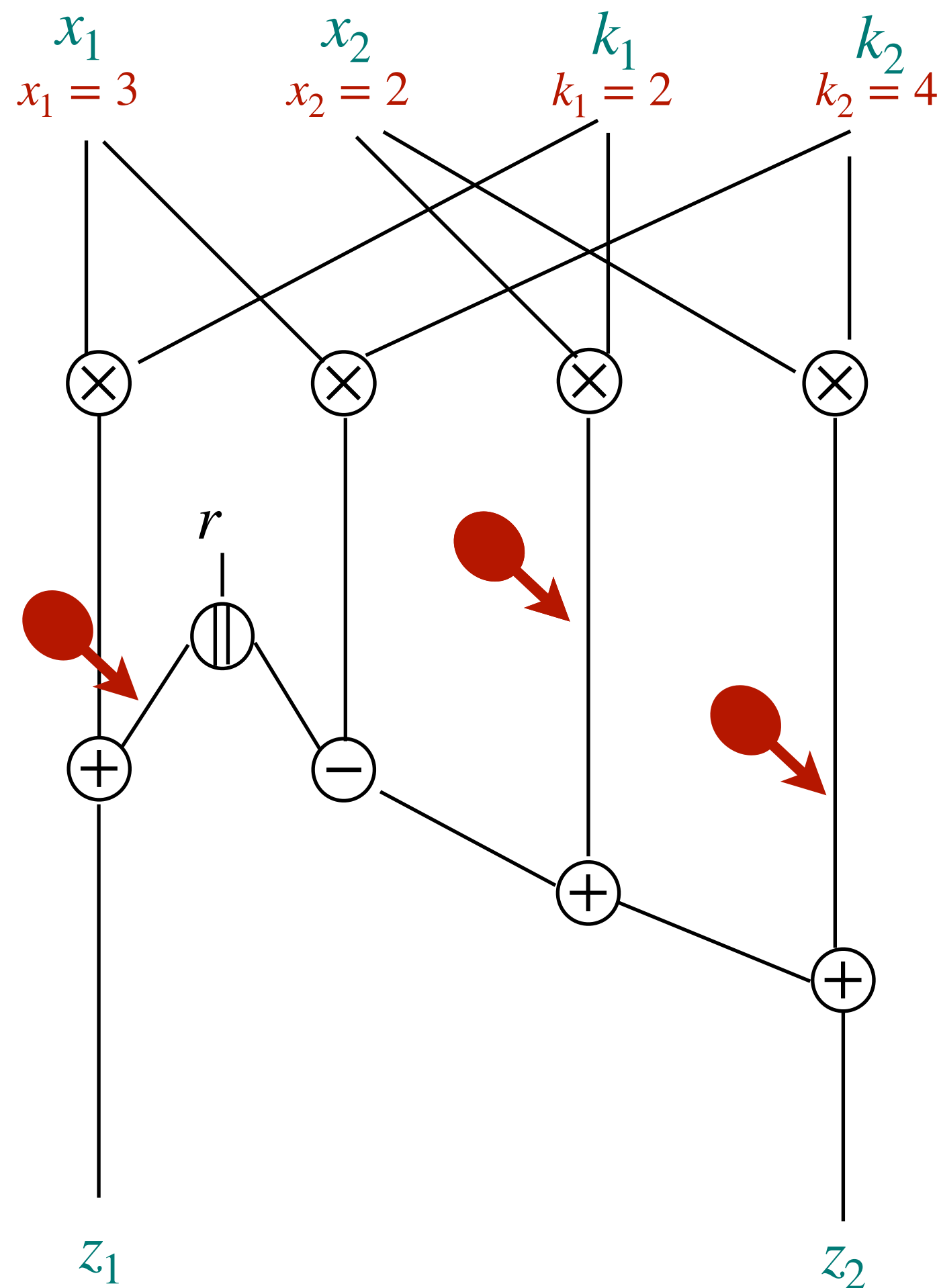
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# Random Probing Composability



## $(p, \epsilon, t)$ -random-probing composability

Let  $\mathcal{W}$  be a set of wires that are drawn with **prob.  $p$** .

Let  $(x_1, \dots, x_{t+1}), (k_1, \dots, k_{t+1})$  be uniform encodings of inputs  $x$  and  $k$ .

Let  $\mathcal{L} \leftarrow \text{AssignWires}(\mathcal{W}, (x_1, \dots, x_{t+1}), (k_1, \dots, k_{t+1}))$  be the values taken by the probes.

There exists a 2-stage simulator such that

$$I_x, I_k \leftarrow \text{SimIn}(\mathcal{W}) \text{ with } |I_x| \leq t \text{ and } |I_k| \leq t$$

$$\text{out} \leftarrow \text{SimOut}(x_{|I_x|}, k_{|I_k|})$$

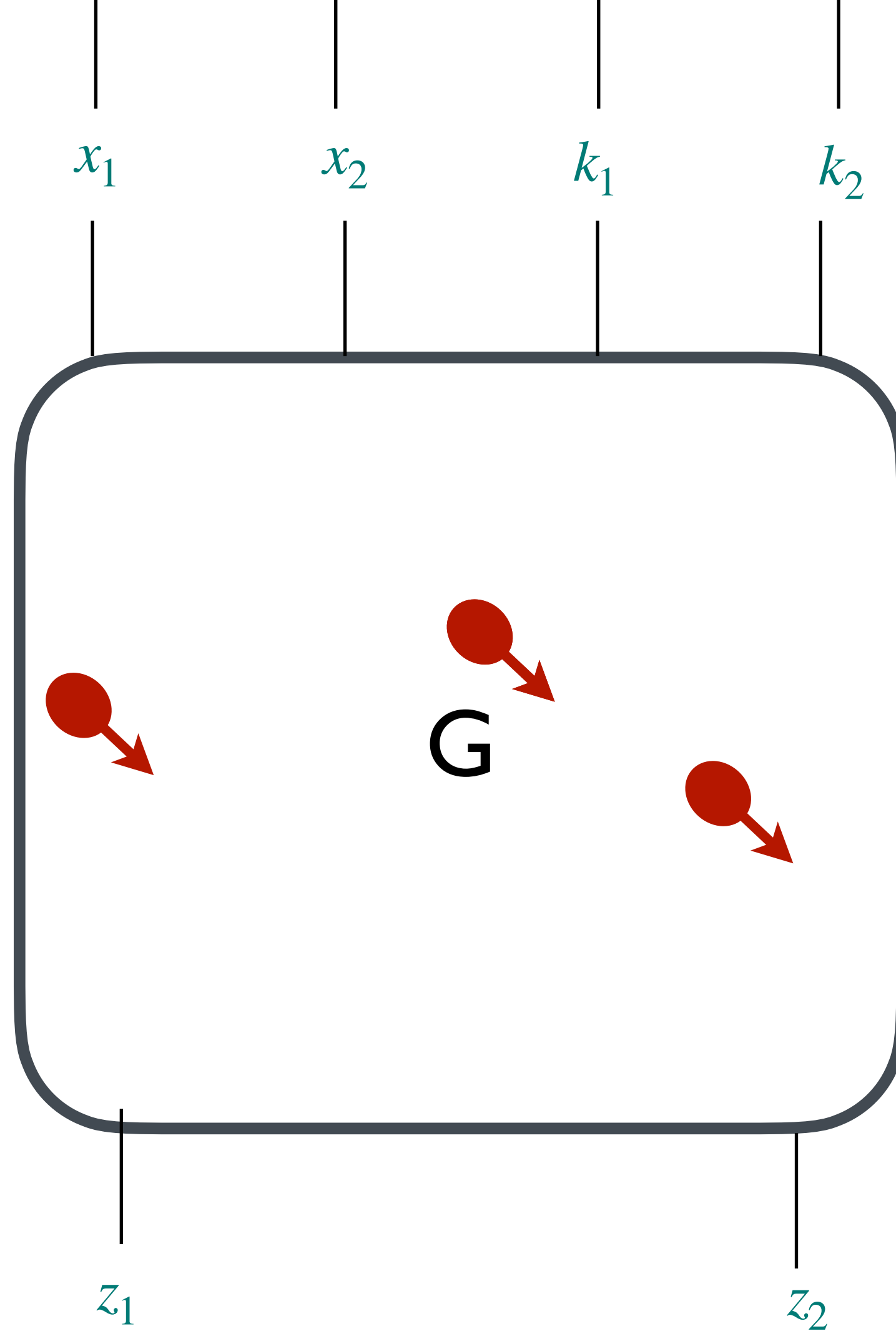
$$\text{and out} \stackrel{\epsilon}{\approx} \mathcal{L}$$

This is simplified, I ignored the leaking outputs.

$$\mathbb{P}(\text{« more than } t \text{ shares of each } [|x|] \text{ and } [|k|] \text{ are required to simulate } \mathcal{L} \text{ »}) \leq \epsilon$$

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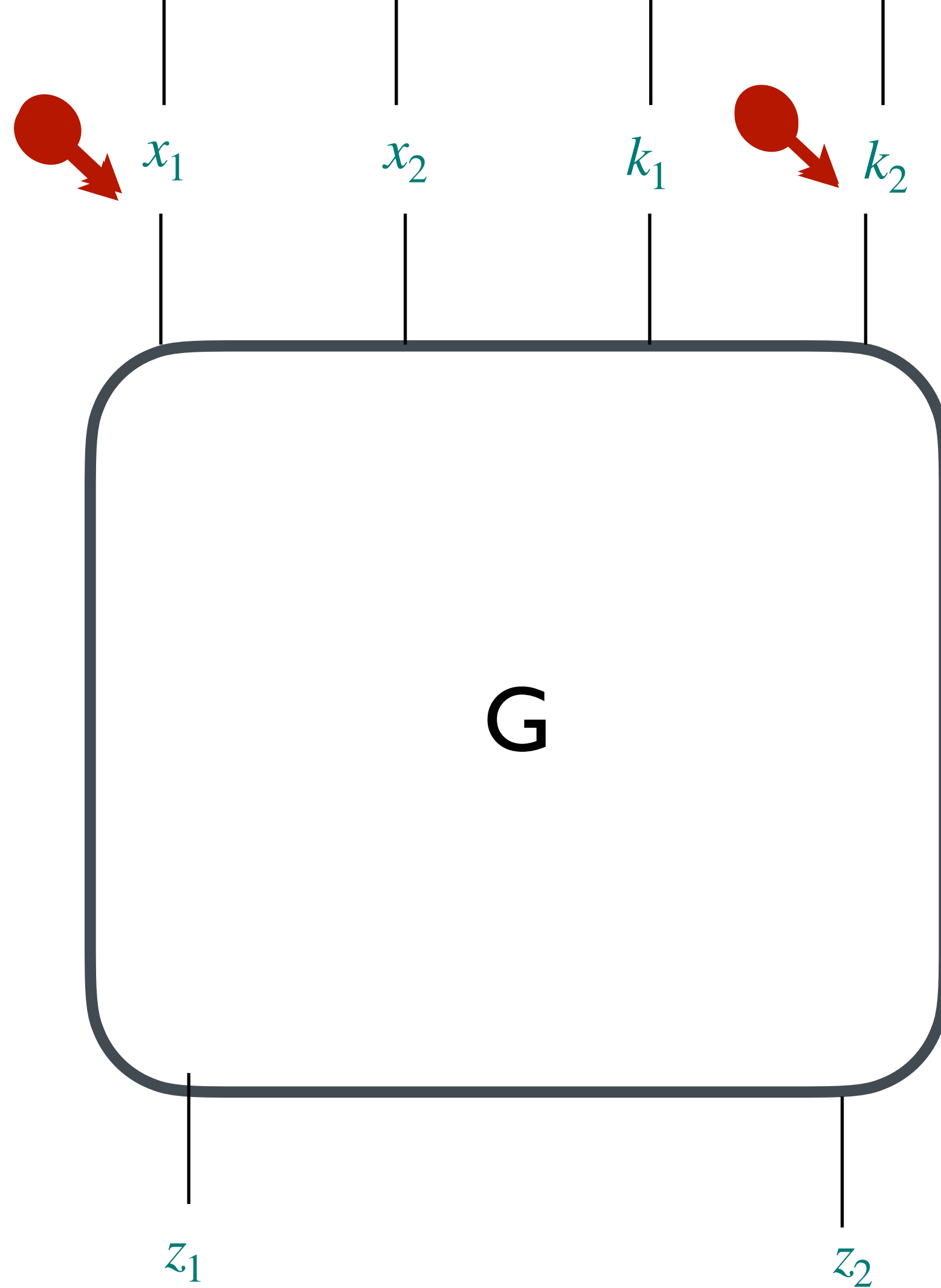
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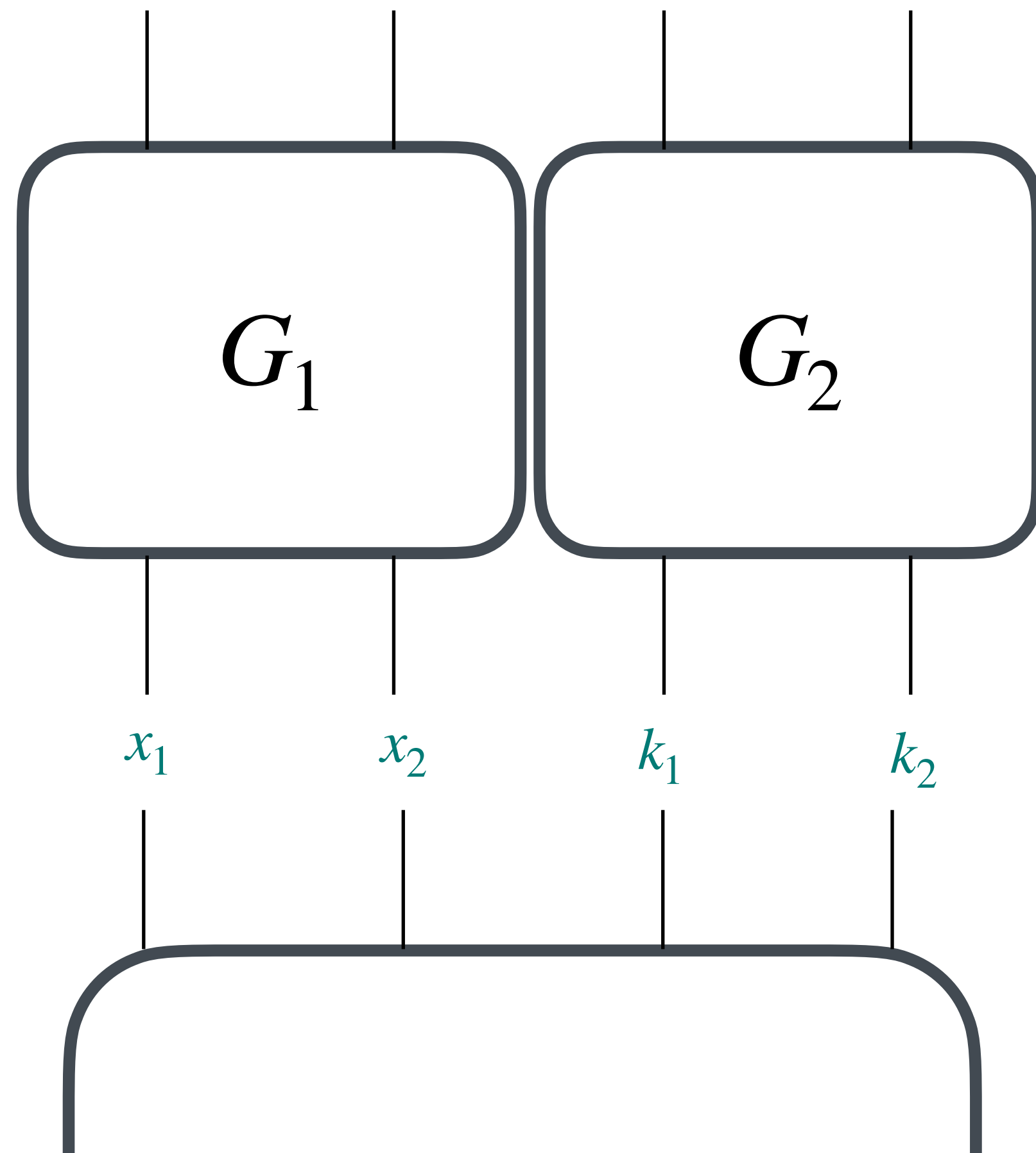
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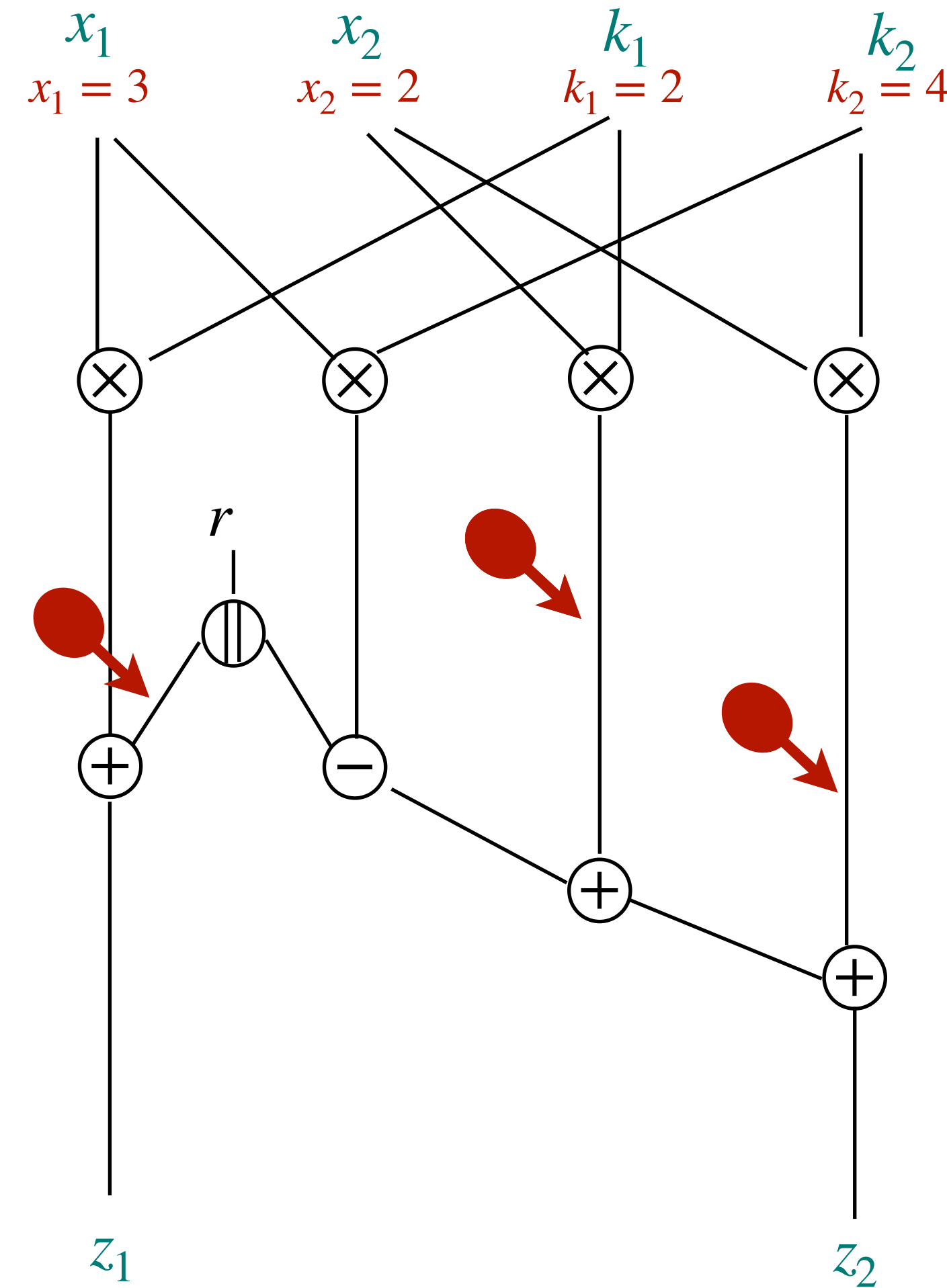
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# Random Probing Composability

RPC:

Propagation of the simulation  
from inside to gadget to its inputs

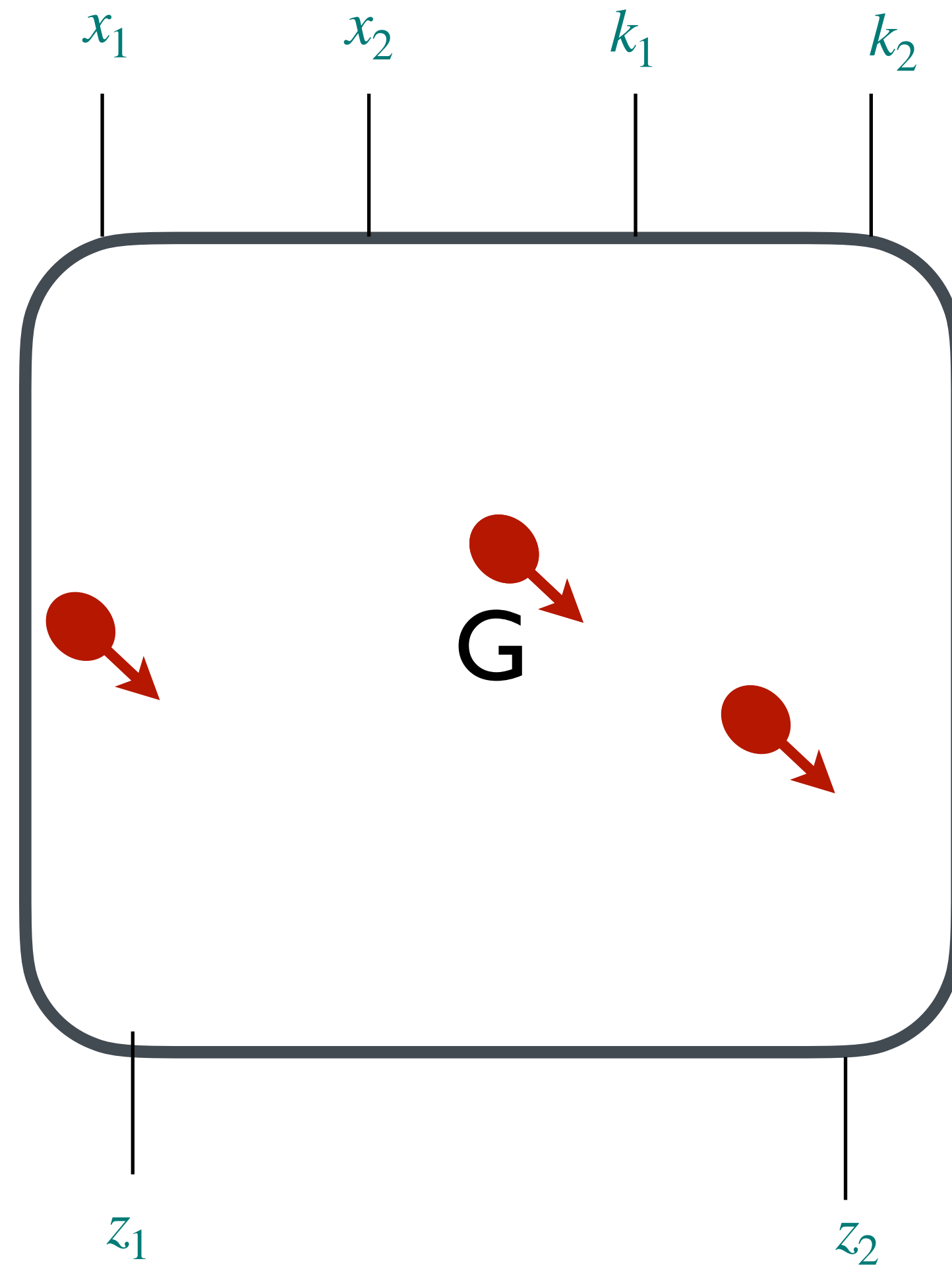


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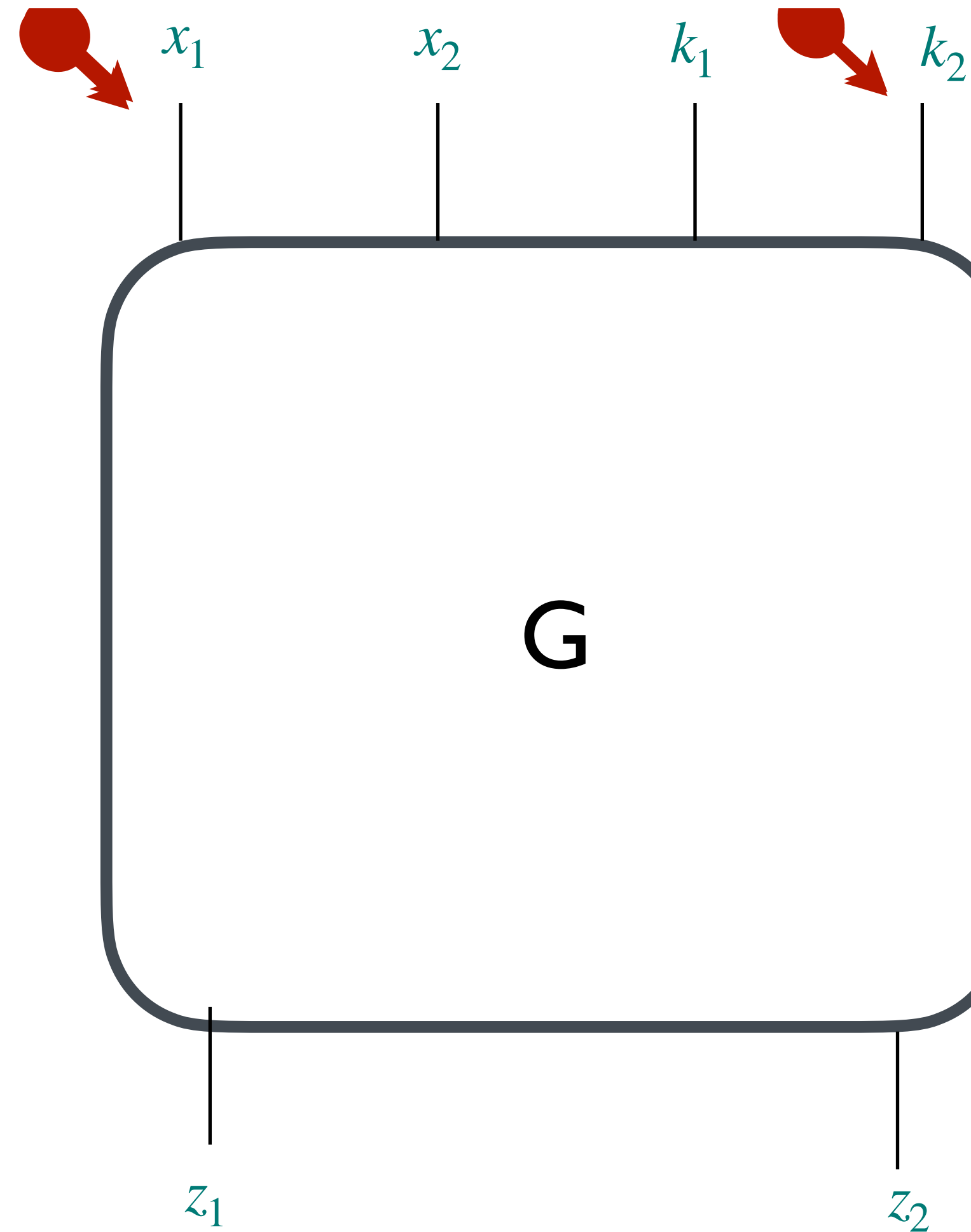


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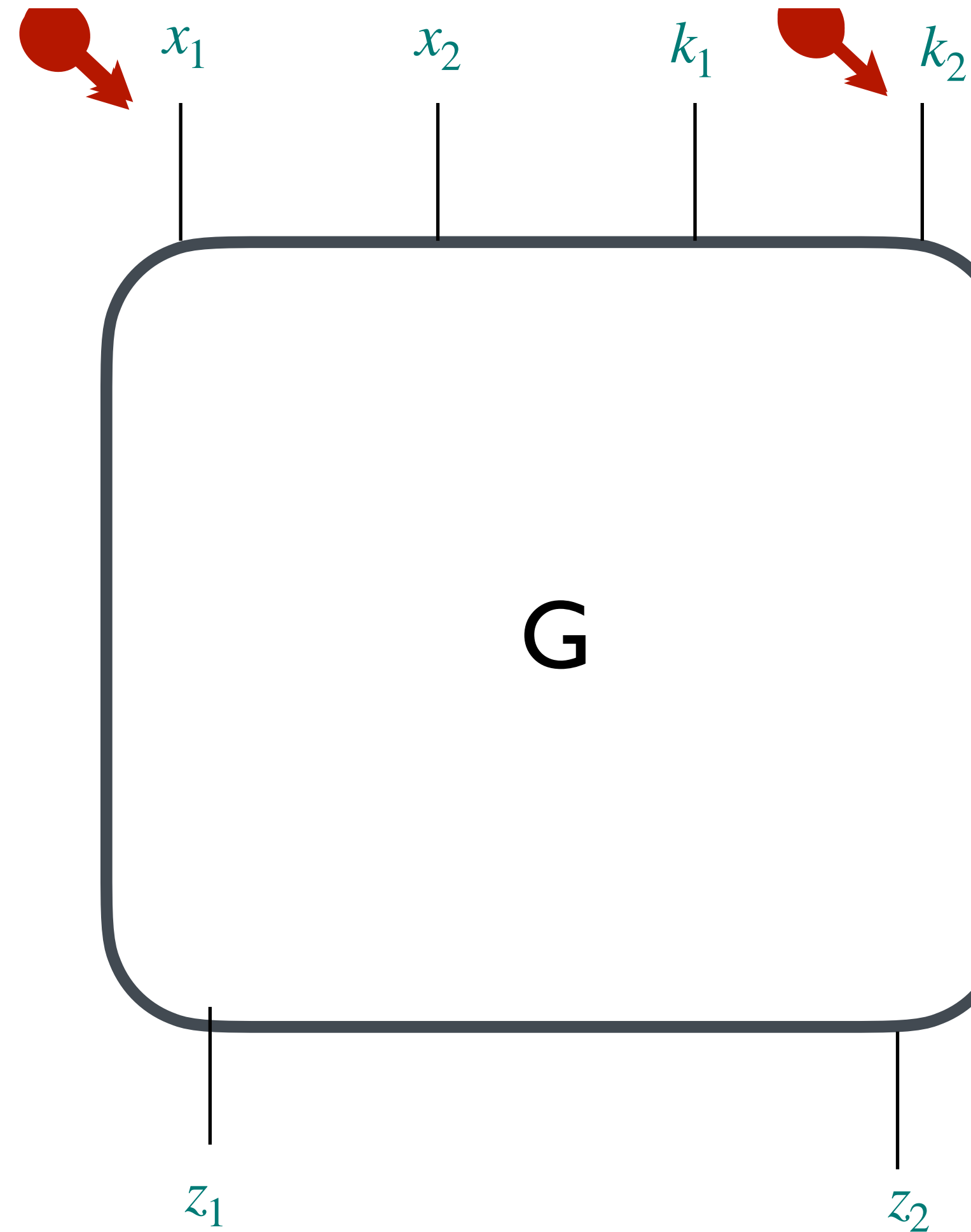
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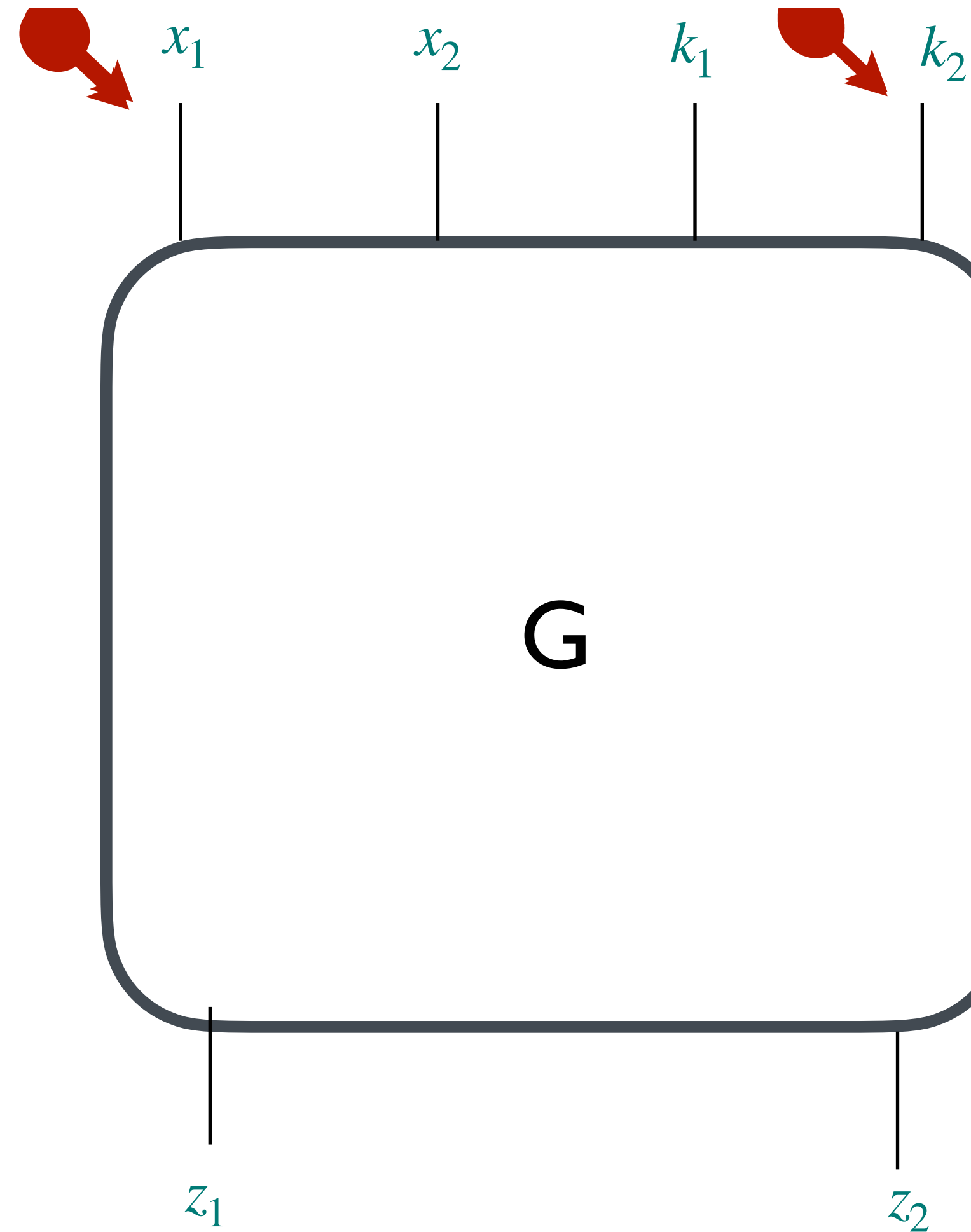
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Composition

A circuit composed of  $(t, p, \epsilon_i)$ -RPC gadgets  
will itself be  $(t, p, \epsilon)$ -RPC with

$$\epsilon = 1 - \prod_{i=0}^k (1 - \epsilon_i).$$

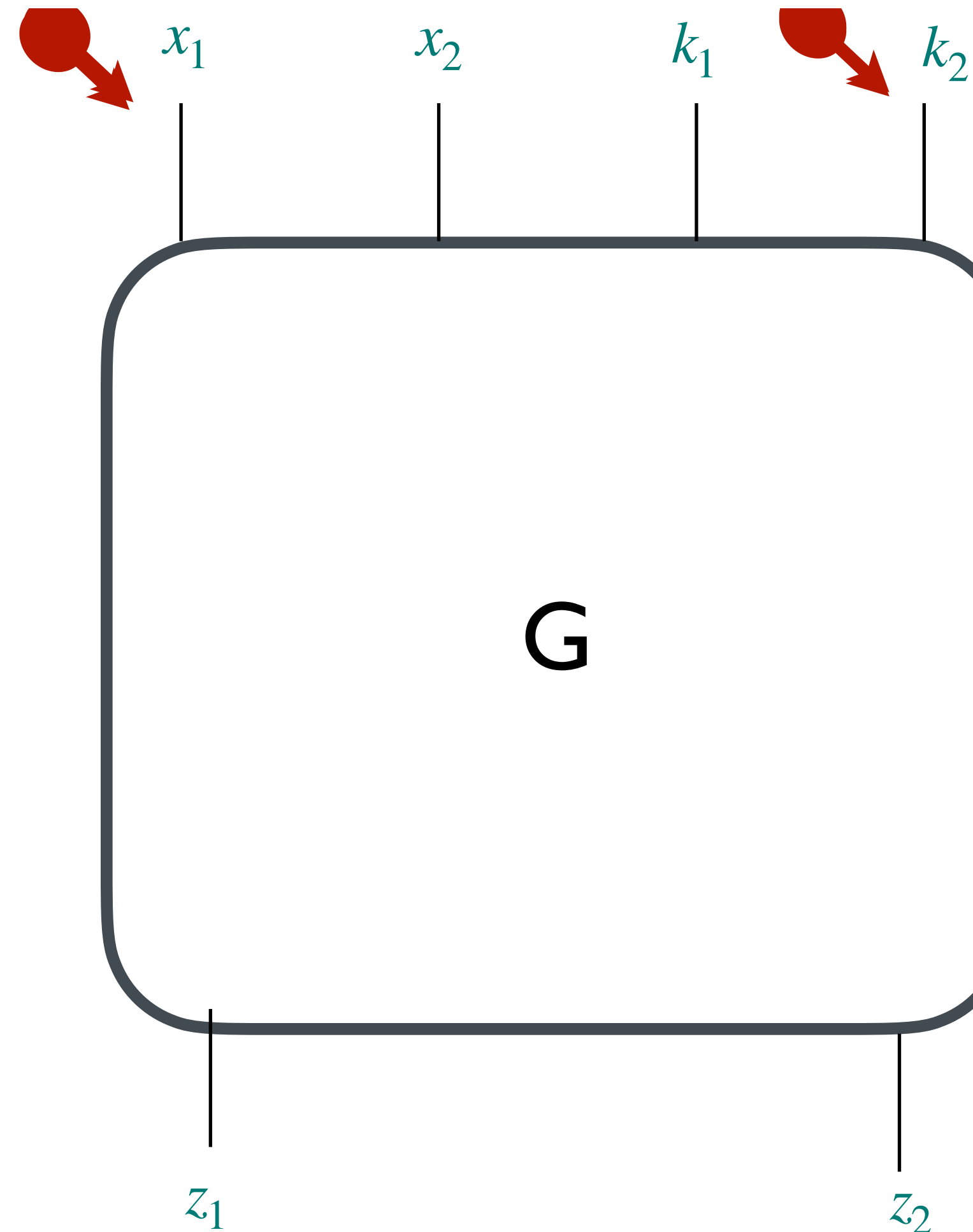
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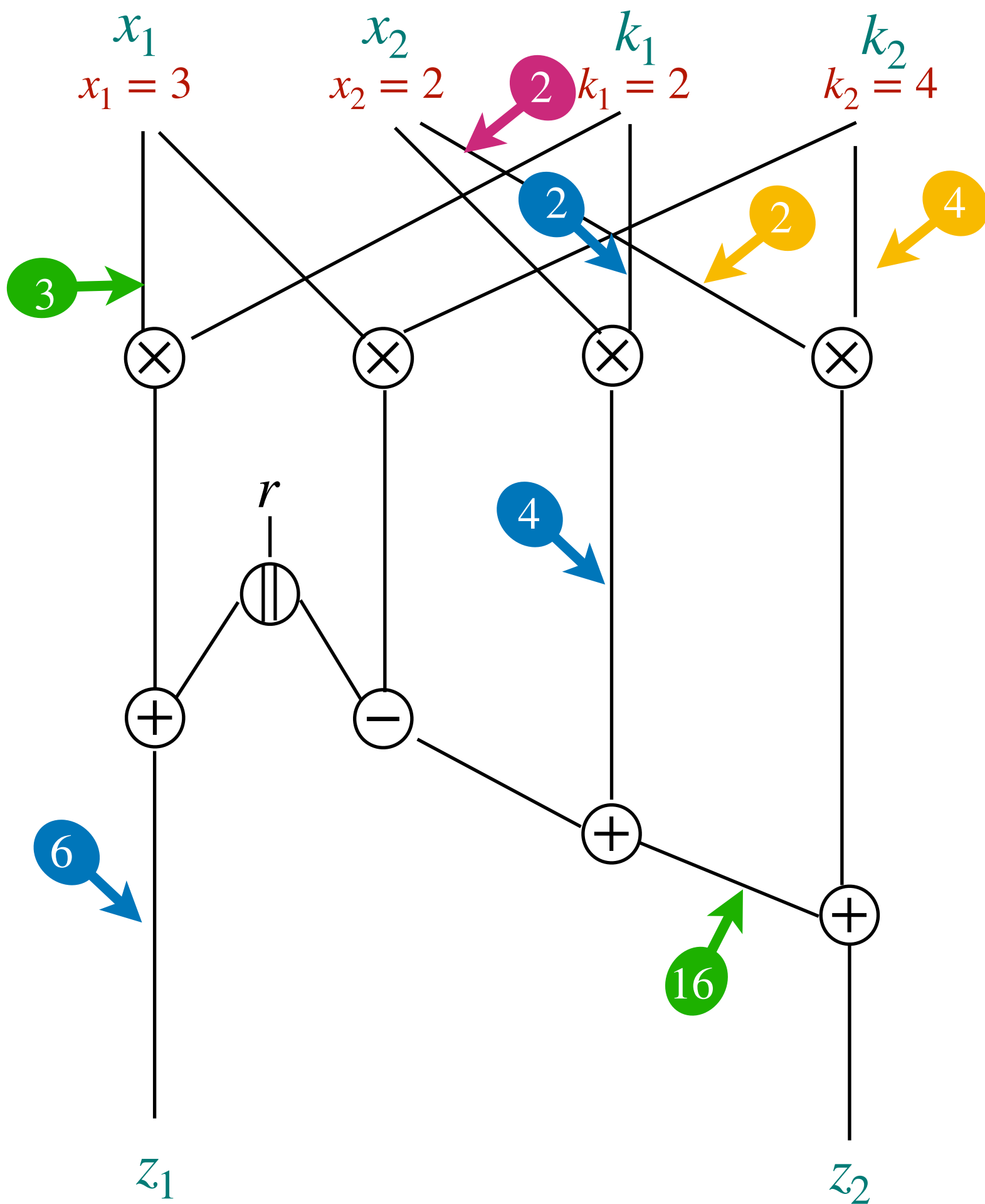
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The more gadgets, the higher the  
simulation is likely to fail.

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# Random Probing Composability

How to estimate the simulation failure probability  $\epsilon$  ?



$\mathcal{W} = \emptyset$  with proba  $(1 - p)^{19}$

$\mathcal{W} = \{x_2\}$  with proba  $p(1 - p)^{18}$   
 $\mathcal{L} = \{2\}$

$\mathcal{W} = \{x_1, r''\}$  with proba  $p^2(1 - p)^{17}$   
 $\mathcal{L} = \{3, 16\}$

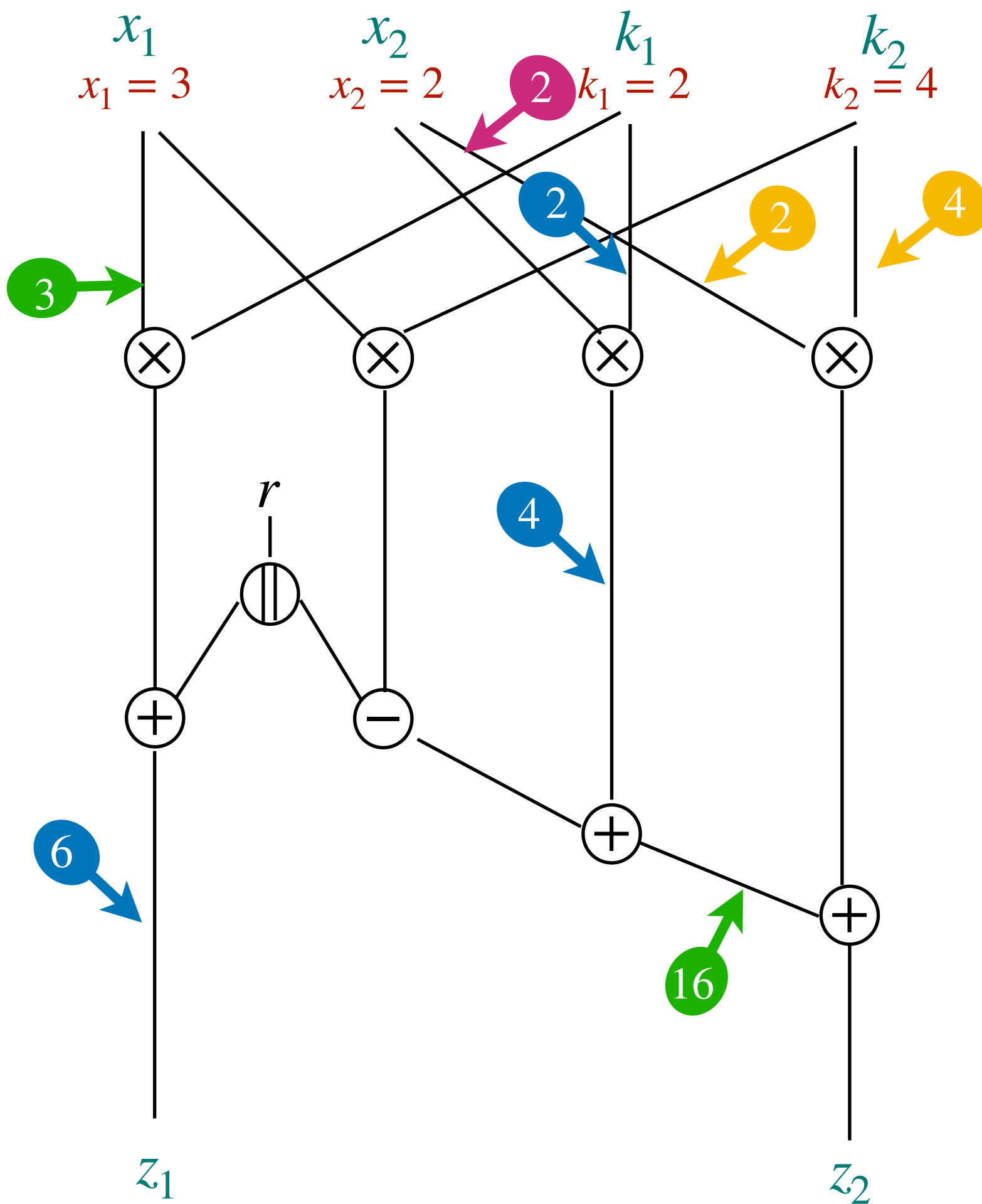
$\mathcal{W} = \{k_1, k_2\}$  with proba  $p^2(1 - p)^{17}$   
 $\mathcal{L} = \{2, 4\}$

$\mathcal{W} = \{x_1 k_1 + r, x_2 k_1, k_1\}$  with proba  $p^3(1 - p)^{16}$   
 $\mathcal{L} = \{6, 4, 2\}$

...  $\approx 2^{19}$  possible sets  $\mathcal{W}$

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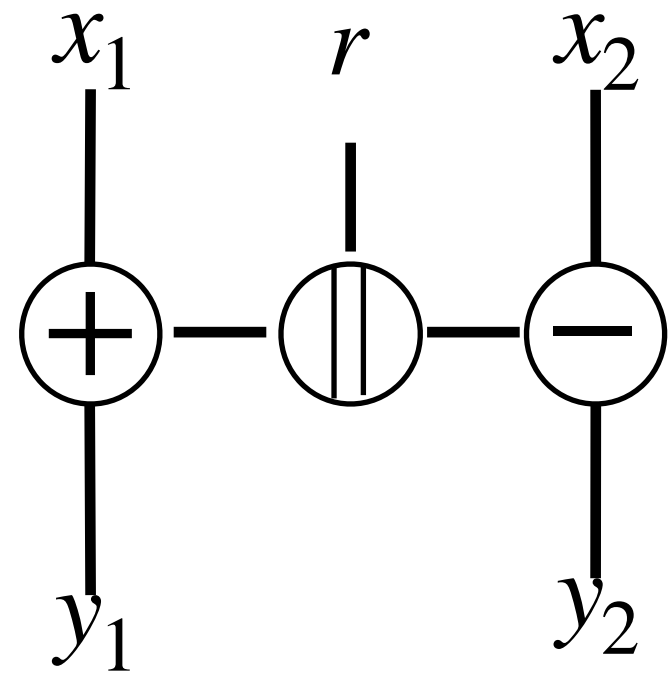
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...  $\approx 2^{19}$  possible sets  $\mathcal{W}$

We need to

- 1) Identify all the sets  $\mathcal{W}$  that cannot be simulated
- 2) Compute the probability to draw one of them.

# How to concretely compute the $\epsilon$ ?



## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

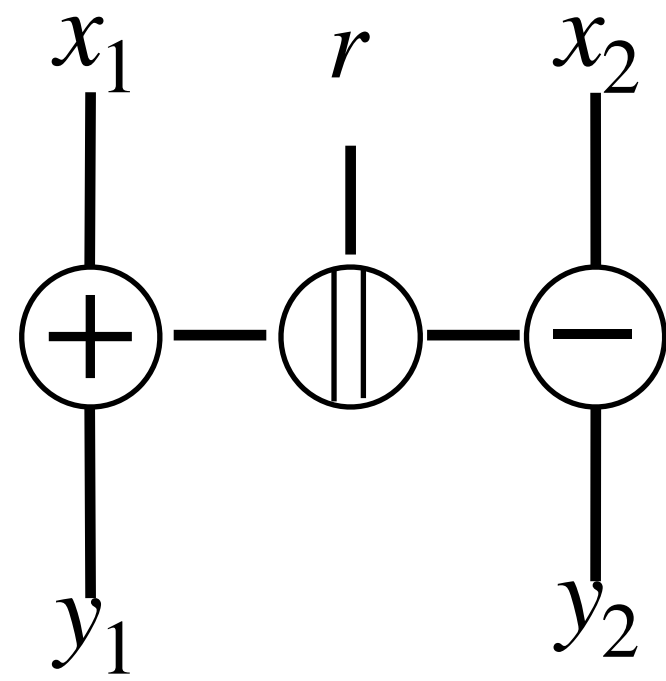
$$r \leftarrow \$$$

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Probe Distribution Table (Crypto 2021)

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Only 5 internal wires for  
3 internal variables:

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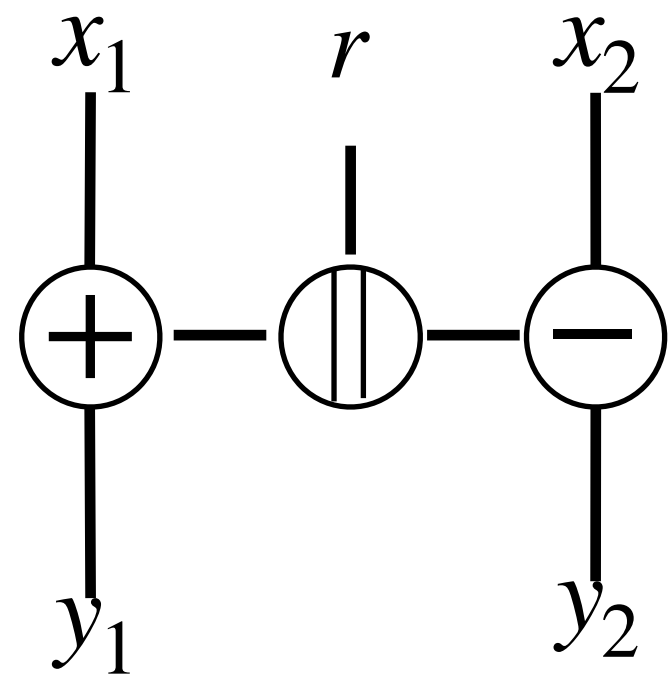
$r$  (proba.  $1 - (1 - p)^3$ )

And 2 output wires:

$y_1$

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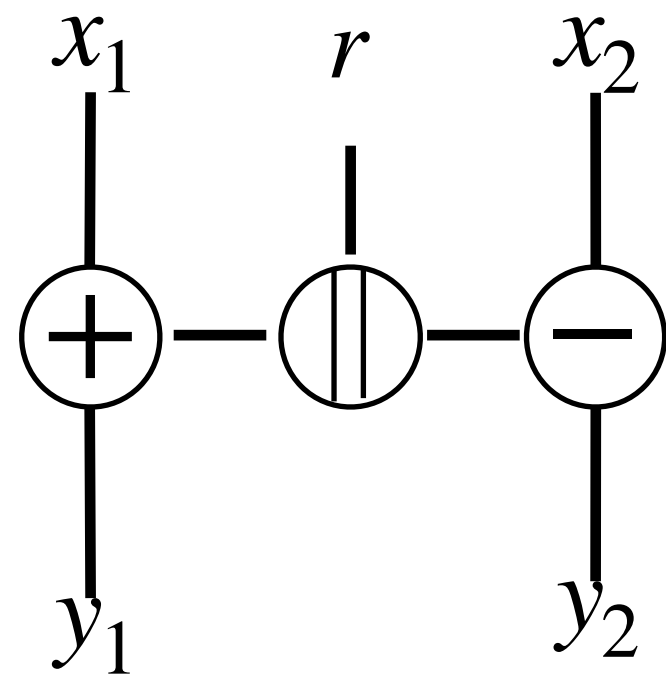
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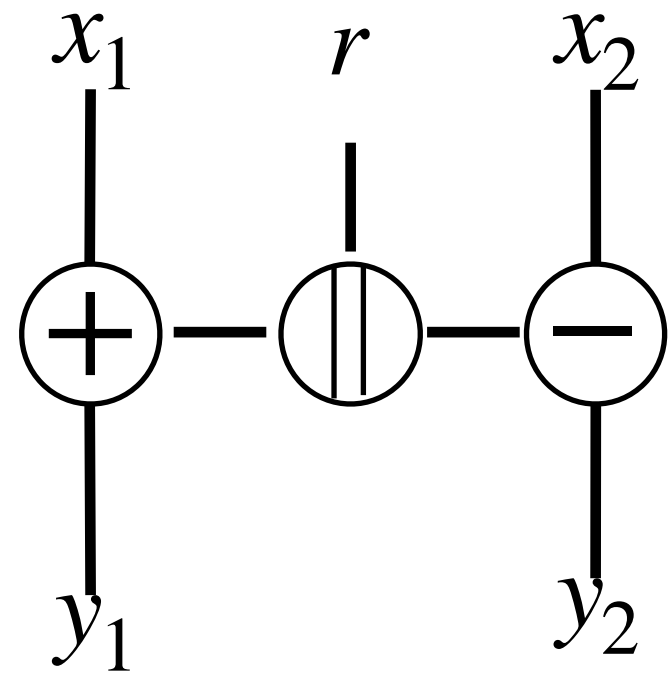
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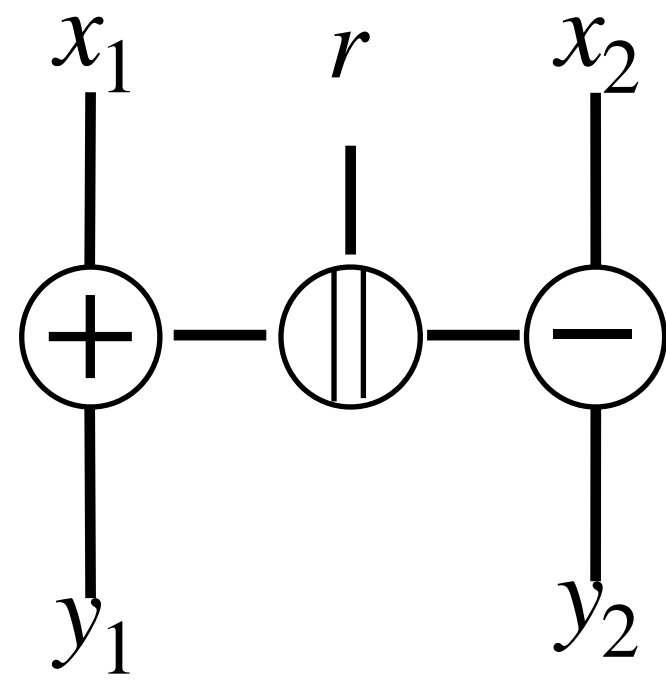
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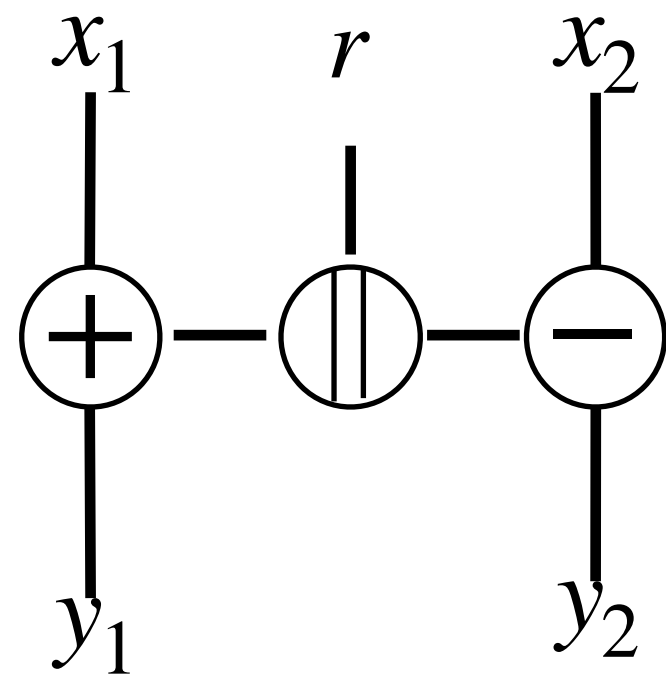
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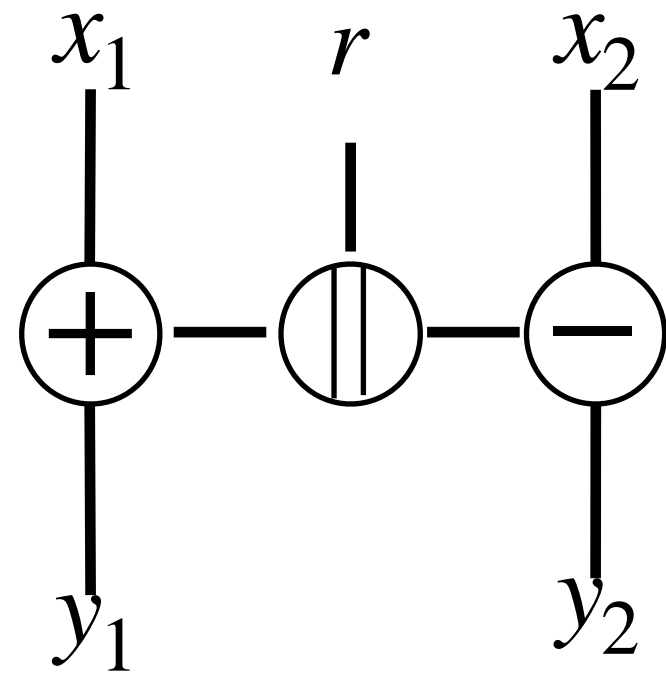
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$$\mathcal{W} = \{r\} \text{ with proba } (1 - (1 - p)^3)(1 - p)^2$$

$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

# How to concretely compute the $\epsilon$ ?



Only 5 internal wires for  
3 internal variables:

$x_1$  (proba.  $p$ )

$x_2$  (proba.  $p$ )

$r$  (proba.  $1 - (1 - p)^3$ )

And 2 output wires:

$y_1$

$y_2$

## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

$$r \leftarrow \$$$

$$y_1 \leftarrow x_1 + r$$

$$y_2 \leftarrow x_2 - r$$

Probe Distribution Table (Crypto 2021)

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

$$\mathcal{W} = \{x_1\} \text{ with proba } p(1 - p)^4$$

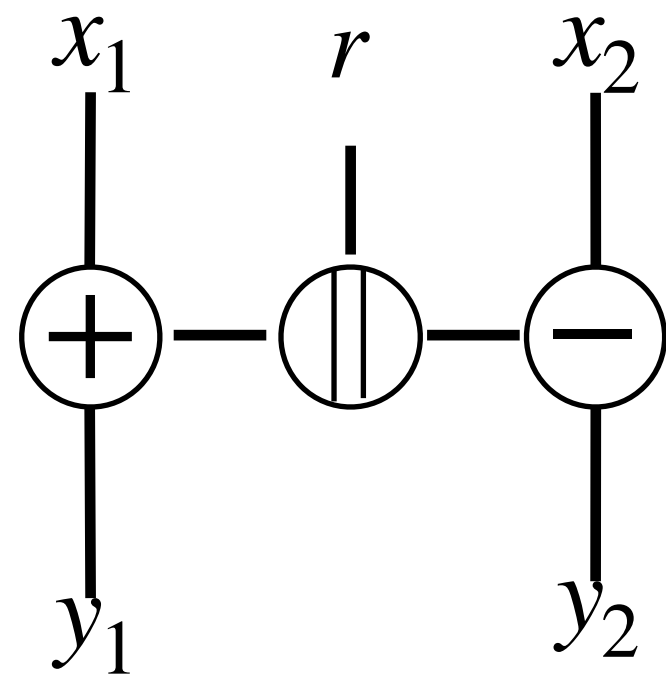
$$\mathcal{W} = \{x_2\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{r\} \text{ with proba } (1 - (1 - p)^3)(1 - p)^2$$

$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

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# How to concretely compute the $\epsilon$ ?



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$$y_1 + y_2 = x_1 + x_2$$

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Probe Distribution Table (Crypto 2021)

Only 5 internal wires for  
3 internal variables:

$x_1$  (proba.  $p$ )

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$r$  (proba.  $1 - (1 - p)^3$ )

And 2 output wires:

$y_1$

$y_2$

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

$$\mathcal{W} = \{x_1\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{x_2\} \text{ with proba } p(1 - p)^4$$

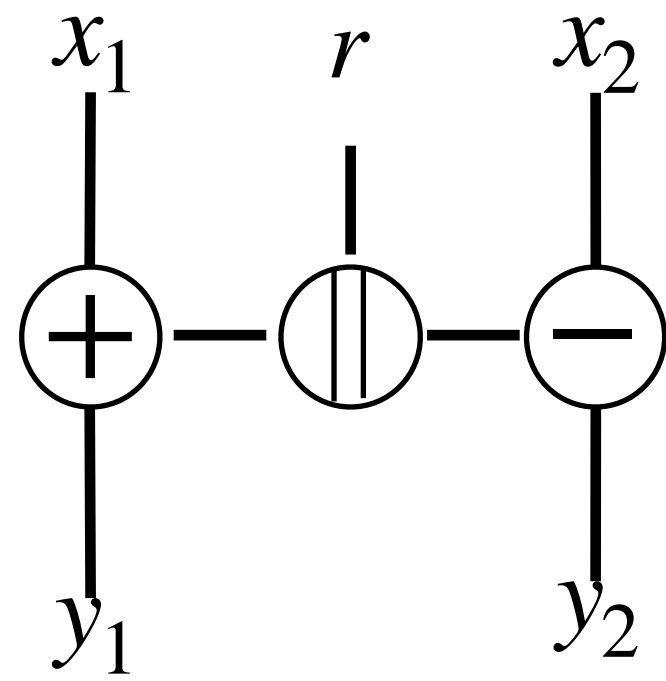
$$\mathcal{W} = \{r\} \text{ with proba } (1 - (1 - p)^3)(1 - p)^2$$

$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

$$\mathcal{W} = \{x_2, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

$$\mathcal{W} = \{x_1, x_2\} \text{ with proba } p^2(1 - p)^3$$

# How to concretely compute the $\epsilon$ ?



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$$y_1 + y_2 = x_1 + x_2$$

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Probe Distribution Table (Crypto 2021)

Only 5 internal wires for  
3 internal variables:

$x_1$  (proba.  $p$ )

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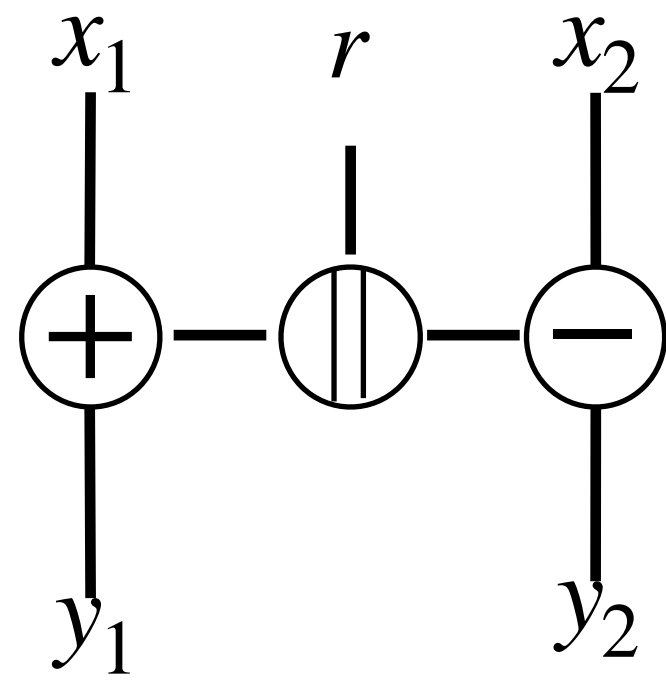
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# How to concretely compute the $\epsilon$ ?



Only 5 internal wires for  
3 internal variables:

$x_1$  (proba.  $p$ )

$x_2$  (proba.  $p$ )

$r$  (proba.  $1 - (1 - p)^3$ )

And 2 output wires:

$y_1$

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$$y_1 + y_2 = x_1 + x_2$$

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$$y_1 \leftarrow x_1 + r$$

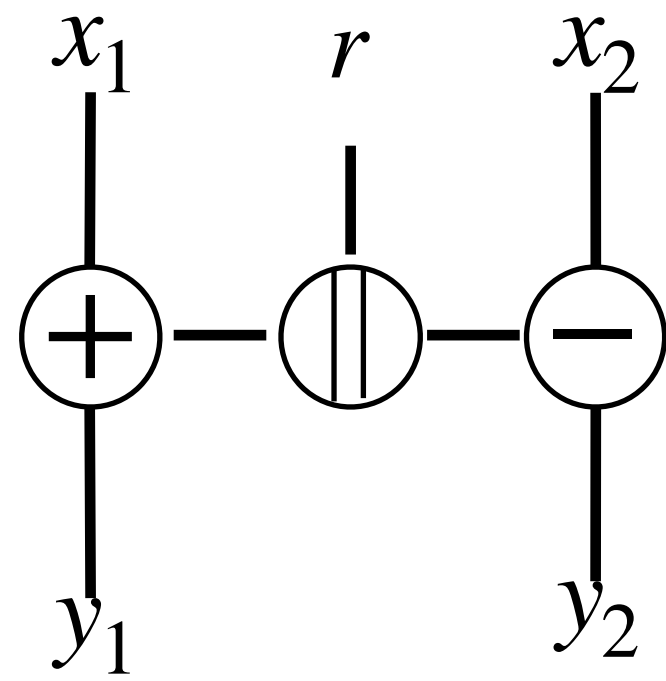
$$y_2 \leftarrow x_2 - r$$

## Probe Distribution Table (Crypto 2021)

|              |             |
|--------------|-------------|
|              | $\emptyset$ |
| $\emptyset$  | $(1 - p)^2$ |
| $x_1$        | $p(1 - p)$  |
| $x_2$        | $p(1 - p)$  |
| $(x_1, x_2)$ | $p^2$       |

- $\mathcal{W} = \emptyset$  with proba  $(1 - p)^5$
- $\mathcal{W} = \{x_1\}$  with proba  $p(1 - p)^4$
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- $\mathcal{W} = \{x_1, r\}$  with proba  $p(1 - p)(1 - (1 - p)^3)$
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- $\mathcal{W} = \{x_1, x_2\}$  with proba  $p^2(1 - p)^3$
- $\mathcal{W} = \{x_1, x_2, r\}$  with proba  $p^2(1 - (1 - p)^3)$

# How to concretely compute the $\epsilon$ ?



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## Probe Distribution Table (Crypto 2021)

|              |             |
|--------------|-------------|
|              | $\emptyset$ |
| $\emptyset$  | $(1 - p)^2$ |
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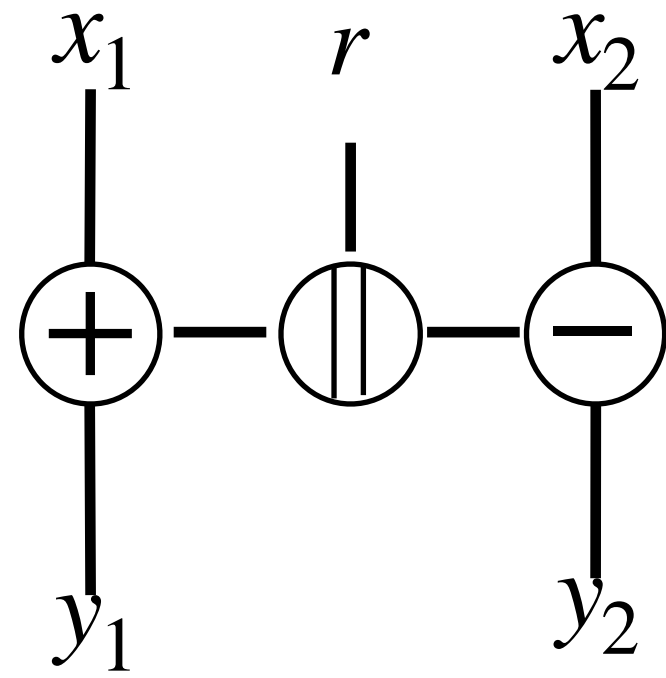
$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

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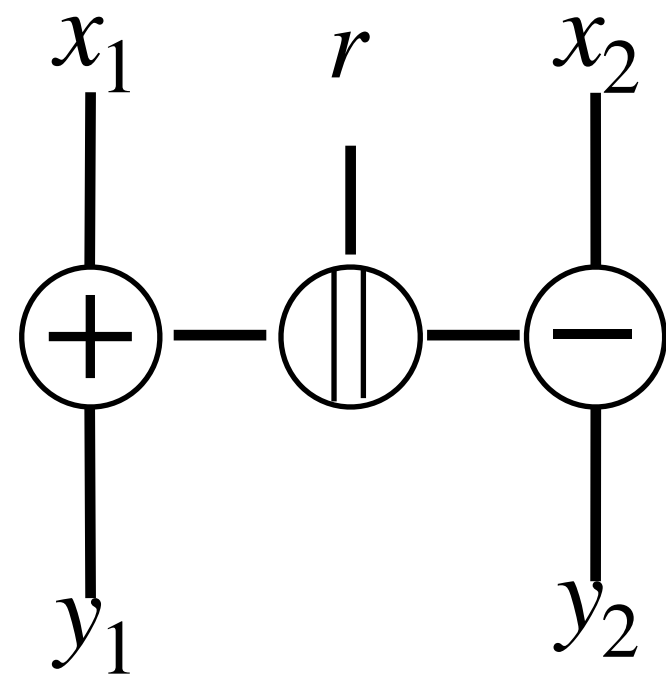
$$\mathcal{W} = \{x_1, x_2\} \text{ with proba } p^2(1 - p)^3$$

$$\mathcal{W} = \{x_1, x_2, r\} \text{ with proba } p^2(1 - (1 - p)^3)$$

## Probe Distribution Table (Crypto 2021)

|              |             |
|--------------|-------------|
|              | $\emptyset$ |
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## Probe Distribution Table (Crypto 2021)

|              |             |
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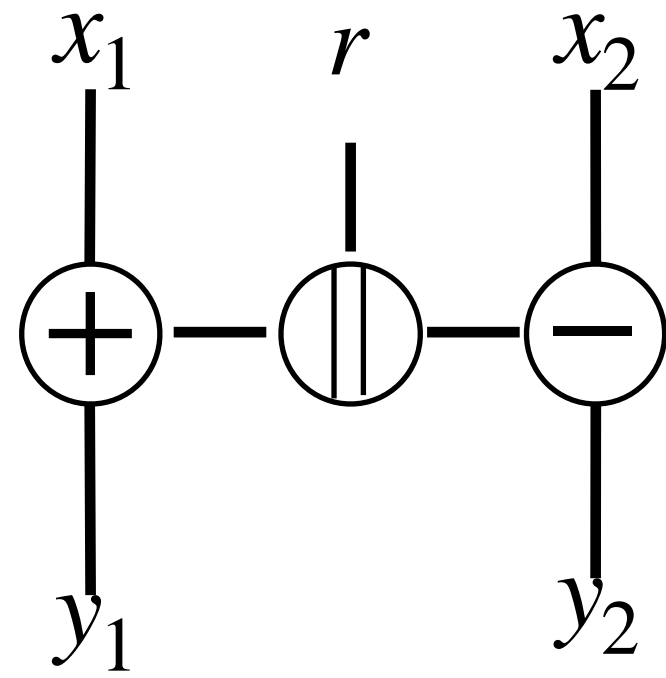
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$$y_1 \leftarrow x_1 + r$$

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## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
|--------------|-------------|---------------------------------------------------------|---------------------------------------------------------|--------------|
| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                             | $(1 - p)^5$                                             | 0            |
| $x_1$        | $p(1 - p)$  | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | $p(1 - p)^4$                                            | 0            |
| $x_2$        | $p(1 - p)$  | $p(1 - p)^4$                                            | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

$$\mathcal{W} = \{x_1\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{x_2\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{r\} \text{ with proba } (1 - (1 - p)^3)(1 - p)^2$$

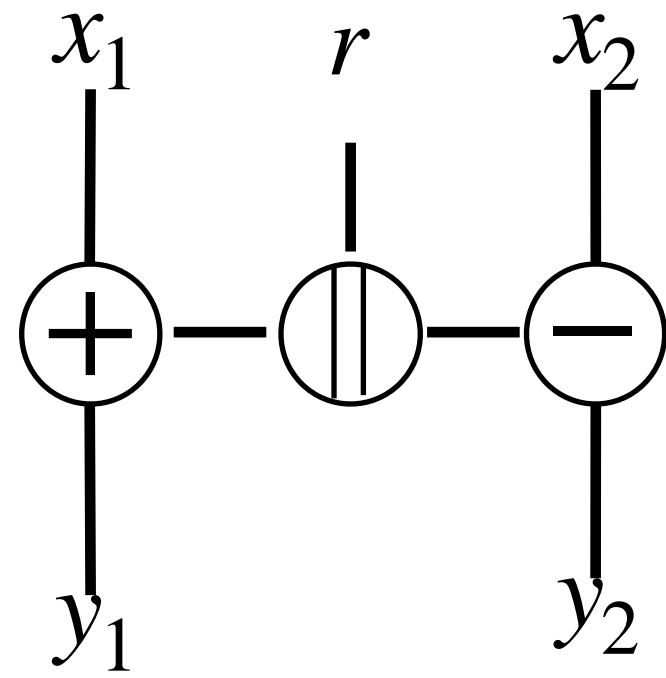
$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

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## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
|--------------|-------------|---------------------------------------------------------|---------------------------------------------------------|--------------|
| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                             | $(1 - p)^5$                                             | 0            |
| $x_1$        | $p(1 - p)$  | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | $p(1 - p)^4$                                            | 0            |
| $x_2$        | $p(1 - p)$  | $p(1 - p)^4$                                            | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

$$\mathcal{W} = \{x_1\} \text{ with proba } p(1 - p)^4$$

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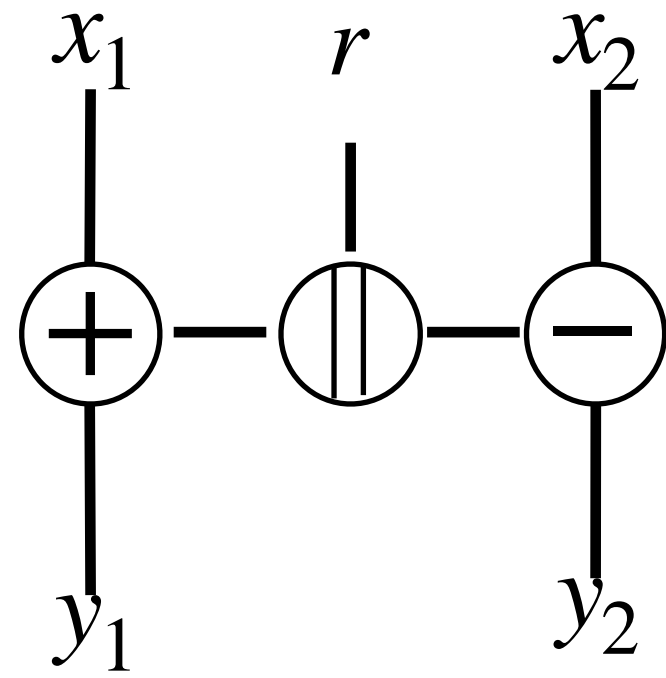
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# How to concretely compute the $\epsilon$ ?



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## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
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| $x_2$        | $p(1 - p)$  | $p(1 - p)^4$                                            | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

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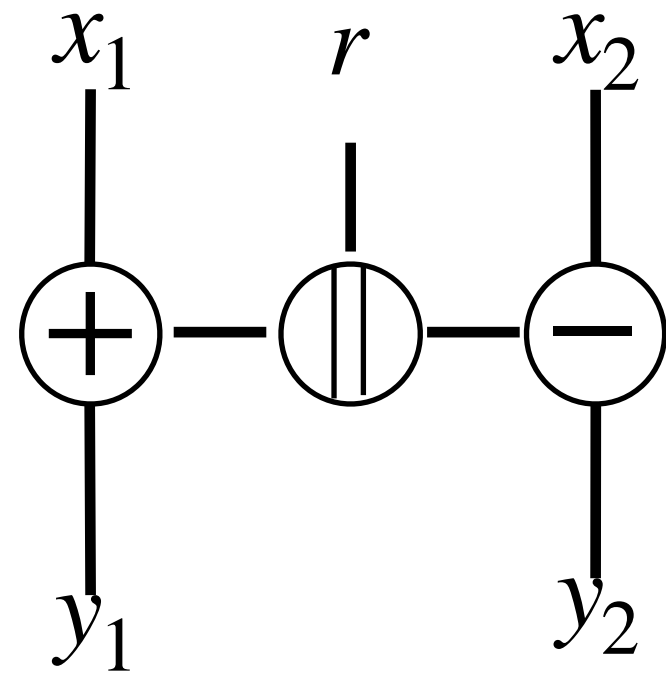
$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

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# How to concretely compute the $\epsilon$ ?



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|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
|--------------|-------------|---------------------------------------------------------|---------------------------------------------------------|--------------|
| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                             | $(1 - p)^5$                                             | 0            |
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| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

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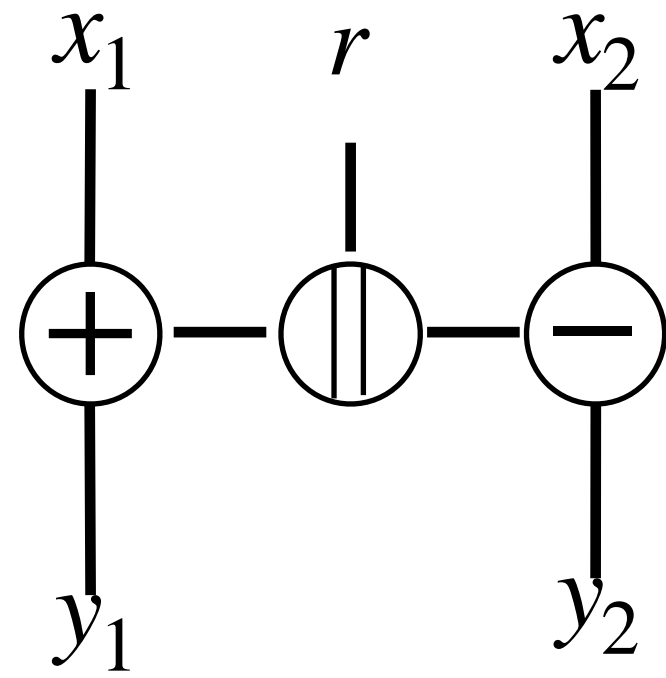
$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

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$$y_1 + y_2 = x_1 + x_2$$

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|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
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| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                             | $(1 - p)^5$                                             | 0            |
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| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

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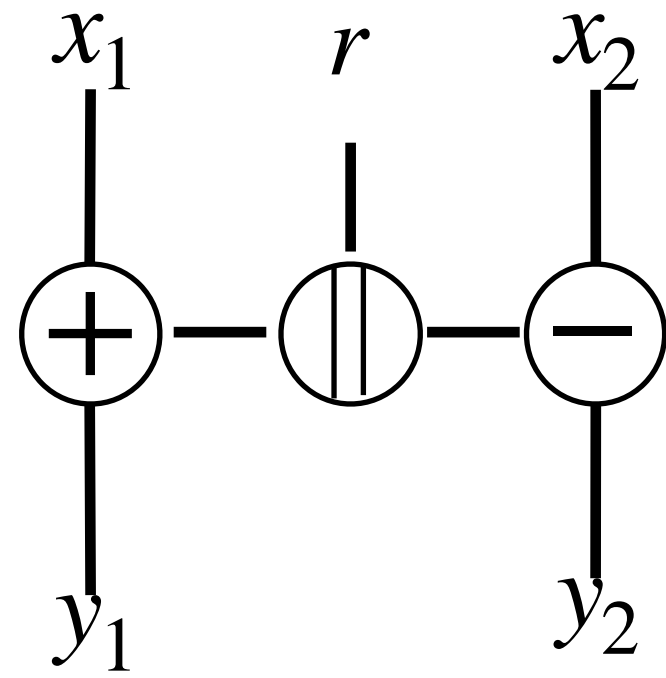
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And 2 output wires:

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## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

$$r \leftarrow \$$$

$$y_1 \leftarrow x_1 + r$$

$$y_2 \leftarrow x_2 - r$$

$$\mathcal{W} = \emptyset \text{ with proba } (1 - p)^5$$

$$\mathcal{W} = \{x_1\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{x_2\} \text{ with proba } p(1 - p)^4$$

$$\mathcal{W} = \{r\} \text{ with proba } (1 - (1 - p)^3)(1 - p)^2$$

$$\mathcal{W} = \{x_1, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

$$\mathcal{W} = \{x_2, r\} \text{ with proba } p(1 - p)(1 - (1 - p)^3)$$

$$\mathcal{W} = \{x_1, x_2\} \text{ with proba } p^2(1 - p)^3$$

$$\mathcal{W} = \{x_1, x_2, r\} \text{ with proba } p^2(1 - (1 - p)^3)$$

## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                                                   | $y_2$                                                   | $(y_1, y_2)$ |
|--------------|-------------|---------------------------------------------------------|---------------------------------------------------------|--------------|
| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                             | $(1 - p)^5$                                             | 0            |
| $x_1$        | $p(1 - p)$  | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | $p(1 - p)^4$                                            | 0            |
| $x_2$        | $p(1 - p)$  | $p(1 - p)^4$                                            | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{(1 - (1 - p)^4)}$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                        | $p - p(1 - p)^4$                                        | 1            |

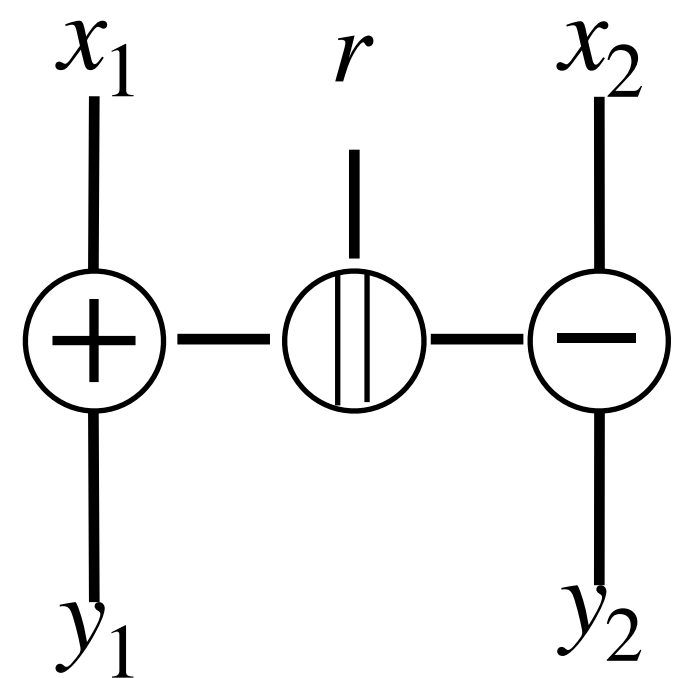
Cases that cannot be simulated (we need all the shares of  $x$ )

$(p, \epsilon, t)$ -random-probing composability

$$\rightarrow \begin{aligned} t &= 1 \\ \epsilon &= p - p(1 - p)^4 \end{aligned}$$

This technique does not scale well  
specially for large gadgets with many shares (PQC)

# Using cardinal tables



## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

$$r \leftarrow \$$$

$$y_1 \leftarrow x_1 + r$$

$$y_2 \leftarrow x_2 - r$$

## Cardinal Distribution Table

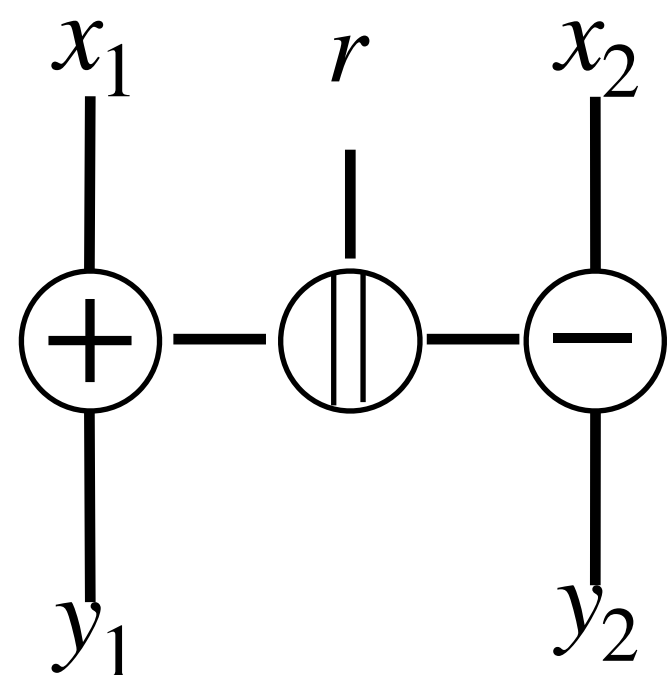
| $t_{\text{in}}$ $t_{\text{out}}$ | 0           | 1                                | 2 |
|----------------------------------|-------------|----------------------------------|---|
| 0                                | $(1 - p)^2$ | $(1 - p)^5$                      | 0 |
| 1                                | $2p(1 - p)$ | $2(1 - p) \cdot (1 - (1 - p)^4)$ | 0 |
| 2                                | $p^2$       | $p - p(1 - p)^4$                 | 1 |

## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                                                 | $y_2$                                                 | $(y_1, y_2)$ |
|--------------|-------------|-------------------------------------------------------|-------------------------------------------------------|--------------|
| $\emptyset$  | $(1 - p)^2$ | $(1 - p)^5$                                           | $(1 - p)^5$                                           | 0            |
| $x_1$        | $p(1 - p)$  | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{1 - (1 - p)^4}$ | $p(1 - p)^4$                                          | 0            |
| $x_2$        | $p(1 - p)$  | $p(1 - p)^4$                                          | $\frac{(1 - p) \cdot (1 - (1 - p)^4)}{1 - (1 - p)^4}$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1 - p)^4$                                      | $p - p(1 - p)^4$                                      | 1            |

[BRR25] S. Belaïd, M. Rivain and M. Rossi, *New Techniques for Random Probing Security and Application to Raccoon Signature Scheme* published in Eurocrypt 2025

# Using cardinal tables



## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

$$r \leftarrow \$$$

$$y_1 \leftarrow x_1 + r$$

$$y_2 \leftarrow x_2 - r$$

Cardinal Distribution Table

| $t_{\text{in}}$ $t_{\text{out}}$ | 0         | 1                          | 2 |
|----------------------------------|-----------|----------------------------|---|
| 0                                | $(1-p)^2$ | $(1-p)^5$                  | 0 |
| 1                                | $2p(1-p)$ | $2(1-p) \cdot (1-(1-p)^4)$ | 0 |
| 2                                | $p^2$     | $p - p(1-p)^4$             | 1 |

Probe Distribution Table (Crypto 2021)

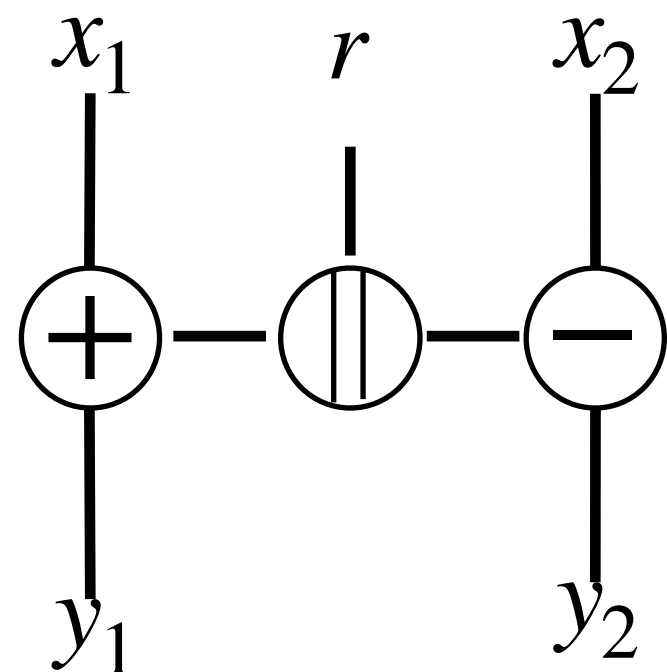
|              | $\emptyset$ | $y_1$                     | $y_2$                     | $(y_1, y_2)$ |
|--------------|-------------|---------------------------|---------------------------|--------------|
| $\emptyset$  | $(1-p)^2$   | $(1-p)^5$                 | $(1-p)^5$                 | 0            |
| $x_1$        | $p(1-p)$    | $(1-p) \cdot (1-(1-p)^4)$ | $p(1-p)^4$                | 0            |
| $x_2$        | $p(1-p)$    | $p(1-p)^4$                | $(1-p) \cdot (1-(1-p)^4)$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1-p)^4$            | $p - p(1-p)^4$            | 1            |

Sum

Max

[BRR25] S. Belaïd, M. Rivain and M. Rossi, *New Techniques for Random Probing Security and Application to Raccoon Signature Scheme* published in Eurocrypt 2025

# Using cardinal tables



## SimpleRefresh

$$y_1 + y_2 = x_1 + x_2$$

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$$y_1 \leftarrow x_1 + r$$

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## Cardinal Distribution Table

| $t_{\text{in}}$ $t_{\text{out}}$ | 0         | 1                          | 2 |
|----------------------------------|-----------|----------------------------|---|
| 0                                | $(1-p)^2$ | $(1-p)^5$                  | 0 |
| 1                                | $2p(1-p)$ | $2(1-p) \cdot (1-(1-p)^4)$ | 0 |
| 2                                | $p^2$     | $p - p(1-p)^4$             | 1 |

## Probe Distribution Table (Crypto 2021)

|              | $\emptyset$ | $y_1$                     | $y_2$                     | $(y_1, y_2)$ |
|--------------|-------------|---------------------------|---------------------------|--------------|
| $\emptyset$  | $(1-p)^2$   | $(1-p)^5$                 | $(1-p)^5$                 | 0            |
| $x_1$        | $p(1-p)$    | $(1-p) \cdot (1-(1-p)^4)$ | $p(1-p)^4$                | 0            |
| $x_2$        | $p(1-p)$    | $p(1-p)^4$                | $(1-p) \cdot (1-(1-p)^4)$ | 0            |
| $(x_1, x_2)$ | $p^2$       | $p - p(1-p)^4$            | $p - p(1-p)^4$            | 1            |

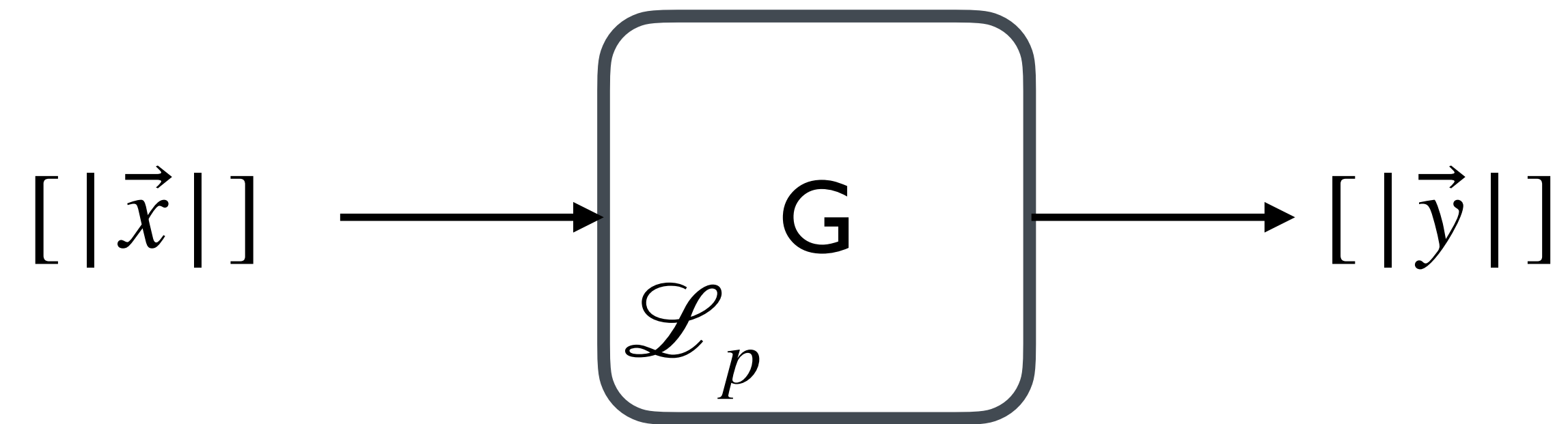
Sum

Max

Probability envelopes:  $\mathcal{E}_{t_{\text{out}}}(t_{\text{in}})$

[BRR25] S. Belaïd, M. Rivain and M. Rossi, *New Techniques for Random Probing Security and Application to Raccoon Signature Scheme* published in Eurocrypt 2025

# Extensions of the Random Probing Security

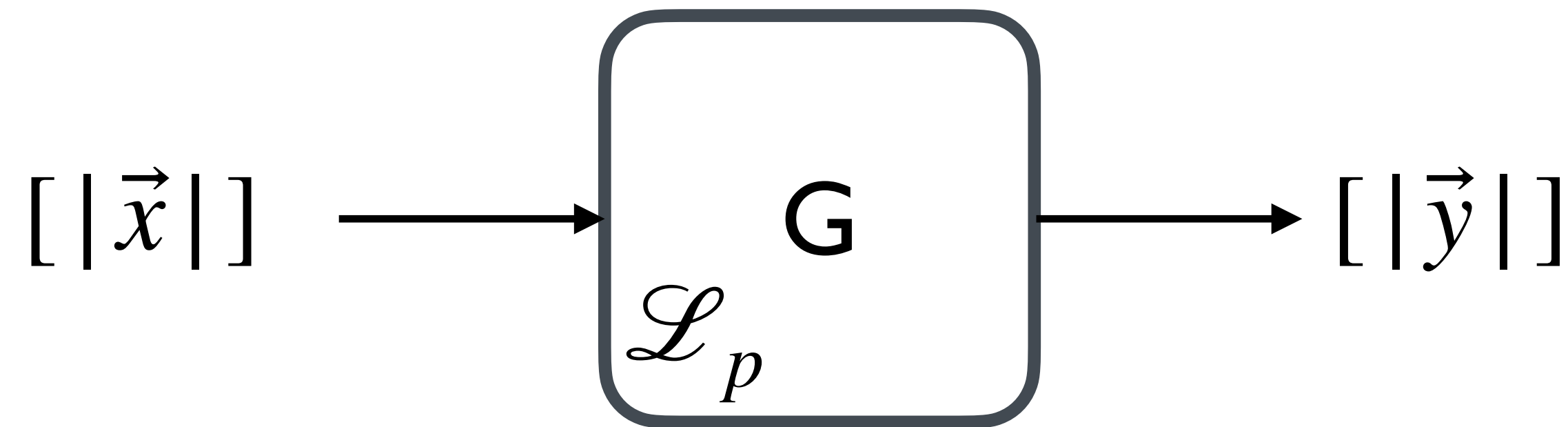


$(p, t, \varepsilon)$ -RPC

$\mathbb{P}(\text{« more than } t \text{ shares of each } [|\vec{x}^i|] \text{ are required to simulate } \mathcal{L}_p \text{ and } t \text{ output shares of each } [|\vec{y}^i|] \text{ »}) \leq \varepsilon$

# Extensions of the Random Probing Security

## Cardinal Random Probing Composability (cardinal-RPC)



$(p, \vec{\mathcal{E}})$ -cardinal RPC

$\mathbb{P}(\text{« exactly } t_i^{in} \text{ shares of each } [|\vec{x}^i|] \text{ are required to simulate } \mathcal{L}_p \text{ and } t_j^{out} \text{ output shares of each } [|\vec{y}^j|] \text{ »}) \leq \mathcal{E}_{\vec{t}^{out}}(\vec{t}^{in})$

$$\forall (t_1^{in}, \dots, t_\ell^{in}) \in [0, n]^\ell, \forall (t_1^{out}, \dots, t_m^{out}) \in [0, n]^m,$$

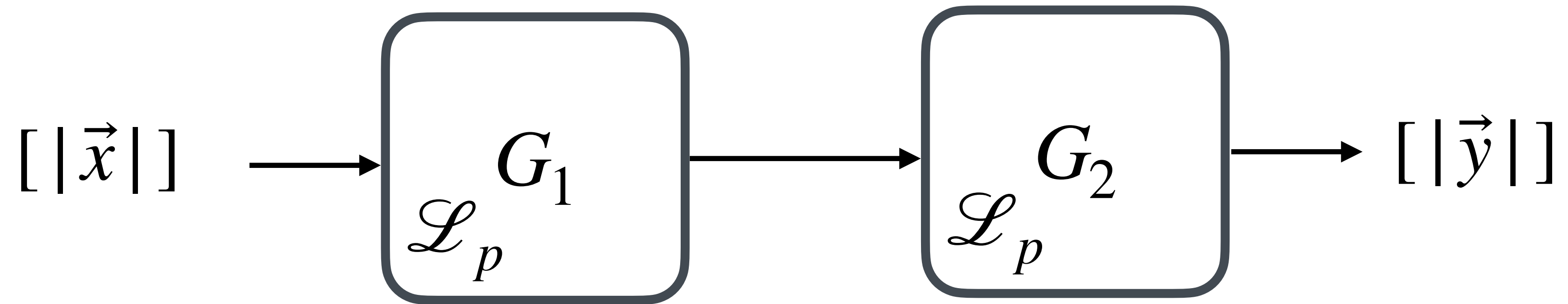
# Extensions of the Random Probing Security

Cardinal Random Probing Composability  
(cardinal-RPC)

Random Probing Security with Auxiliary Inputs and  
public Outputs  
(RPS-AI-O)

# Extensions of the Random Probing Security

## Cardinal Random Probing Composability (cardinal-RPC)



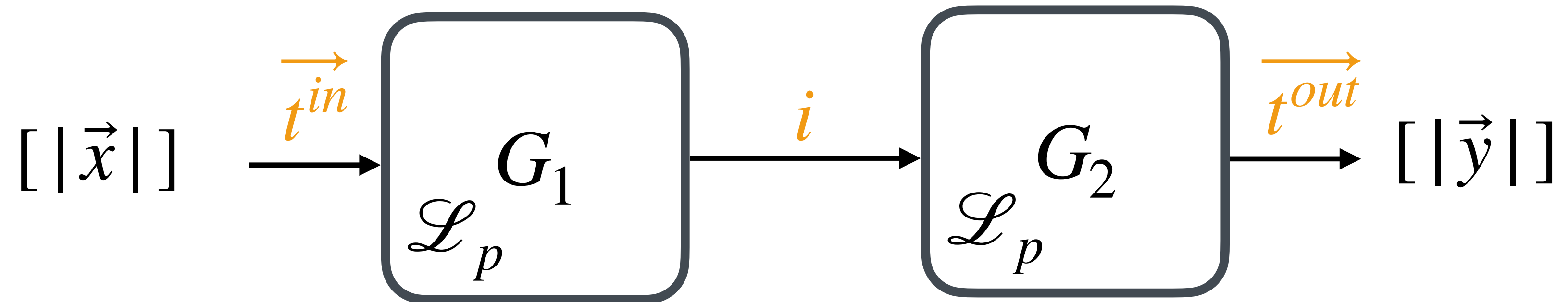
$(p, t, \varepsilon)$ -RPC

$(p, t, \varepsilon_3)$ -RPC advantage of the composition:

$$\varepsilon_3 \leq 1 - (1 - \varepsilon_1)(1 - \varepsilon_2)$$

# Extensions of the Random Probing Security

## Cardinal Random Probing Composability (cardinal-RPC)



$(p, \vec{\mathcal{E}})$ -cardinal RPC

$(p, \vec{\mathcal{E}}^3)$ -cardinal RPC advantage of the composition:

$$\mathcal{E}_{\vec{t}^{out}}^3(\vec{t}^{in}) = \sum_{i=0}^n \mathcal{E}_i^1(\vec{t}^{in}) \cdot \mathcal{E}_{\vec{t}^{out}}^2(i)$$

# Current state of the art

- ☑ Existing elementary gadgets proved (Cardinal or threshold)-RPC
  - ➔ Addition
  - ➔ Multiplication
  - ➔ Copy
  - ➔ Refresh
- ☑ Composition achievable by combining the enveloppes.
- ☑ Other composition techniques

[BFO23] Berti, F., Faust, S., Orlt, M. *Provable secure parallel gadgets*. TCHES 2023

[JMB24] V. Jahandideh, B. Mennink and L. Batina  
*An Algebraic Approach for Evaluating Random Probing Security With Application to AES*. TCHES 2024

# Current state of the art

Exciting work still lies ahead !

- ☒ Existing elementary gadgets proved (Cardinal or threshold)-RPC
  - ➔ Addition
  - ➔ Multiplication
  - ➔ Copy
  - ➔ Refresh
- ☒ Composition achievable by combining the enveloppes.
- ☒ Other composition techniques

- ☐ More advanced gadgets
  - ➔ Mask conversions, comparisons
  - ➔ Sampling with specific distributions
- ☐ Optimized composition for tighter bounds
- ☐ Formal verification
- ☐ Efficient protected implementations

[BFO23] Berti, F., Faust, S., Orlt, M. *Provable secure parallel gadgets*. TCHES 2023

[JMB24] V. Jahandideh, B. Mennink and L. Batina  
*An Algebraic Approach for Evaluating Random Probing Security With Application to AES*. TCHES 2024

1) The relevance of the random probing model

2) The challenges: scaling up

3) Random-probing Raccoon

4) Ideas for future works

1) The relevance of the random probing model

2) The challenges: scaling up

3) Random-probing Raccoon

4) Ideas for future works

# Raccoon Signature Scheme

## KeyGen

1. Generate a large matrix  $\mathbf{A} \in \mathcal{R}_q^{k \times \ell}$
2.  $[[s]] = (0, \dots, 0)$
3. Add noise to  $[[s]]$
4. Compute  $[[t]] = \mathbf{A} \cdot [[s]]$
5. Add noise to  $[[t]]$
6. Decode  $[[t]]$  to  $t$
7. The verification key is  $(\mathbf{A}, t)$
8. The signing key is  $[[s]]$

## Signature

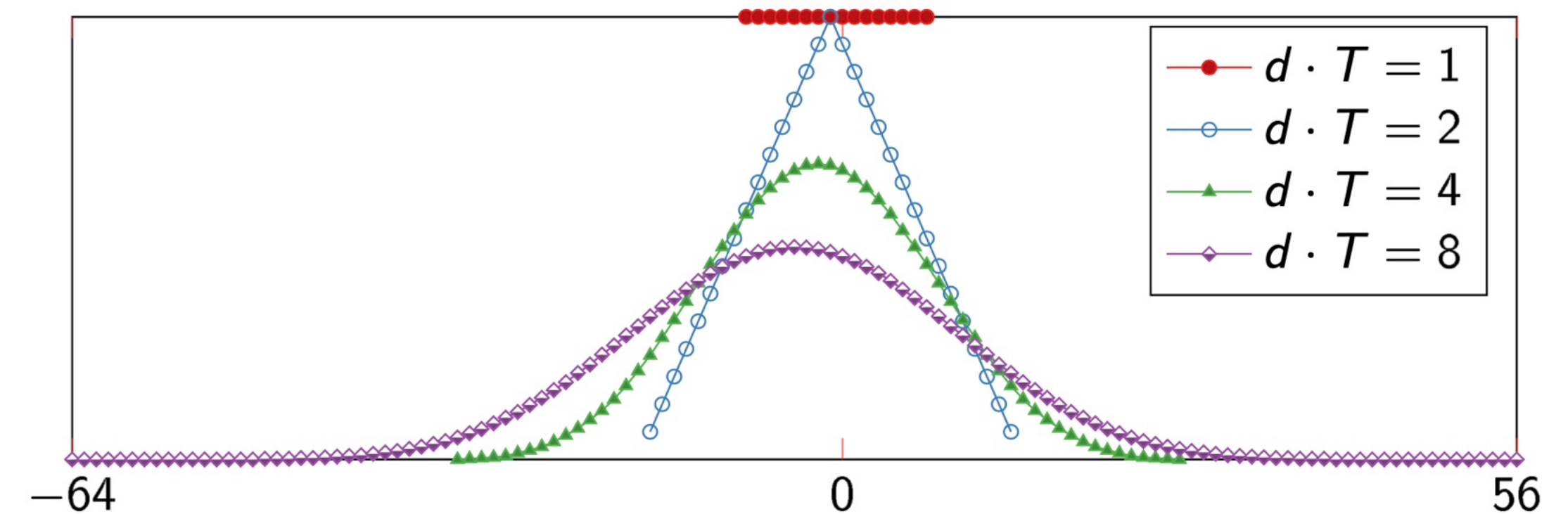
1.  $[[r]] = \text{Refresh}(0, \dots, 0)$
2. Add noise to  $[[r]]$
3. Compute the commitment  $[[w]] = \mathbf{A} \cdot [[r]]$
4. Add noise to  $[[w]]$
5. Decode  $[[w]]$  to  $w$
6. Compute the challenge  $c = H(w, \text{msg}, \text{vk})$
7. Compute the response  $[[z]] = [[s]] \cdot c + [[r]]$
8. Decode  $[[z]]$  to  $z$
9. The signature is  $\text{sig} = (c, z)$

No Rejection Sampling

## « Add noise to »

For  $i \in [0, T]$ :

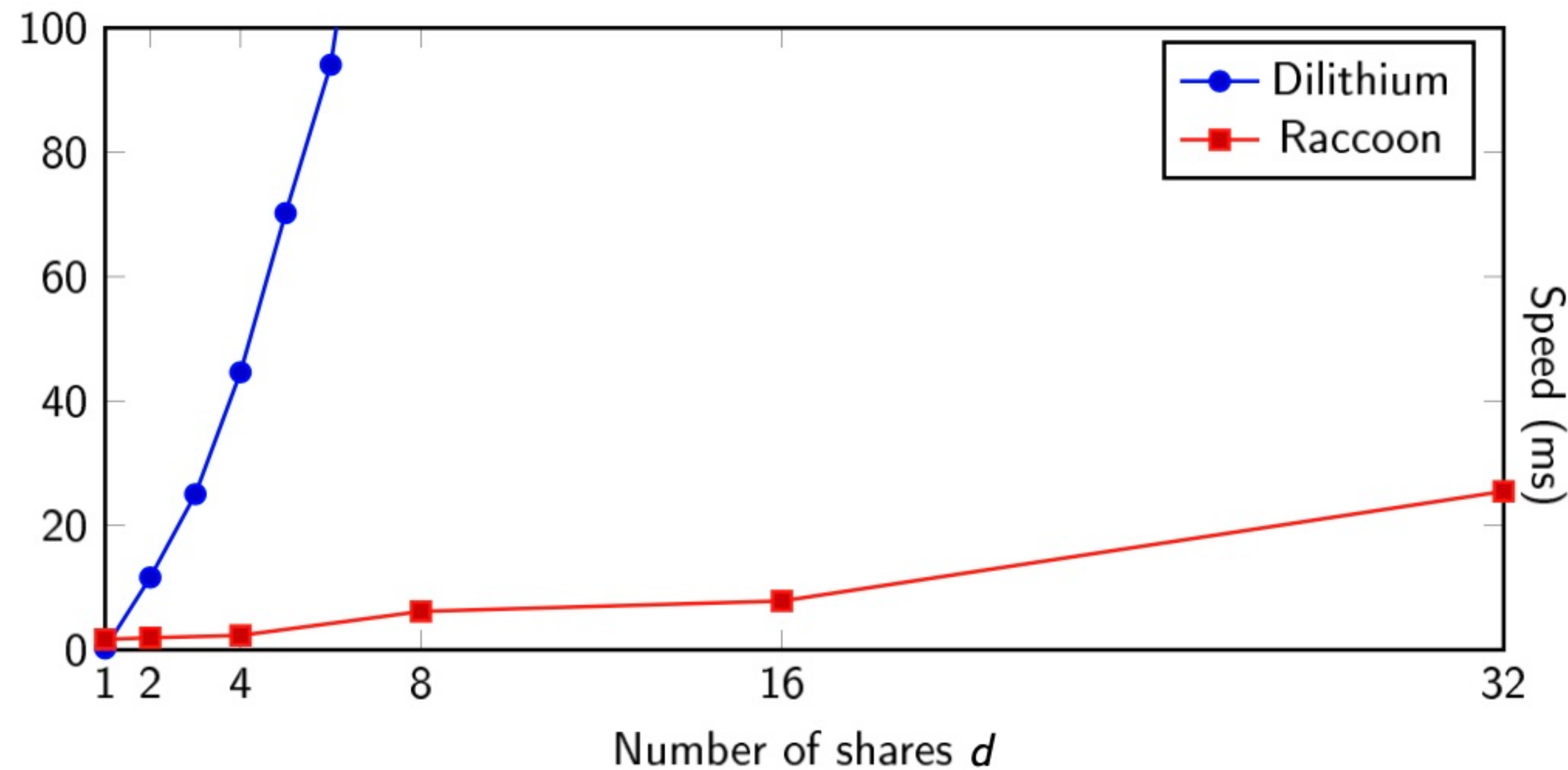
1. Sample  $d$  small uniforms randoms  
 $[[r]] = (r_0, \dots, r_{d-1})$
2.  $[[x]] = [[x]] + [[r]]$
3. Refresh  $[[x]]$



Distribution of the random that is added

[dPKPR24] R. del Pino, S. Katsumata, T. Prest and M. Rossi  
*Raccoon: A Masking-Friendly Signature Proven in the Probing Model.* CRYPTO 2024

# Objective of Raccoon



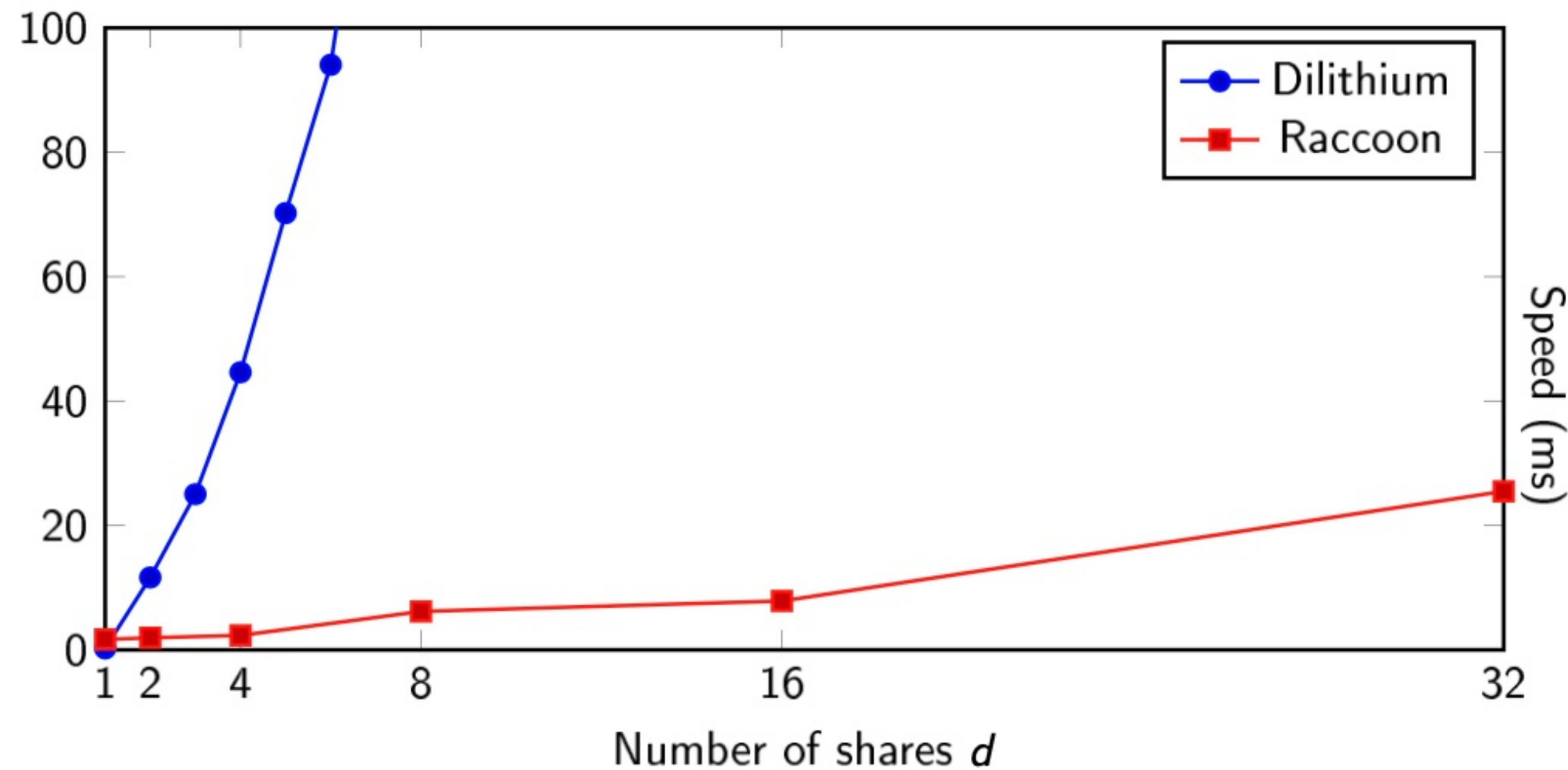
## Raccoon 128-16

|   |                 |
|---|-----------------|
| q | 549824583172097 |
| n | 512             |
| k | 5               |
| l | 4               |
| d | 16              |
| T | 2               |

- ➡ Quasi-linear in the masking order
- ➡ Proof in the  $(d - 1)$ -probing model
- ➡ Same assumptions as Dilithium/ML-DSA
- ➡ Simpler
- ➡ Same key size for the verification key
- ➡ When masked, orders of magnitude faster

Signatures 4 × larger

# Objective of Raccoon



## Raccoon 128-16

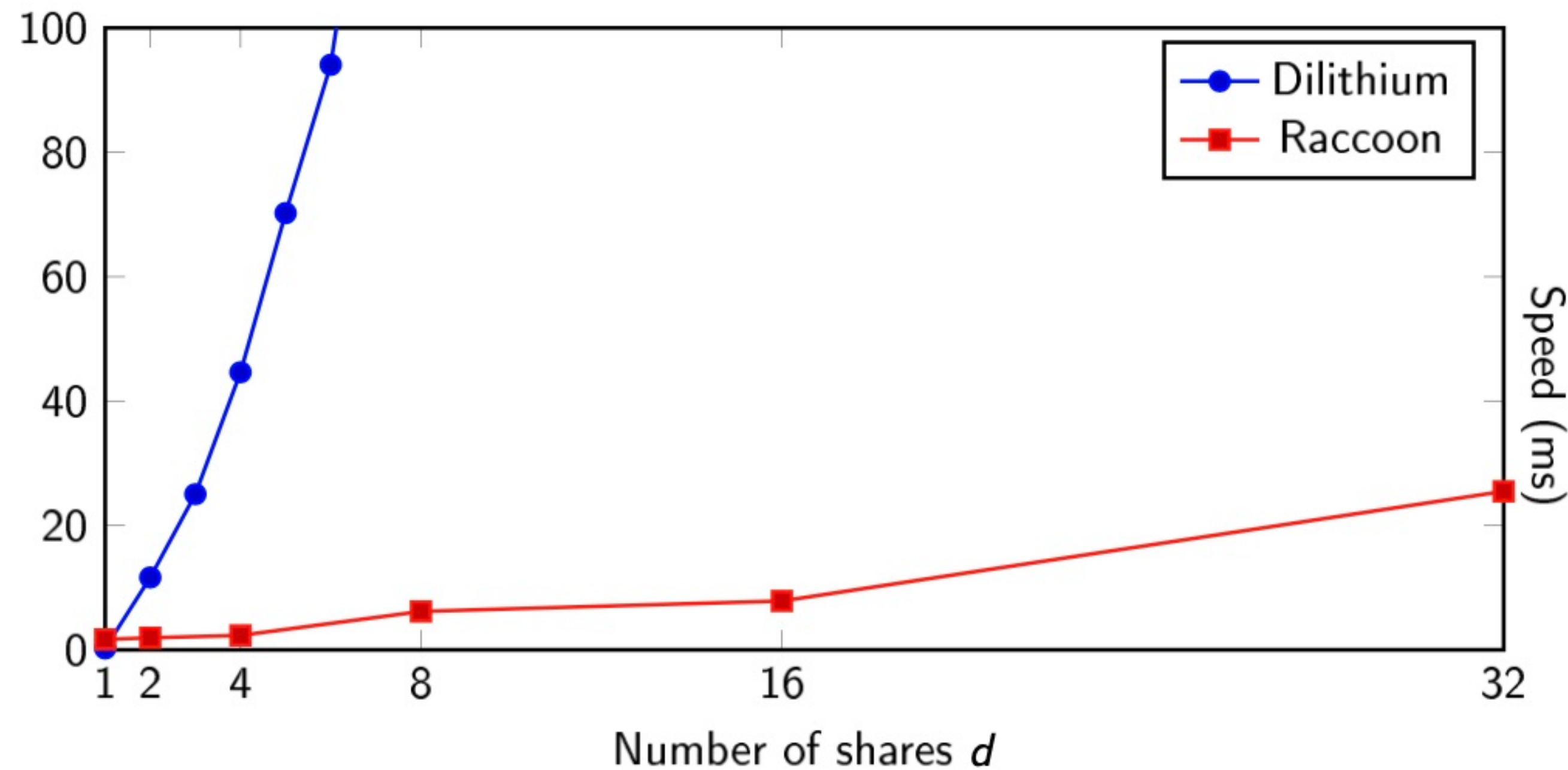
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Signatures 4 × larger

Not selected for NIST additional post-quantum signatures

# Objective of Raccoon



## Raccoon 128-16

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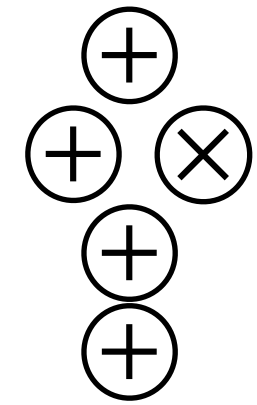
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Signatures 4 × larger

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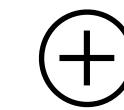
But thresholdizable

## KeyGen



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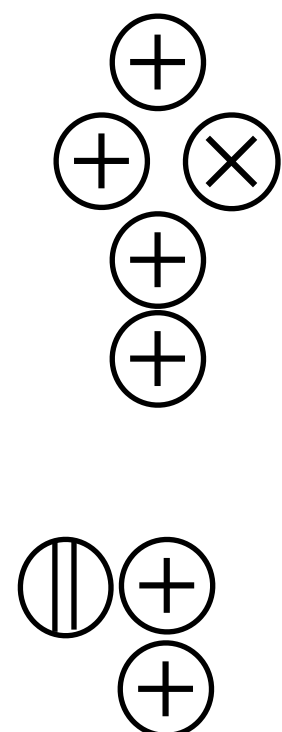
## Functionally



« Add noise to »

Add  $d \cdot T$  small uniform randoms

## Signature



1.  $[[r]] = \text{Refresh}(0, \dots, 0)$
2. Add noise to  $[[r]]$
3. Compute the commitment  $[[w]] = \mathbf{A} \cdot [[r]]$
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8. Decode  $[[z]]$  to  $z$
9. The signature is  $\text{sig} = (c, z)$

No Rejection Sampling



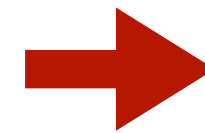
# Design rationale of our new refresh

Composable (cardinal or threshold RPC)  
elementary gates are needed



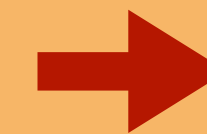
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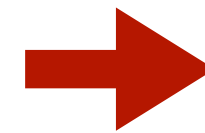
To be composable, they need to include  
some refreshes

Refresh



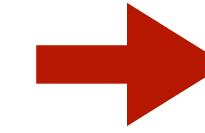
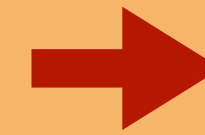
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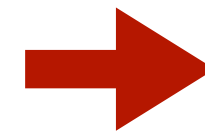
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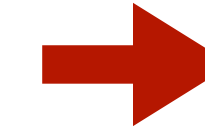
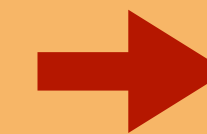
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Refresh



Efficient  
random-probing  
composable  
refresh

➔ Raccoon's refresh is not (yet?) proved RPC (cardinal or threshold).

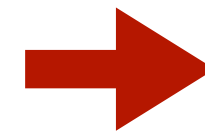
We could not prove the **random probing composability of the quasilinear refresh**.



[BCPZ16] A. Battistello, J.-S. Coron, E. Prouff, and R. Zeitoun. Horizontal side-channel attacks and countermeasures on the ISW masking scheme. CHES 2016

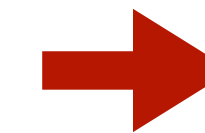
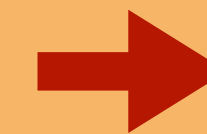
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Refresh



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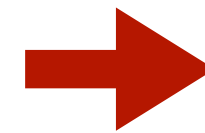
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The probability computation rapidly explodes if there are too many dependencies in the intermediate variables.

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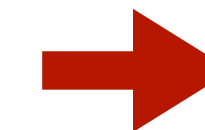
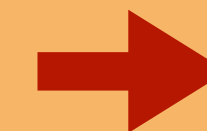
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Refresh



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We could not prove the **random probing composability of the quasilinear refresh**.

The probability computation rapidly explodes if there are too many dependencies in the intermediate variables.

Random-probing-friendly feature

The gadget should contain as much independent random as possible (including the indexes of the shares that are touched)

[BCPZ16] A. Battistello, J.-S. Coron, E. Prouff, and R. Zeitoun. Horizontal side-channel attacks and countermeasures on the ISW masking scheme. CHES 2016

# New Random Probing Composable Refresh

$$[|z|] = (0,0,0,0,0,0,0,0)$$

# New Random Probing Composable Refresh

$$[|z|] = (0,0,0,0,0,0,0,0)$$

1st iteration

$$r_1 \leftarrow \$, (i_1, j_1) \leftarrow \$ \quad [(i_1, j_1) = (3,7)]$$

$$[|z|] = (0,0,r_1,0,0,0,-r_1,0)$$

# New Random Probing Composable Refresh

$$[|z|] = (0,0,0,0,0,0,0,0)$$

1st iteration

$$r_1 \leftarrow \$, (i_1, j_1) \leftarrow \$ \quad [(i_1, j_1) = (3,7)]$$

$$[|z|] = (0,0,r_1,0,0,0, -r_1,0)$$

2nd iteration

$$r_2 \leftarrow \$, (i_2, j_2) \leftarrow \$ \quad [(i_2, j_2) = (1,8)]$$

$$[|z|] = (r_2,0,r_1,0,0,0, -r_1, -r_2)$$

# New Random Probing Composable Refresh

$$[|z|] = (0,0,0,0,0,0,0,0)$$

1st iteration

$$r_1 \leftarrow \$, (i_1, j_1) \leftarrow \$ \quad [(i_1, j_1) = (3,7)]$$

$$[|z|] = (0,0,r_1,0,0,0, -r_1,0)$$

2nd iteration

$$r_2 \leftarrow \$, (i_2, j_2) \leftarrow \$ \quad [(i_2, j_2) = (1,8)]$$

$$[|z|] = (r_2,0,r_1,0,0,0, -r_1, -r_2)$$

3rd iteration

$$r_3 \leftarrow \$, (i_3, j_3) \leftarrow \$ \quad [(i_3, j_3) = (2,3)]$$

$$[|z|] = (r_2, r_3, r_1 - r_3, 0, 0, 0, -r_1, -r_2)$$

# New Random Probing Refresh

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**Algorithm 1**  $\text{RPZeroEnc}^{n,\gamma}$ 

---

**Output:**  $\llbracket z \rrbracket = (z_1, \dots, z_n) \in \mathbb{K}^n$  such that  $z_1 + \dots + z_n = 0$

1.  $\llbracket z \rrbracket = (0, 0, \dots, 0)$   $\{n \text{ zeros}\}$
  2. **for**  $i = 1$  to  $\gamma$  **do**
  3.   Select two distinct indices  $i_1, i_2 \in [1, n]$  uniformly at random
  4.    $r \xleftarrow{\$} \mathbb{K}$
  5.    $z_{i_1} \leftarrow z_{i_1} + r$
  6.    $z_{i_2} \leftarrow z_{i_2} - r$
  7. **end for**
  8. **return**  $\llbracket z \rrbracket$
- 

---

**Algorithm 2**  $\text{RPRefresh}^\gamma(\llbracket a \rrbracket)$ 

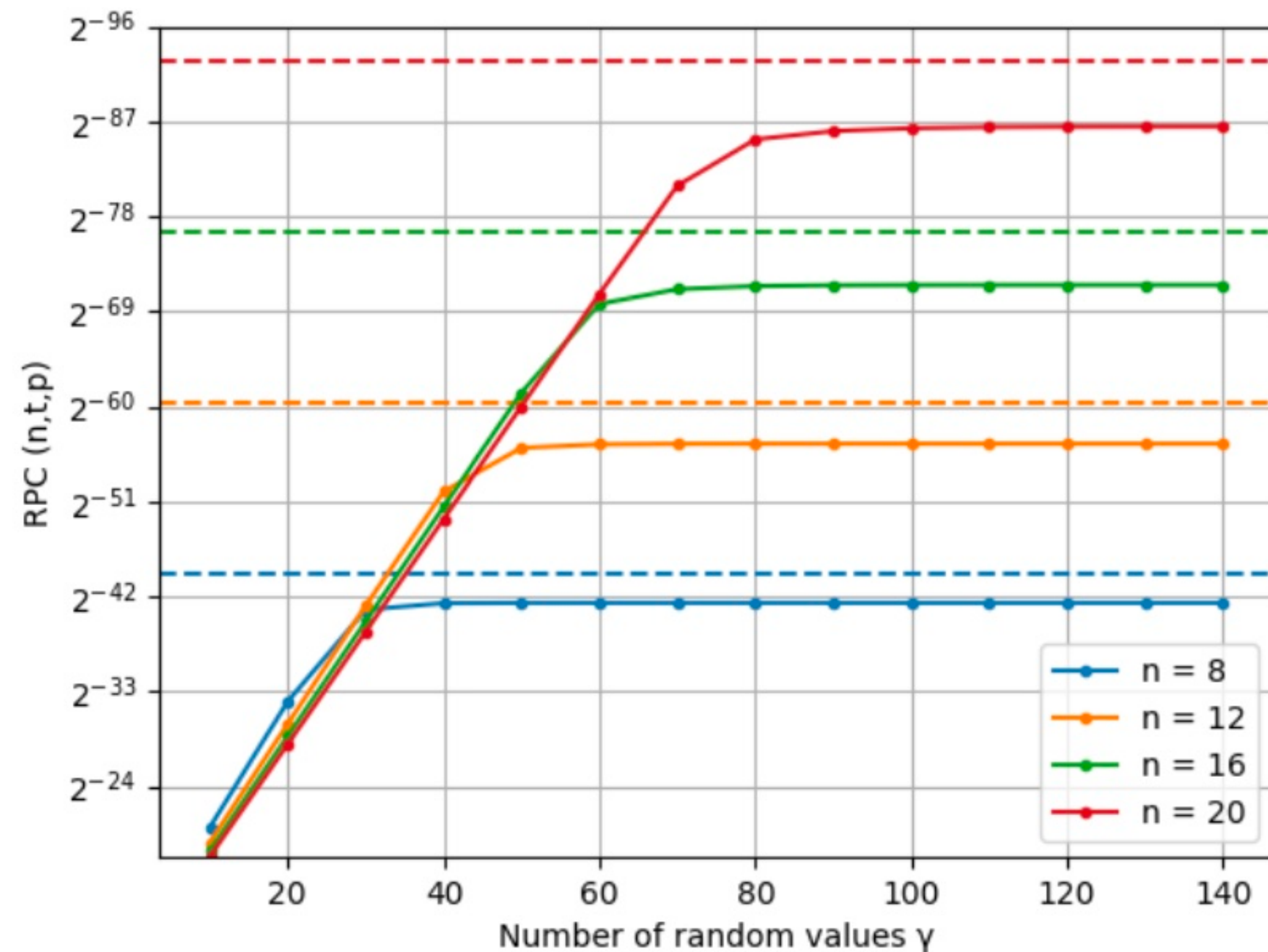
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**Input:**  $\llbracket a \rrbracket = (a_1, \dots, a_n) \in \mathbb{K}^n$

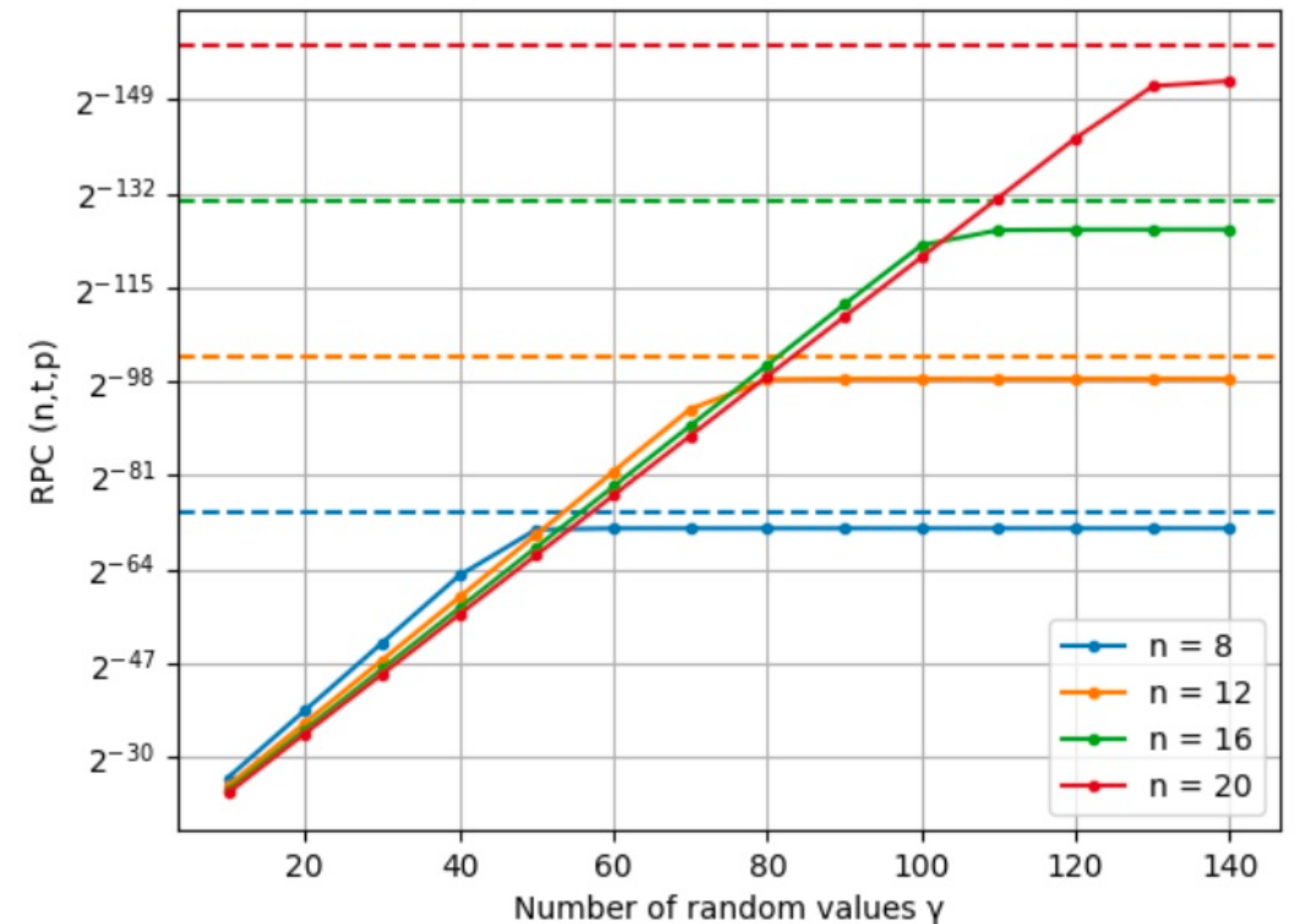
**Output:**  $\llbracket s \rrbracket = (s_1, \dots, s_n) \in \mathbb{K}^n$  such that  $s_1 + \dots + s_n = a_1 + \dots + a_n$

1.  $\llbracket z \rrbracket \leftarrow \text{RPZeroEnc}^{n,\gamma}()$
  2. **for**  $i = 1$  to  $n$  **do**
  3.    $s_i \leftarrow a_i + z_i$
  4. **end for**
  5. **return**  $\llbracket s \rrbracket$
-

# New Random Probing Composable Refresh



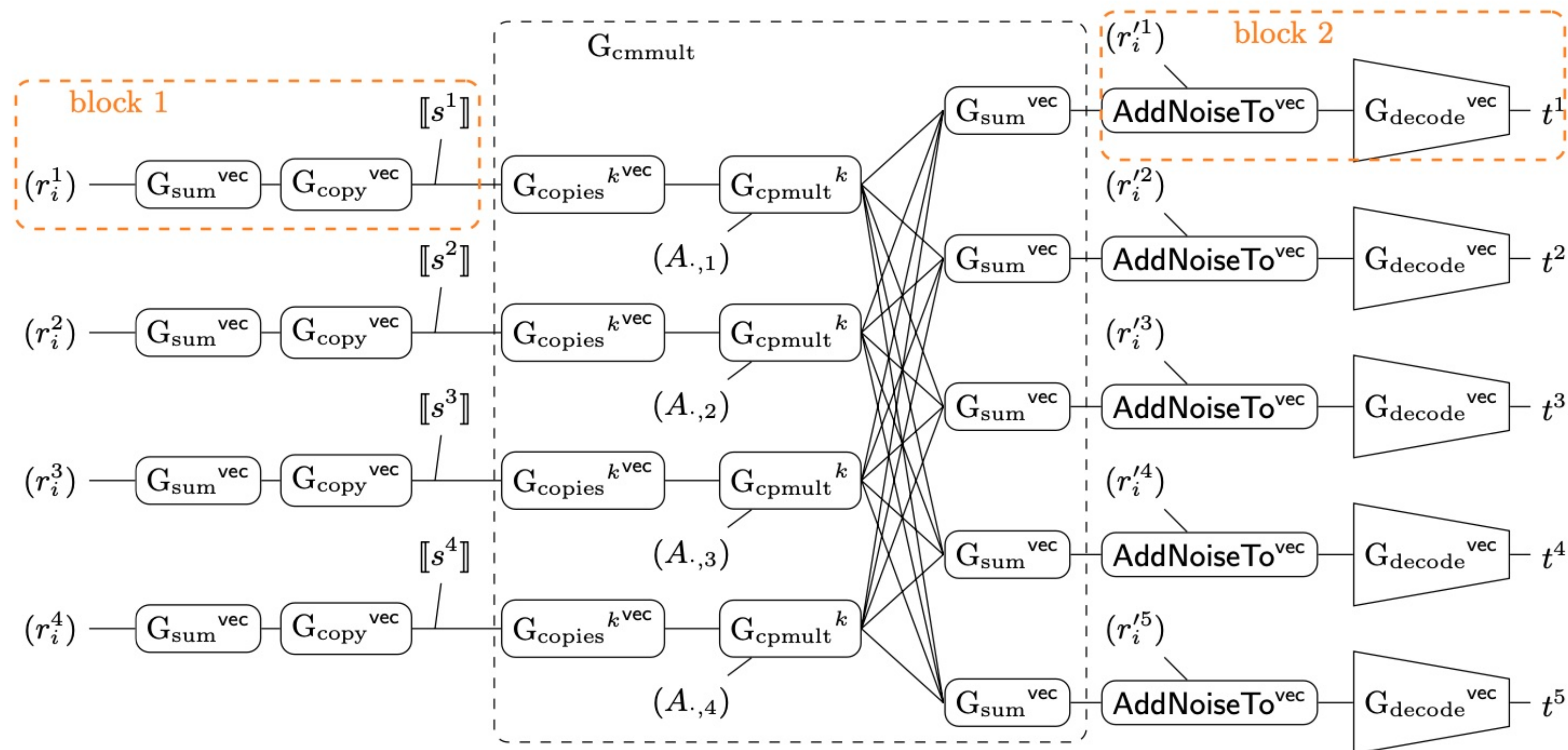
(a)  $p = 2^{-10}$



(b)  $p = 2^{-16}$

RPC-AI of RPRefresh from cardinal-RPC ( $t = n/2$ )

# Key Generation of Raccoon with random probing secure gadgets



## Raccoon 128-16:

- $n = 16$  shares
- 32  $(r_i)$  or  $(r_i')$  per vector and polynomial coefficient
- EUF-CMA secure even if 15 values of each  $(r_i)$  or  $(r_i')$  leak

# Random Probing Secure version of Raccoon

|                | Key Generation |  |             | Signature |  |             |
|----------------|----------------|--|-------------|-----------|--|-------------|
|                | Original       |  | New Gadgets | Original  |  | New Gadgets |
| # shares       | 16             |  | 16          | 16        |  | 16          |
| # additions    | $8.49e7$       |  | $1.82e9$    | $1.02e8$  |  | $3.44e9$    |
| # linear mult. | $8.39e7$       |  | $8.39e7$    | $1.01e8$  |  | $1.01e8$    |
| # randoms      | $3.60e5$       |  | $6.57e8$    | $5.57e5$  |  | $1.42e9$    |
| Security RPS/C | 1              |  | $2^{-132}$  | 1         |  | $2^{-130}$  |

## Raccoon 128-16:

- $n = 16$  shares
- 32  $(r_i)$  or  $(r'_i)$  per vector and polynomial coefficient
- EUF-CMA secure even if 15 values of each  $(r_i)$  or  $(r'_i)$  leak
- $p = 2^{-24}$

# Random Probing Secure version of Raccoon

|                | Key Generation |               |             | Signature |               |             |
|----------------|----------------|---------------|-------------|-----------|---------------|-------------|
|                | Original       |               | New Gadgets | Original  |               | New Gadgets |
| # shares       | 16             |               | 16          | 16        |               | 16          |
| # additions    | $8.49e7$       | $\times 20$   | $1.82e9$    | $1.02e8$  | $\times 30$   | $3.44e9$    |
| # linear mult. | $8.39e7$       | $\times 1$    | $8.39e7$    | $1.01e8$  | $\times 1$    | $1.01e8$    |
| # randoms      | $3.60e5$       | $\times 2000$ | $6.57e8$    | $5.57e5$  | $\times 2500$ | $1.42e9$    |
| Security RPS/C | 1              |               | $2^{-132}$  | 1         |               | $2^{-130}$  |

## Raccoon 128-16:

- $n = 16$  shares
- 32  $(r_i)$  or  $(r'_i)$  per vector and polynomial coefficient
- EUF-CMA secure even if 15 values of each  $(r_i)$  or  $(r'_i)$  leak
- $p = 2^{-24}$

1) The relevance of the random probing model

2) The challenges: scaling up

3) Random-probing Raccoon

4) Ideas for future works

1) The relevance of the random probing model

2) The challenges: scaling up

3) Random-probing Raccoon

4) Ideas for future works

# Completing the toolbox

- ➡ All gadgets can be accessed with the elementary gates but dedicated designs allow for better performance.
- ➡ Proofs are more difficult than with  $t$ -probing for large gadgets: a lot of cases to account for.
- ➡ A technique could be to look at small dedicated gadgets from PQC like the quasilinear refresh and the secadd and try to separate it in 'independent steps' and add randomness.

# Completing the toolbox

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## Idea behind secadd

$$x + y = x \oplus y \oplus c$$

Where  $c^{(0)} = 0$  and  $\forall i \geq 1, c^{(i)} = (c^{(i-1)} \& x^{(i-1)}) \oplus (c^{(i-1)} \& y^{(i-1)}) \oplus (x^{(i-1)} \& y^{(i-1)})$

# Improving composition

- ➡ Several composition techniques already exists with very different ideas.
- ➡ Compare them, find links and look at the best way of composing random probing gadgets.
- ➡ Current composition techniques lack a lot of tightness.

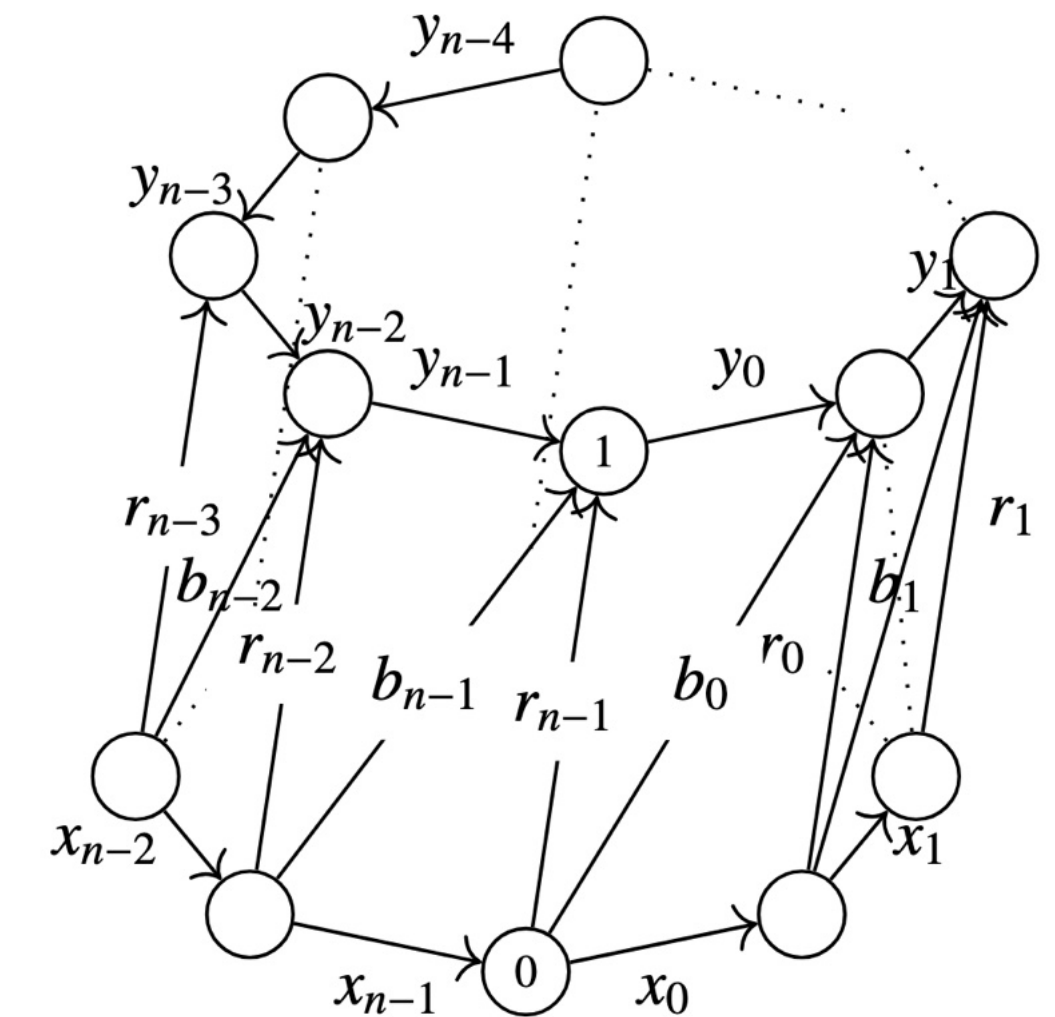


Figure extracted from [BFO23]

[BCPRT20] 8. Belaïd, S., Coron, J.S., Prouff, E., Rivain, M., Taleb, A.R. *Random probing security: Verification, composition, expansion and new constructions*. CRYPTO 2020

[BFO23] Berti, F., Faust, S., Orlt, M. *Provable secure parallel gadgets*. TCHES 2023

[DFZ19] S. Dziembowski, S. Faust, K. Zebrowski  
*Simple refreshing in the noisy leakage model*. ASIACRYPT 2019

[JMB24] V. Jahandideh, B. Mennink and L. Batina  
*An Algebraic Approach for Evaluating Random Probing Security With Application to AES*. TCHES 2024

The background of the slide is a solid light orange color, overlaid with a pattern of small, darker orange squares. These squares are scattered across the entire surface, with some appearing as simple outlines and others as slightly filled-in shapes, creating a textured, pixelated effect.

Thank you